

# Target classification of experimentally-acquired low-frequency backscattering coefficients by construction of subspaces

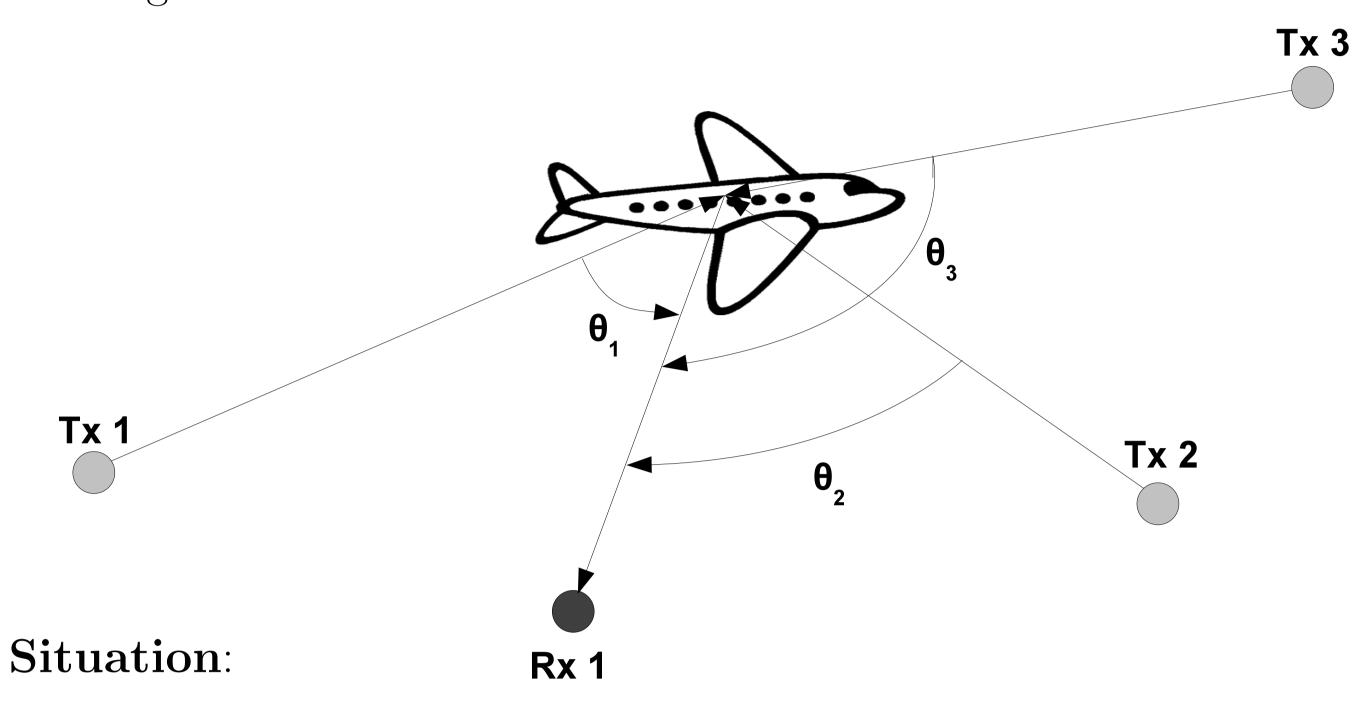
S O N R A

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#### CONTEXT

- Goal: Automatic recognition of flying targets based on data collected by sensor
- Usually, data = reconstructed images of targets
- Here, recognition system is based on complex backscattering coefficients of targets



- Various emitters and 1 receiver
- 3 frequency bands  $f_i$  at Tx: 190-250 MHz, 450-550 MHz, and 1.2-1.3 GHz
- 2 polarizations  $P_k$  at Tx: H or V
- 6 angular sectors  $\theta_i$  for Tx-Target-Rx: from 1° to 160°, per step of 25°
- 2 classes: missile-like targets, and planes-like targets: analog silhouettes

  → difficult to classify because of same geometric profile



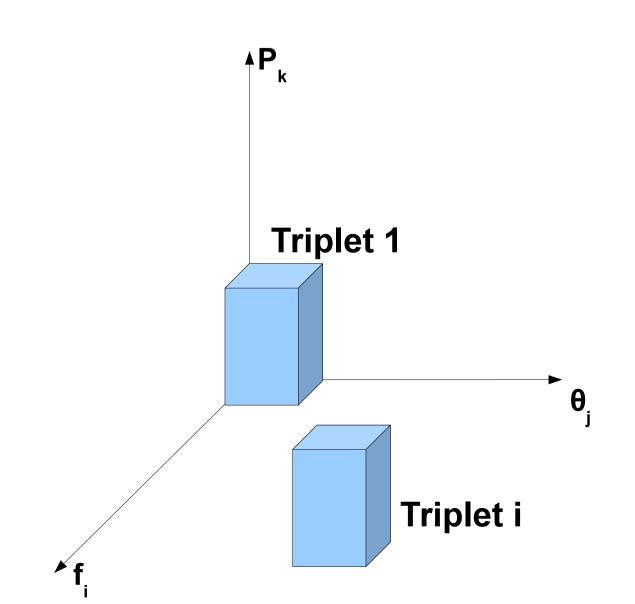


# CONSTRUCTION OF SUBSPACES

- Data divided according to  $\{f_i, \theta_j, P_k\}$
- For each  $\{f_i, \theta_j, P_k\}$ , 1 subspace per class  $\rightarrow 3*6*2*2 = 72$  subspaces
- Subspaces built according to Singular Value Decomposition [1]:

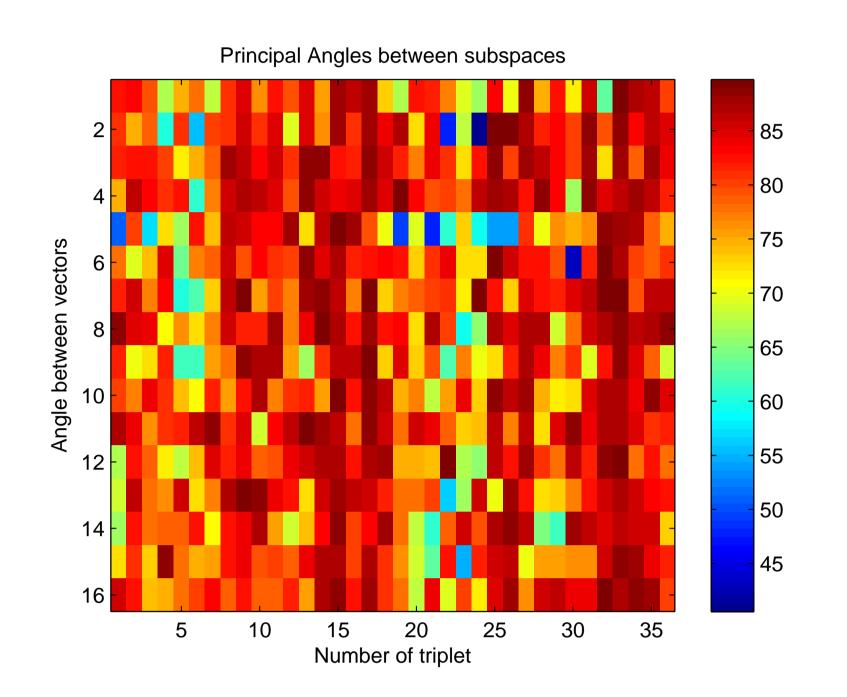
$$H = U\Lambda V^H \tag{1}$$

ullet 4 singular values  $\Lambda$  and singular vectors U per subspace



#### PRINCIPAL ANGLES [2]

- Angles vary between  $40^{\circ}$  and  $90^{\circ} \rightarrow$  subspaces well separated
- 4 singular vectors per subspace, and 2 classes per triplet  $\rightarrow$  4<sup>2</sup> angles per triplet (y-coordinate)
- 36 triplets  $\{f_i, \theta_j, P_k\}$  (x-coordinate)



## CLASSIFICATION [2]

- Triplet  $\{f_i, \theta_j, P_k\}$  known for each input data
- Projector of each input data vector z computed for each subspace (1 per class):

$$P_z = UU^H (2)$$

• Energy of projection computed  $E_z$ , for each subspace:

$$E_z = z^H P_z z \tag{3}$$

• Percentage of energy computed, for each subspace:

$$PercE_z = E_z/z^H z \tag{4}$$

- Class  $C_z$  assigned to z according to highest  $PercE_z$  among 1 specific triplet
- Data to classify recorded in bistatic anechoic chamber
- Classification rate: 95% for missile-like targets, 75% for plane-like targets.
- Overall classification rate: 83.5%

### CONCLUSIONS

### Future work include:

- Use of oblique projection
- More efficient selection of subspace dimension
- More accurate class definition
- Combination of different emitters

# References

- [1] L. Scharf and C. Demeure, Statistical Signal Processing: detection, estimation, and time series analysis. Addison-Wesley Reading, MA, 1991.
- [2] R. Behrens, L. Scharf, C. Inc, and C. Broomfield, "Signal processing applications of oblique projection operators," *IEEE Transactions on Signal Processing*, vol. 42, no. 6, pp. 1413–1424, 1994.