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Microtomographic investigation of a yeast grain porous structure

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8 Abstract

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Drying behavior of baker's yeast depends on the internal structure of the grain. In this paper, investigation of the porous structure of a dry grain using X-ray microtomography is presented. The resulting data are treated to deduce pore network characteristics for drying modeling. The treatment algorithm is based on segmentation kriging and medial axis calculation by thinning. Complementary informations are also calculated using auto-correlation function. The complete procedure is first tested on a virtual solid and then applied to yeast. The results present a large pore size distribution and a high connectivity between the pores. Both those effects can partially be attributed to the choice of the algorithms to deduce the pore network.

⁹ Key words: Yeast, microtomography, porosity, porous network

10 1. Introduction

Granular baker's yeast is industrially dried to reduce transport costs and to increase conservation time. This energy intensive process may cause viability loss of the product (Bayrock and Ingledew, 1997): drying conditions are crucial to achieve well inactivated yeast without causing the cells death (Volkov et al., 1990). Knowledge of the local conditions (temperature, air moisture content) inside and around the grains is therefore important to predict the yeast survival chances (Marechal et al., 1999). Thus, detailed modeling of the drying process

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¹⁸ would be a powerful tool to understand, control and optimize baker's yeast¹⁹ drying.

Most models applied to yeast drying hide the impact of the inner-grain structure on the evaporation in desorption isotherms or in fitted diffusion coefficients that have a limited physical meaning. This approach neither allows correct understanding of viability loss mechanisms nor offers a general explanation of the observed drying rate curves (Debaste et al., 2008).

Two modeling approaches have been tested recently to tackle those limita-25 tions. The first one, (Debaste et al., 2008), is based on the explicit expression 26 of the limiting transport phenomena affecting drying considering two succes-27 sive steps. This model gives satisfactory results for process optimization but 28 no insight is gained on viability. Indeed, the assumption of a known limit-29 ing phenomenon allows hiding the impact of the porous structure in physically 30 based fitting parameters, offering only a rough description of the inner grain 31 phenomena. 32

In a second step, porous network modeling of yeast drying has been investigated (Debaste and Halloin, 2009). Although offering encouraging and well fitting results, this model was based on drastic and unrealistic assumptions about geometry and pore network topology: two dimensional slices of the grain were simulated and pore network parameters were very roughly estimated, limiting the validity scope of the results.

The global aim of this work is to obtain a more detailed, three dimensional, pore network model of the drying of yeast. This paper is focused on the investigation of the porous structure and on the deduction of a porous network to be used to model the drying.

To characterize the porosity of *Saccharomyces cerevisiae*, a living organism, the use of classical intrusive pore size identification methods, such as mercury porosimetry, gives doubtful results. Although yeast is known to survive at very high pressure (Espinasse et al., 2007), little is known about its behavior in contact with high pressure mercury. Therefore X-ray microtomographic investigation of a yeast grain is realized. This non-intrusive technique has already been

shown to be an alternative to mercury porosimetry for foam materials shrinking
under the pressure (Léonard et al., 2008b). The resulting three dimensional
numeric representation of the grain is then used to deduce pore network parameters.

X-ray microtomography has already been used to deduce information about 53 the porous structure of food such as bread (Falcone et al., 2008; Babin et al., 54 2006), cellular foam food (Lim and Barigou, 2004; Trater et al., 2005), meat 55 (Frisullo et al., 2009), dried bananas (Léonard et al., 2008a), apples and pears 56 (Verboven et al., 2008). Except for the work of Verboven et al. (2008), who 57 directly used the void space dimensions as a domain for solving numerically 58 reaction-diffusion equations, focus was set on qualitative and simple quantitative 59 datas. However, no complete networks parameters were deduced. 60

This last point has already been tested in geological science (Al-Raoush and Willson, 2005; Al-Raoush and Alshibli, 2006). In this paper, an application of similar algorithms to deduce detailed porous network in yeast grain is presented, highlighting the potential of this method for further detailed investigations.

⁶⁵ 2. Materials and methods

The applied image treatment procedure is similar to the one presented by 66 Al-Raoush and Willson (2005). However, different algorithms are considered 67 for the final network generation. The principle of the procedure is sketched 68 on Figure 1. The original gray-level images (a) are segmented: every voxel is 69 assigned to solid or void (Gonzalez and Woods, 1993). The medial axis, a one 70 voxel thick assembly characteristic of all the paths present in the void network 71 (Couprie et al., 2007), is then deduced (c). Finally, pore network properties 72 are computed (d). The auto-correlation function and the tortuosity are also estimated. 74

This procedure, implemented in MATLAB 7.6, is tested on a computer generated set of images and then applied to experimental images obtained through
X-ray microtomographic investigation of a yeast grain. The different steps are
detailed in the following subsections.

79 2.1. Image segmentation

The simplest segmentation procedure, further called the *threshold technique*, is based on one fixed threshold: every voxel whose gray level is darker than the threshold is assigned to fluid; the rest is assigned to solid.

This method is simple but highly sensitive to background noise on the im-83 ages (Oh and Lindquist, 1999). An alternative, less noise sensitive, is indicator 84 kriging, further called the kriging technique, for which two thresholds are de-85 fined. Every voxel with a gray level lower than the lowest threshold is assigned 86 to the solid and every voxel with a gray level higher than the highest threshold 87 is put in the fluid. For intermediate values, indicator kriging, computation of 88 the most probable value of a voxel based on the values of the surrounding vox-89 els, is used (Oh and Lindquist, 1999). This method has two drawbacks. First, 90 when the size of the smallest objects to be found is only of a few voxels, the 91 treatment might suppress physically relevant informations. Second, the kriging 92 technique requires intensive calculations. For those reasons, the two techniques 93 are compared in our application. 94

95 2.2. Medial axis calculation

The medial axis is calculated using the thinning algorithm presented by 96 Palagyi and Kuba (1998). The principle of this algorithm is to modify iteratively 97 the segmented image until the only fluid voxels left form the medial axis. At 98 every iteration, every fluid voxel neighboring a solid voxel is considered. If the 99 configuration of the types of its neighbors fits some specifics configurations, 100 called masks, the studied voxel is changed to solid. The key of this algorithm 101 is the choice of the masks allowing to keep only the medial axis. The chosen 102 algorithm and the corresponding set of masks are detailled by Palagyi and Kuba 103 (1998).104

105 2.3. Porous network identification

Different definitions of network properties are possible, depending on the goal of the network. In this paper, using the same definition as presented in Debaste and Halloin (2009), pores are defined as fluid volumes presenting no resistance to

flow. Capillary pressure, pressure drop and concentration gradient are assumed 109 to be negligible in the pores. The pores are connected to each other by throats, 110 that are zero volume objects where all the fluid flow resistance is concentrated : 111 capillary pressure, pressure drop and concentration gradients in the throats are 112 limiting the global mass transport within the network. The pores are therefore 113 characterized by a volume and a connectivity (or pore coordination number) to a 114 known number of throats. The throats are characterized by different parameters 115 (global pressure drop coefficient, effective surface tension, diffusion length) to 116 evaluate the transport phenomena limitation steps. Usually, those different 117 parameters are correlated to the characteristic length and diameter of idealized 118 throats (Metzger et al., 2007). 119

Each voxel of the medial axis which is at the intersection of multiple branches is defined as being a pore. At this stage, each pore corresponds to a single voxel. The connectivity of the different pores is evaluated by travelling on the different medial axis branches until reaching the other pores. While doing this, the distance from every voxel to the nearest solid voxel on the segmented image is calculated. The smallest value for a voxel of the medial axis between two pores is stored as being the radius of that throat.

As shown by Al-Raoush and Willson (2005), this pore definition leads to the 127 definition of too many pores : multiple medial axis division occurs in a volume 128 usually considered as a single pore. To solve this issue, pores are merged if the 129 distance between them is smaller than distance between the pore and the nearest 130 solid voxel. The new pore is located in the middle of the straight line between 131 the two former pores. It inherits the connections of both previous pores, except 132 the one linking the two former pores. All the pores are checked for merging one 133 by one, iteratively, until no new merging happens. 134

The volume of each pore is then evaluated. Following the proposed network definition, the volume of the pore is limited by the pores walls and the connected throats. In the throat, the limit should be defined by the plan normal to the medial axis direction. However, due to the discretization of the medial axis, unsatisfactory volume division are achieved. Therefore, in this work, a simplified

evaluation is chosen, based on two iterative steps. First, all the voxels that are 140 in the largest fully fluid sphere centered at a pore position are assigned to that 141 pore. The pore merging step ensure that no overlapping occurs between pores. 142 Second, every unassigned voxel neighboring an assigned voxel is assigned to the 143 same pore. Unassigned voxels neighboring voxels assigned to different pores 144 are assigned randomly to one of those pores. As those voxels correspond to 145 a less than half a percent of the total number of voxels, their impact on the 146 final volume distribution is considered to be negligible. The voxel assignment is 147 iterated until all the fluid voxels are assigned to a pore. Counting the voxels of 148 a pore gives its volume. 149

150 2.4. Auto-correlation function

The auto-correlation function gives the probability of having two voxels, 151 separated by a given distance, to be both in the fluid phase. It is correlated 152 to informations on the structure such as the specific surface, the porosity, the 153 typical size of a constitutive element of the solid and an estimate of the length 154 to which porosity tends to reach its macroscopic value. This last value is useful 155 to estimate the representative elementary volume (REV) to be used in porous 156 media modeling following the continuous approach. Indeed, the REV can be 157 defined as the volume over which an averaged property can be considered to 158 be independent of the position (Bear, 1972). At the length scale of the REV 159 for porosity, the autocorrelation function must be approximately constant. The 160 mathematical expression of the autocorrelation function was taken from Berry-161 man and Blair (1986). 162

2.5. Tortuosity measurement

163

Tortuosity is defined to take globally into account the increased fluid path length due to the presence of the solid. It is defined the ratio between the average effective length that fluid has to follow to connect two points in the fluid phase and the Euclidian distance separating those two points.

A direct computation of porosity is obtained by travelling on the medial axis and by counting the smallest number of voxels required to go from one

pore to another. However, in this case, this is not straightforward because the 170 uniqueness of the medial axis path between two directly connected pores is lost 171 at the pore merging step. Therefore, in this work, it is proposed to calculate 172 the porosity based on the product of two terms. The first one is the throat 173 tortuosity, calculated for two directly connected pores before the pore merging 174 step, and defined as the ratio between the medial axis length and the Eucledian 175 distance between those two pores. The second one is the *network tortuosity* 176 defined as the tortuosity between two non directly connected pores, considering 177 that the directly connected pores are joined by straight lines. 178

Network tortuosity is evaluated for couples of pores distant by one third
to one half of the sample dimension. For higher distances, considering a cubic
sample implies that some directions present more data than others, leading to
a bigger influence of those direction on a global averaged tortuosity. Inversely,
for pores that are too close, the deduced porosity represent a too local value.

184 2.6. Virtual solid for validation

To validate the method, the complete algorithm is tested on a virtual sample 185 of known properties. The fluid phase is defined by the junction of regular 186 octahedrons of uniformly distributed size but centered on a regular cubic lattice. 187 The minimal and maximal value of the size distribution is chosen to ensure 188 that every octahedron is in contact with its six neighbors. Figure 2 presents 189 the visualisation of the void structure for $2x2x^2$ octahedrons already voxelized 190 (presented as small cubes). Figure 3 illustrates a slice in a structure of $10 \times 10 \times 10$ 191 octahedrons (white is void, black is solid). 192

For this solid, the throats have a square section with a side length d_{lia} given by

$$d_{lia} = \left(\frac{\sqrt{2}}{2}\overline{d_o}\right) - L_o,\tag{1}$$

where $\overline{d_o}$ is the average of the length of the border of the two connected octahedrons and L_o is the distance between the center of two successive octahedron.

Similarly, the volume of a pore, obtained by truncating the full octahedron, writes as

$$V_{pore} = \left(\frac{\sqrt{2}}{3}d_o^3\right) - \frac{\sqrt{2}}{6}\sum_{lia}d_{lia}^3.$$
 (2)

Exact throat tortuosity is 1 and the averaged isotropic network tortuosity is of 1.52. The generated samples contain 1000 pores with normally randomized sizes and distributed in 100x100x100 voxels. For a comparison with the experimental images obtained by microtomography, the voxel length is chosen to be 2.95 μm , which is the calibrated voxel size for the yeast samples.

200 2.7. Noise addition to the virtual solid images

To test noise influence, present on experimental samples, a perturbed volume is computed based on the previously defined void space. A gray level in a range of 64 values , based on a normal random distribution, is given to every voxel. A different distribution is applied for fluid and for solid voxels. Both distributions have the same standard deviation but different averages. The solid distribution center is set on the 22nd gray level while the fluid is centered on the 43rd. Different noise standard deviation are tested going from 2.5 to 7.5 gray levels.

208 2.8. Microtomographic imaging of yeast grains

The analyzed *Saccharomices Cerevisiae* grains are industrially produced by 209 Beldem (Andenne, Belgium) and then dried in a desiccator during one week at 210 25°C and 5 % of relative humidity. The microtomographic investigation was re-211 alized using a Skyscan-1172 high-resolution desktop micro-CT system (Skyscan, 212 Kontich, Belgium). A dried yeast sample was placed vertically in a polystyrene 213 holder, the latter being almost transparent to X-rays. The cone beam source operated at 60 kV and 167 $\mu A.$ The detector is 2D, 1048x2000 voxels, 16-bit 215 X-ray camera. The distance source-object-camera was adjusted to produce im-216 ages with a voxel size of 2.95 μ m. The rotation step was fixed at 0.4°. For each 217 angular position, a radiograph of the sample, was recorded by a 2D camera. 218 The Feldcamp back projection algorithm was used to reconstruct 2D images of 219 the cross-sections of the sample from the radiographs. The corresponding yeast 220

 $_{221}$ 3D image is obtained by stacking the 2D cross-sections. The obtained 3D image

 $_{222}$ is $1024 \times 1024 \times 1024$ voxels wide.

223 3. Results

224 3.1. Application of the algorithm to the virtual solid

Ten solids, with no noise addition, were generated and tested with the full algorithm. No significant differences were observed between those ten solids.

The network deduction of the virtual solid leads to 1070 pores in average, instead of 1000. Figure 4 presents the coordination number of the different pores. Globally, predictions are satisfactory although toward lower values, a bias is observed. The merging algorithm leads to two error types that can explain the discrepancies. First, two pores that should be merged are not, leading to pores with lower coordination. Second, two pores that should not be merged are, leading to a highly coordinate pore.

As the total pore number is higher than theoretically, for this sample, the first error is slightly more present. Enhancing the resolution (number of voxel per pore) would lower both errors. For the virtual solid, only the computational power limits the resolution. For the yeast sample, measurement resolution is the limiting factor.

Figure 5 presents the throat size distribution. As the throat size is the smallest element to be identified, it is more affected by resolution limitation than other parameters. For the chosen resolution, only four different sizes can be distinguished. Indeed, the largest possible throat radius is only 8 time the estimated error on the radius measurement which is of around 2 voxels. The obtained size is globally underestimated. Tests with a higher resolution confirm the ability of the algorithm to reduce this error.

Figure 6 shows the pore volume distribution. Theoretically, as obtained from equation (2), the pore size should be, in the studied case, divided in four well marked peaks. However, although two of those peaks are predicted, these are included in a bell-shaped curve. The average value of the distribution is however

 $_{\rm 250}~$ well predicted. The simplified algorithm proposed in this work is thus unable

²⁵¹ to predict multimodal porosity.

The predicted throat tortuosity is 1.045, which is only slightly overevaluated. The network tortuosity is estimated at 1.41, which corresponds to a 10 % underestimation.

255 3.2. Impact of the segmentation algorithm

The virtual solid volume with different noises is submitted to the two seg-256 mentation algorithms with various segmentation thresholds. Figure 7 presents 257 the percentage of wrongly attributed voxels for various threshold values with 258 different noises. For the kriging, where two thresholds have to be set, the ab-250 scissa value corresponds to the lower threshold value. The higher threshold is 260 fixed seven grey levels higher. As expected, the number of errors are minimal for 261 both methods exactly at the average of the mean of the distributions. Except 262 when the noise is really small, the kriging leads to less errors than the one level 263 technique. However, kriging only leads to maximum 25% less errors than the 264

²⁶⁵ other method.

Bloc	1		2		3	
Method	Kriging	Thres.	Kriging	Thres.	Kriging	Thres.
Simple threshold		72		78		76
Lowest kriging threshold	71		75		73	
Highest kriging threshold	75		79		77	
Porosity	0.581	0.581	0.5805	0.579	0.5975	0.597
Specific surface (m^{-1})	123000	123000	115600	115600	114100	114100
Mean coordination number	4.63	4.46	4.41	4.32	4.72	4.55
Median coordination number	4	4	4	4	4	4
Pores number	1536	1678	1582	1676	1518	1658
Throats number	7104	7496	6981	7242	7168	7545
Average pore volume (μm^3)	9200	8500	9400	8900	10100	9300
Throat tortuosity	1.33	1.31	1.30	1.30	1.37	1.36
Network tortuosity	1.53	1.53	1.55	1.54	1.61	1.58

Table 1: Comparison of yeast analysis results for 3 different samples.

266 3.3. Application to yeast

Figure 8 illustrates a reconstructed 2D slice obtained by X-ray microtomog-

²⁶⁸ raphy for a dry yeast grain.

Segmentation parameters and results for three regions of 100x100x100 voxels inside the yeast grain are summarized in Table 1. The segmentation threshold is unknown, it is chosen to achieve a global porosity around 0.6 which was estimated experimentally using a gravimetric method. Table 1 shows a fairly good reproductivity of the results. Details are therefore given only for one sample.

Figure 9 presents the coordination number of pores for the two segmenta-275 tion techniques. Both methods show similar results. A very large range of 276 value is observed. Such distributions have been reported previously with sim-277 ilar algorithm applied to porous rocks (Baldwin et al., 1996; Al-Kharusi and 278 Blunt, 2006). The large values of coordination numbers can be attributed to 279 the definition given to a pore. Indeed, as every crossing of the medial axis is 280 initially considered as a pore, every irregularity in the solid structure leads to 281 the definition of a pore. The pore merging step reduces that effect, but leads to 282 highly connected pores. Globally, pores with a coordination number superior 283 to 8 represents less than 10% of the total and therefore only play a minor role. 284 Pores having a coordination number of 2 are also present. These pores appears 285 at the crossing of medial axis branches leading outside the sample. Such pores 286 do not affect the connectivity of the network and are therefore generally sup-287 pressed. Their volume is added to the pore connected with the largest throat. 288 The smaller throat is assigned to link the two pores connected to the suppressed 289 290 one

The throat diameter distribution is presented on Figure 10. No major difference can be stressed out between the two segmentation techniques. Most observed throats have a diameter of maximum 3 voxels, which is estimated just above the error of the throat size evaluation. The largest throats are only 3 times larger. Therefore, few informations can be deduced as the measurement resolution is limiting.

Similarly, the pore volume distribution is presented on Figure 11. As for the throats, a non negligible fraction of the pores have a size corresponding to the estimated precision of our algorithm. However, a very large size distribution

can be observed. As shown for the virtual solid, this distribution has to be
interpreted with care as the methodology does not allow to predict multimodal
porosity.

Also, the auto-correlation function predicts a porosity REV typical length scale of about 100 μm .

305 4. Analysis and discussion

The analysis of a limited region of $100 \times 100 \times 100$ voxels allows the compu-306 tation of a set of average values characterizing the network of a yeast grain. 307 The validity of using a reduced part of the grain is supported by both the re-308 productivity of the results for different regions of the grain and the fact that 309 the autocorrelation function predicts a REV typical length three times smaller 310 than the considered region. This value ensures that for common applications, 311 where a grain is of a millimetric size, the continuous modeling approach can be 312 used to describe the global behavior of the grain. 313

The choice of the segmentation technique seems to have only a limited impact on the deduced network and other averaged properties. Three main reasons can explain this :

the rest of the image treatment is not affected by the observed variations
 in segmentation,

319 2. the thresholds used were correctly estimated,

320 3. the noise on the samples is too high for the difference between the methods
321 to be significant.

The average coordination number obtained is of the order of 4, which corresponds to the coordination number of the void space of a monodisperse dense sphere packing. This value is therefore acceptable. A few pores have an unrealistically high coordination number, due to their deduction from a highly noise sensitive medial axis.

The throat size distribution is barely exploitable due to limitation in the resolution method. However, more careful treatment algorithm (based on the

whole throat section measurement rather than on their radius) could already offer better results using the same images. The obtained results only allows a rough description of the throats. This information is however the first to be available.

For the pore volume size distribution, also, a gross estimate has been obtained. Alternative algorithm for this step should be considered.

The results can be used as input parameters for different models. Except for the pore volume distribution, for which the results are not reliable, all the other parameter measurement present a net enhancement compared to the data previously used in Debaste and Halloin (2009).

The tortuosity and the approximate size of the REV are useful information to be used in continuous models, such as the one presented in Debaste et al. (2008). The total tortuosity obtained by this analysis is around 2, which is of an acceptable order of magnitude. However this value is lower than the value used in Debaste et al. (2008), where tortuosity, used as a fitting parameter, was evaluated around the value of 5, suggesting a need for further model refinement.

345 5. Conclusion

A general simplified method to deduce porous structure, based on existing algorithms, was presented, tested and applied to 3D images of granular yeast obtained by X-ray microtomography. This algorithm allows detailed investigation of the porous structure without altering the structure of the material, offering valuable information for inner grain drying modeling.

Pore and throat size distributions, connectivity, specific surface, tortuosity and REV size have all been determined. However, both algorithm approximations and experimental resolution limitations limit the scope of the results. The obtained results can however be directly integrated in existing models for which simpler assumptions had been previously taken. Enhancement of the presented algorithm could lead to more precise data, fully satisfactory for all the considered modeling approaches.

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Figure 1: Different steps of image treatment to extract the network information.



Figure 2: Virtual solid visualisation.



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Figure 3: Virtual solid slice visualisation (void is in white, solid is in black).



Figure 4: Predicted and theoretical coordination number of the virtual solid.



Figure 5: Predicted and theoretical throat diameter of the virtual solid.



Figure 6: Predicted and theoretical pore volume distribution of the virtual solid.



Figure 7: Fraction of wrongly attributed voxels using different segmentation techniques.



Figure 8: A reconstructed 2D yeast grain slice, obtained by microtomography.











Figure 11: Pores volume distribution for a yeast sample.