

Gaia GraL: *Gaia* DR2 Gravitational Lens Systems. IV. Keck/LRIS spectroscopic confirmation of GRAL113100-441959 and model prediction of time-delays

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ABSTRACT

We report the spectroscopic confirmation and modeling of the quadruply imaged quasar GRAL113100-441959, the first gravitational lens (GL) to be discovered mainly from astrometric considerations. Follow-up spectra obtained with Keck/LRIS reveal the lensing nature of this quadruply-imaged quasar with redshift $z_s = 1.090 \pm 0.002$, but show no evidence of the central lens galaxy. Using the image positions and *G*-band flux ratios provided by *Gaia* Data Release 2 as constraints, we model the system with a singular power-law elliptical mass distribution (SPEMD) plus external shear, to different levels of complexity. We show that relaxing the isothermal constraint of the SPEMD is not statistically significant, and thus we simplify the SPEMD to a singular isothermal ellipsoid to estimate the Einstein radius of the main lens galaxy $\theta_E = 0''.851$, the intensity and position angle of the external shear $(\gamma, \theta_\gamma) = (0.044, 11^\circ.5)$, and we predict the lensing galaxy position to be $(\theta_{\text{gal},1}, \theta_{\text{gal},2}) = (-0''.424, -0''.744)$ with respect to image A. We provide time delay predictions for pairs of images, assuming a plausible range of lens redshift values z_l between 0.5 and 0.9. We finally examine the impact on time delays of the so-called Source Position Transformation, a family of degeneracies existing between different lens density profiles that reproduce most of the lensing observables equally well. We show that this effect contributes significantly to the time delay error budget and cannot be ignored during the modelling. This has implications for robust cosmography applications of lensed systems. GRAL113100-441959 is the first in a series of seven new spectroscopically confirmed GLs discovered from *Gaia* Data Release 2.

Key words. Gravitational lensing: strong, Quasars: general, Astrometry.

1. Introduction

Already suspected before General Relativity (Einstein 1916), it was only after Einstein's final formulation of its theory that strong gravitational lensing (GL) was described quantitatively. Then it took no less than three-quarters of a century to obtain a definitive observational proof when Walsh et al. (1979) discovered a pair of quasars separated by 6 arcseconds, with identical colors, redshifts, and spectra, thereby confirming the first doubly-imaged quasar. Because the study of GLs constitutes a unique tool in various fields of astronomy (see, e.g., Treu & Marshall 2016; Gilman et al. 2017; Jauzac et al. 2018; Zavala et al. 2018; Tagore et al. 2018, and references therein), they

are highly sought, but not without difficulty. Even in this era of all-sky surveys, their discovery remains a great challenge, with barely a few hundred systems currently confirmed. A state-of-the-art list of currently known GLs can be found in Ducourant et al. (2018, hereafter paper II).

Data from the ESA/*Gaia* space mission (Gaia Collaboration et al. 2016) is expected to change the situation dramatically. *Gaia* is conducting the largest, most precise, most accurate all-sky astrometric survey from space. Its main goal is to chart a three-dimensional map of our Galaxy based on measurements of parallaxes, proper motions, positions and spectro-photometric parameters for more than a billion stars. With an order of magnitude improvement over typical *HST* astrometric accuracy, *Gaia*

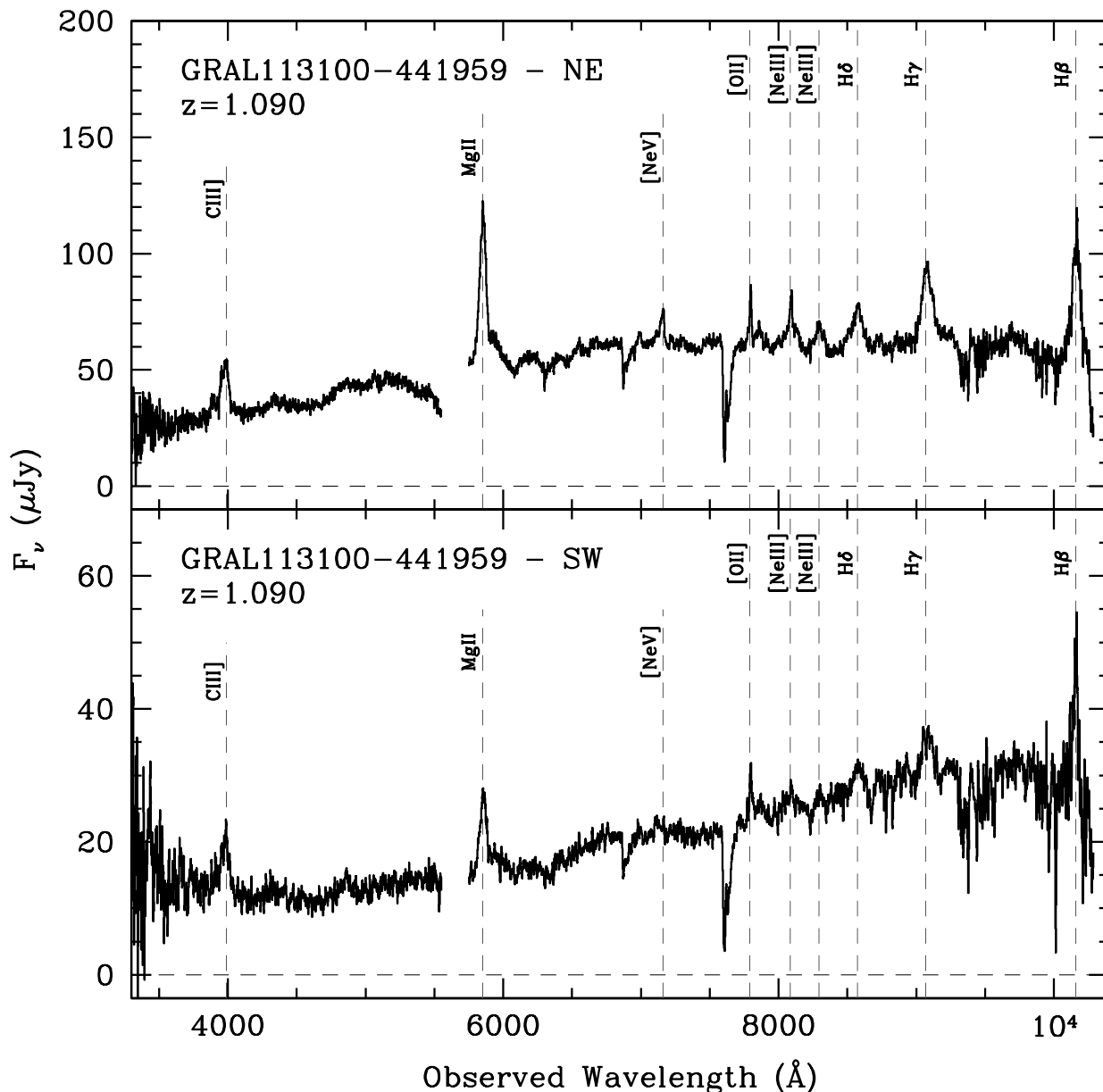


Fig. 1. Keck/LRIS spectra of images (A+B) and (C+D) at position angle 60° . Dashed lines identify emission lines used to confirm the lensing nature of GRAL113100-441959.

will also detect $\sim 600,000$ quasars (Mignard 2012; Robin et al. 2012), of which 2900 are expected to be multiply-imaged and resolved in the final *Gaia* Data Release (*Gaia* DR), including 250 systems with more than two lensed images (Finet & Surdej 2016).

As part of a larger effort to discover and study multiply-imaged quasar systems hidden in the heart of *Gaia* DRs, the *Gaia* *GrL* group has recently developed and successfully applied various techniques to identify new highly probable gravitational lens candidates from *Gaia*'s data. Our strategy is twofold and can be summarized as follows. Initially, our research focused on all known quasars that we compiled in a state-of-the-art list populated primarily with the Million Quasars Catalog (Flesch 2015, 2017), searching for the presence in *Gaia* DR2 of one or more nearby ($< 6''$) point-like companion(s). This was the ini-

tial approach we took in Krone-Martins et al. (2018), hereafter paper I. Next, we designed a dedicated method to blindly identify clusters of point-like objects from the information available in the *Gaia* DRs using the Hierarchical Triangular Mesh technique (Kunszt et al. 2001). This was the approach we took in Delchambre et al. (2018), hereafter paper III.

The list of clusters generated from these two approaches is expected to be polluted with contaminants, resulting primarily from chance alignments of unrelated sources. To discard the most obvious ones, we thus applied soft astrometric filters to differentiate genuine candidates from fortuitous clusters of stars by studying the image proper motions and parallaxes of known lenses, as measured by *Gaia* (see paper II). *Gaia* DR2 also provides broad band photometric measurements in the *G*-band (330 to 1050 nm), in particular, a color indicator derived from the inte-

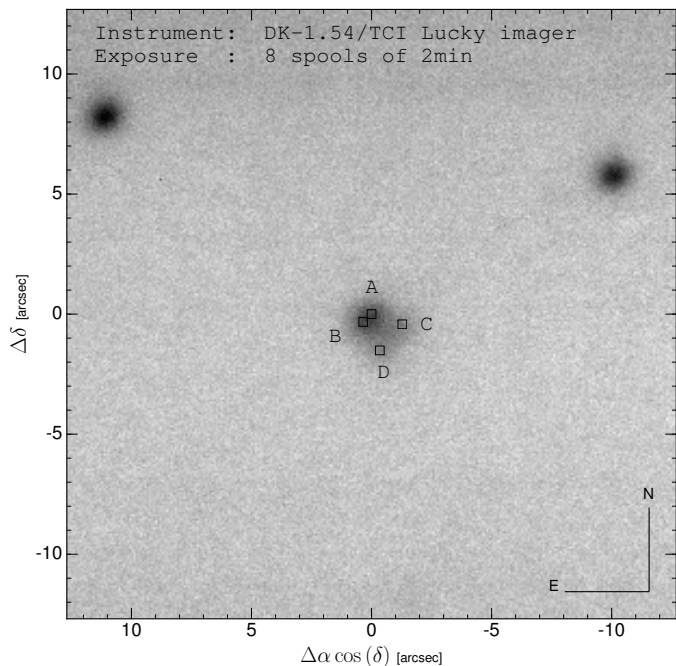


Fig. 2. The first direct imaging of GRAL113100-441959 obtained with the DK-1.54/TCI Lucky imager during the night of UT 2018 July 31. The black squares locate the lensed imaged positions as reported in the *Gaia* DR2.

grated flux of the low-resolution blue photometer (BP, 300 – 680 nm) and red photometer (RP, 630 – 1050 nm) spectra (Jordi et al. 2010; Evans, D. W. et al. 2018). Because the gravitational lensing phenomenon is achromatic, we also rejected clusters for which the individual component BP–RP color indicators significantly differ from each other. With the purpose of considering only the most plausible candidates, we classified the remaining clusters that successfully passed the astrometric and photometric filters with respect to their chance of being a multiply-imaged quasar candidate. To this end, we assigned to each of them a probability that reflects the match between a candidate and the learning set composed of more than 10^8 simulated image configurations that we used to build Extremely Randomized Trees (Geurts et al. 2006). When considering a non-singular isothermal ellipsoid (NIE) plus external shear as the lens model, various tests have shown this method to be efficient in identifying known GLs from fortuitous clusters of stars with a detection probability of 97% in the case of configurations with four lensed images along with a contamination ratio of 1.37%. By implementing this strategy to *Gaia* DR2, we discovered 15 new highly probable quadruply-imaged quasar candidates, recently presented in paper III. Furthermore in this blind search, we also found 17 well-known quadruply-imaged quasars for which three or four components are detected in *Gaia* DR2. This constitutes additional evidence of the robustness of our methodology.

GRAL113100-441959 was identified for the first time as a new highly probable GL candidate in paper I, and was then rediscovered independently with an ERT probability of 96% from the blind search technique presented in paper III (candidate number [12] their Fig. 3). This is likely the first gravitationally lensed quasar discovered from astrometric/photometric survey data. Prior to its spectroscopic confirmation, we were not able to perform any visual inspection of this candidate because the available surveys either lack spatial resolution and/or sensitiv-

ity (e.g., SkyMapper, Wolf et al. (2018), and ALLWISE, Wright et al. (2010)), or they lack spatial coverage (e.g., Pan-STARRS, Chambers et al. 2016). The limited spatial resolution of current all-sky southern surveys probably explains why GRAL113100-441959 remained unnoticed so far, confirming that a large number of GLs that can be observed from the ground still waits to be discovered.

In Sect. 2 we describe the spectroscopic observations and confirm the lensing nature of GRAL113100-441959. In Sect. 3, we describe the details of the simple lens modeling, and provide predictions for the time delays between pairs of lensed images in Sect. 4. Finally, we summarize our findings and conclude in Sect. 5.

2. Lens confirmation

2.1. Observations

On UT 2018 May 13, we observed GRAL113100-441959 with the dual-beam Low Resolution Imaging Spectrometer (Oke et al. 1995) on the Keck I telescope. The conditions were photometric, and we obtained two 300s spectra, at position angles (PAs) of 60° and 135° . We used the $1''$ width slit, the 5600\AA dichroic, the $600 \ell \text{ mm}^{-1}$ blue grism ($\lambda_{\text{blaze}} = 4000 \text{\AA}$), and the $400 \ell \text{ mm}^{-1}$ red grating ($\lambda_{\text{blaze}} = 8500 \text{\AA}$). This instrument configuration covers the full optical window at moderate resolving power, $R \equiv \lambda/\Delta\lambda \approx 1100$. The observations were processed using standard techniques within IRAF, and flux-calibrated using observations of the spectrophotometric white dwarf standard stars Feige 34, Feige 67, and Wolf 1346 obtained on the same night.

The target appears as a single source in the $\text{PA} = 135^\circ$ observation, which was aligned along the brighter NE components of the lens. Though the two components are not differentiated in the spectroscopy, the source is clearly spatially resolved, with a FWHM of $\sim 1''.4$ compared to the $\sim 1''.0$ seeing.

In the $\text{PA} = 60^\circ$ observation, the target is clearly resolved into two sources separated by $\sim 1''.2$ with identical spectroscopic features. One component is significantly brighter than the other. Fig. 1 presents the spectra of the brighter (NE) and fainter (SW) components, each extracted with $0''.5$ box width. Based on Gaussian fits to the typical broad, quasar emission lines such as $\text{C III } \lambda 1909$, $\text{Mg II } \lambda 2800$, and Balmer transitions of hydrogen, we measured a redshift of $z = 1.090$ with a conservative estimate of the uncertainty of 0.002.

On UT 2018 July 31, GRAL113100-441959 was also observed with the $0''.09/\text{px}$ Two Color Instrument (TCI) Lucky imager (Evans et al. 2016) mounted on the 1.54m Danish telescope at La Silla, Chile. A sequence of eight spools of two minute exposures was obtained with the RED color channel. We combined all the quality bins of each spool to generate the 16 min total exposure image shown in Fig. 2.

2.2. The lensing nature of GRAL113100-441959

Fig. 1 presents the calibrated spectra of GRAL113100-441959 from the $\text{PA} = 60^\circ$ observation; a wide aperture was extracted containing both observed components. The $\text{PA} = 135^\circ$ observation is identical to the NE component. The source is clearly identified as a quasar at $z_s = 1.090$ based on strong detections of broad emission from $\text{C III } \lambda 1909$, $\text{Mg II } \lambda 2800$, $\text{H}\gamma$ and $\text{H}\beta$. In addition, narrow, forbidden transitions of oxygen and highly ionized neon are also evident. These features, seen in both components of the $\text{PA} = 60^\circ$ spectra, clearly confirm the lensing nature of GRAL113100-441959. There is no clear evidence of the

Table 1. *Gaia*'s lensing observables for GRAL113100-441959.

| Image | $\Delta\alpha \cos(\delta)$ ["] | $\Delta\delta$ ["] | flux ratios in <i>G</i> -band |
|-------|------------------------------------|-----------------------|----------------------------------|
| A | 0.00000 ± 0.0021 | 0.0000 ± 0.0020 | 1.00 ± 0.15 |
| B | 0.3454 ± 0.0020 | -0.3246 ± 0.0015 | 0.95 ± 0.15 |
| C | -1.2825 ± 0.0021 | -0.4246 ± 0.0015 | 0.47 ± 0.15 |
| D | -0.3434 ± 0.0023 | -1.5110 ± 0.0015 | 0.40 ± 0.15 |

lensing galaxy in the Keck data, neither in the sky-subtracted two-dimensional spectra, nor in the extracted, calibrated one-dimensional spectra.

3. Lens modeling

In this section, we describe the method applied to obtain a simple lens model that can adequately reproduce the lensing observables provided by *Gaia* DR2. Our motivation is to use this model to predict time delays between pairs of lensed images for a range of plausible lens redshift values.

3.1. Overview

The constraints on the lens mass distribution include the relative angular positions θ_i of the lensed images with respect to the brighter image, hereafter labelled image A, and the flux ratios $f_i \equiv F_i/F_A$ in the *G*-band between the images *i* and A. Because the number of constraints is quite limited, we reconstructed the lens mass distribution using only a simple physically motivated and fully parametrized model, which is described in Sect. 3.2.

Both the astrometric and photometric *Gaia* measurements are affected by statistical errors. However, the flux uncertainties as given in *Gaia* DR2 do not reflect various well-known sources of uncertainty that have to be taken into account in the modeling scenario, the most important of which are (i) microlensing effects of one or several of the macrolensed images (see, e.g., Wambsganss & Paczynski 1991; Chae et al. 2001; Akhunov et al. 2017), (ii) small scale structures in the lens galaxy at the image positions (Mao & Schneider 1998; Metcalf & Madau 2001; Hsueh et al. 2017, and references therein), (iii) differential dust-reddening (see, e.g., Murphy & Liske 2004; Jean & Surdej 2007; Ménard et al. 2008), and (iv) source variability which propagates into image light curves with lags due to time delays (Treu & Marshall 2016). To represent these unquantified effects, we thus used conservative 15% Gaussian errors for the image flux ratios. Both the lensing observables and their related uncertainties are reported in Table 1.

We performed the modeling using pySPT (Wertz & Orthen 2018), a software package mainly dedicated to the study of the Source Position Transformation (SPT) but which comes with several simple modeling tools, and gravlens, a lensing-dedicated software package developed by C. R. Keeton (Keeton 2001b, 2010, 2011).

3.2. Lens mass models

We modeled the mass distribution of the lens galaxy using a singular power-law elliptical mass distribution (SPEMD), which is broadly consistent with typical lens galaxies and has been extensively used in the literature (see, e.g., Suyu et al. 2009; Sonnenfeld et al. 2013; Birrer et al. 2016; Wong et al. 2017; Shajib et al.

2018). The corresponding dimensionless surface mass density profile, also known as the convergence, is defined by

$$\kappa(\theta_1, \theta_2) = \frac{a}{2} \left(\frac{\theta_E}{\sqrt{\theta_1^2/q + q\theta_2^2}} \right)^{2-a}, \quad (1)$$

where θ_E is the Einstein radius, a the power-law slope¹, and q the minor-to-major axis ratio of the elliptical iso-density contours. The on-sky Cartesian angular coordinates (θ_1, θ_2) are clockwise rotationally transformed into the coordinates $(\underline{\theta}_1, \underline{\theta}_2)$, whose axes are aligned with the minor and major axes of the lens. Specifically, we write $\underline{\theta} = R(-\theta_q)\theta$ where R is the rotation matrix and θ_q the position angle of the minor axis. The SPEMD simplifies into a singular isothermal ellipsoid (SIE) when $a = 1$, and into a singular isothermal sphere (SIS) when both $a = 1$ and $q = 1$. Closed-form expressions for the SPEMD deflection angle α and deflection potential ψ can be found in Keeton (2001a).

We also included external shear (see, e.g., Meylan et al. 2006) to describe the weak influence of long-scale structure and possible local massive objects. This adds the two parameters γ (shear strength) and θ_γ (shear position angle) to the lens model. In addition to the model parameters, both the position of the source (β_1, β_2) and the lens galaxy centroid $(\theta_{\text{gal},1}, \theta_{\text{gal},2})$ are also unknown quantities. A first estimate may however be inferred from the centroid of the four lensed image positions, namely $(c_1, c_2) = (-0''.320, -0''.565)$ with respect to the image A, which has been used as a prior for both (β_1, β_2) and $(\theta_{\text{gal},1}, \theta_{\text{gal},2})$.

3.3. Modeling procedure

For a given lens model, the parameter space is in general populated with several local solutions which optimize the objective function in some feasible neighborhood. As a first step, we explored the parameter space using the differential evolution algorithm (Storn & Price 1997), which is designed to search for the global solution with no absolute guarantee to find it. As a benefit, this method requires no initial solution, but ranges of parameter values only. We defined half the largest angular separation θ_{max} between the images as a prior for θ_E , and considered the initial range $[\theta_{\text{max}}/4, 4\theta_{\text{max}}]$. For both the source position and lens galaxy centroid, we set the initial range $[c_j - \theta_{\text{max}}/2, c_j + \theta_{\text{max}}/2]$ for each coordinate ($j = 1, 2$). We also set the initial ranges $q \in [0.1, 1.0]$, $\gamma \in [0.0, 0.3]$, $a \in [0.5, 1.5]$, and $[0, 2\pi]$ for the two angular parameters θ_q and θ_γ .

For this first step, we ignored the observed flux ratios and only minimized the dispersion of the sources $\beta_i \equiv \beta(\theta_{\text{obs},i}, \mathbf{p}) = \theta_{\text{obs},i} - \alpha(\theta_{\text{obs},i})$, which are traced back from the observed image positions θ_{obs} for a given set of parameters \mathbf{p} . Because it does not require the lens equation to be solved, calculating β_i is very efficient. We obtained a first set of parameters \mathbf{p}_0 , which includes the SPEMD model parameters, the lens galaxy centroid, and the source position β_0 derived from the median value of β_i resulting from the best fit. To decrease the chance of getting stuck in a local solution, we also ran the minimization process on sub-regions of the parameter space, and compared the sub-results with the one obtained when running on the entire parameter space. We thus used the flux ratios as an additional constraint to separate plausible from poor solutions.

As a second step, we refined the solution using a downhill simplex algorithm (Nelder & Mead 1965) with \mathbf{p}_0 as the first

¹ The power-law slope a is linked to the 3-dimensional slope γ' of the power-law mass distribution through the relation $a = 3 - \gamma'$.

guess. Assuming that the errors follow a Gaussian distribution, the goodness of the fit was evaluated with a reduced χ^2 statistics, $\chi_{\text{red}}^2 = \chi^2/N_{\text{dof}}$, where N_{dof} represents the number of degrees of freedom, naively defined as the difference between the number of lensing observables and that of the model free parameters (Andrae et al. 2010). The χ^2 statistic results from the sum of the two contributions χ_{img}^2 and χ_{flux}^2 , characterized by

$$\chi^2 = \sum_{j=1}^{N_{\text{img}}-1} \frac{(\theta_{\text{obs},j} - \theta_j)^2}{\sigma_{\theta,j}^2} + \sum_{j=1}^{N_{\text{img}}-1} \frac{(f_{\text{obs},j} - f_j)^2}{\sigma_{f,j}^2}, \quad (2)$$

where θ_{obs} and θ are respectively the observed and model-predicted positions of the lensed images, f_{obs} and f are the observed and model-predicted flux ratios, and σ their associated uncertainties.

We initiated the modeling procedure by fixing the parameters $a = 0$ and $q = 1$, and successively increased the model complexity. We tested the statistical significance of including these parameters using an F -test (see, e.g., Bevington 1969). Following Cohn et al. (2001) and Protassov et al. (2002), we recall that adding a parameter to a given model is statistically significant, with a confidence level $0 < \nu < 1$ compared to the improvement expected for a random variable, if the difference between the χ^2 statistics, $|\Delta\chi^2| > h \chi^2/N_{\text{dof}}$, exceeds the reduced χ^2 obtained for the unmodified model by a factor $h = \text{ppf}(\nu, \Delta N_{\text{dof}}, N_{\text{dof}})/\Delta N_{\text{dof}}$, where ppf is the so-called percent point function of the F -distribution (David 1949; Pearson 1951). For instance, if adding one parameter to a model having $N_{\text{dof}} = 4$ improves the fit from $\chi^2 = 21.1$ to 3.5, one obtains $|\Delta\chi^2| = 17.6 \geq 6.79 = (21.1/4) \times \text{ppf}(0.68, 1, 4)$, and the F -test suggests that adopting the new model is statistically justified under the 1σ confidence level hypothesis. Similarly, one can compute the confidence level ν^* for which $|\Delta\chi^2| = h \chi^2/N_{\text{dof}}$, and compare it with the 1σ confidence level $\nu_{1\sigma} \simeq 0.68 = 68\%$. In our example, one has $\nu^* \simeq 86\% > \nu_{1\sigma}$, which leads to the same conclusion.

As a third step, we further explored the parameter space of the best fit model and deduced confidence intervals for each model parameter using a Bayesian inference method based on a Monte-Carlo Markov Chain (MCMC) sampling. We sampled the posterior probability distribution function (pdf) of the model parameters using *emcee* (Foreman-Mackey et al. 2013), a Python package which implements the affine-invariant ensemble sampler for MCMC proposed by Goodman & Weare (2010). We monitored the chains, also called walkers, using the fraction of accepted to proposed candidates (the so-called acceptance rate, Mackay 2003), and assessed the convergence with the integrated autocorrelation time (Christen & Fox 2010; Goodman & Weare 2010), which gives an estimate of the number of posterior pdf evaluations required to draw an independent sample. We then computed the 1σ confidence intervals from the 16- and 84-th percentiles.

3.4. Model properties

We first examined the SPEMD with $a = 1$ and $q = 1$ in an external shear field, hereafter denoted as the SISg model. This model is characterized by seven parameters ($\theta_E, \gamma, \theta_\gamma, \beta_1, \beta_2, \theta_{\text{gal},1}, \theta_{\text{gal},2}$) and $N_{\text{dof}} = 4$. With $\chi^2/N_{\text{dof}} = (89.3 + 1.3)/4$, the SISg model poorly fits the data, in particular the image positions. Although this result comes as no surprise considering the incredible simplicity of the SISg model, it provides a first estimate of the Einstein radius, $\theta_E = 0''.851$, and of the external shear, $(\gamma, \theta_\gamma) =$

$(0.048, -3''.7)$, see Table 2. Adding an ellipticity (q, θ_q) parameter to the SISg, thus transforming it into a SIEg, considerably improves the fit to $\chi^2/N_{\text{dof}} = (0.0 + 1.2)/2$, and is statistically significant with a confidence level $\nu^* = 75\%$ ($> 68\%$) for the F -test. Letting the parameter a vary during the optimization process, we relaxed the isothermal hypothesis. This slightly improves the fit, $\chi^2/N_{\text{dof}} = (0.0 + 1.1)/1$, but is not statistically significant according to the F -test ($\nu^* = 28\%$). Increasing the model complexity favors slightly higher ellipticity ($1 - q$) along with smaller external shear strength. This clearly reflects the well-known degeneracy existing between these two sources of angular structure (see, e.g., Keeton et al. 1997; Keeton 2010; Kneib & Natarajan 2011).

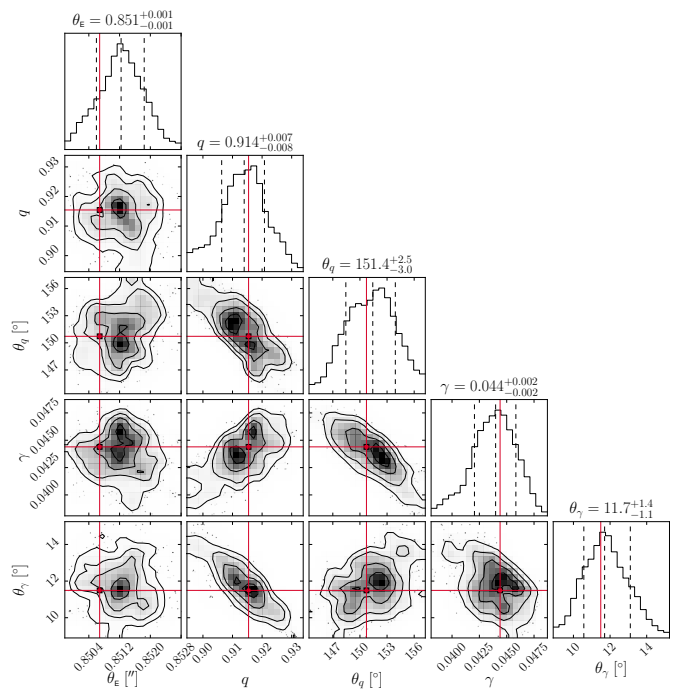


Fig. 3. Results of MCMC sampling for the SIEg model parameters. The diagonal panels illustrate the posterior pdfs while the off-axis ones illustrate the correlation between the parameters. The vertical red lines and red crosses correspond to the best solution obtained from the downhill simplex algorithm and used to initiate the 250 walkers. The vertical dashed lines locate the 16- and 84-th percentiles.

The errors σ_f adopted for the image flux ratios are to some extent arbitrary. We thus explored the impact on the fit when we modify these values. In this regard, we restrained ourselves to estimate these errors by rescaling σ_f to artificially obtain $\chi_{\text{red}}^2 = 1$, because this method has been shown to be incorrect (e.g., Andrae 2010). We found that the SIEg remains the one providing the most statistically significant results. As a next step, we sampled the pdfs for all SIEg parameters, using the best fit parameter values reported in Table 2 to initialize 250 walkers. The resulting pdfs and the correlation between model parameters are represented with two corner plots, in Figs. 3 and 4 respectively. The corresponding confidence intervals are also reported in Table 2. As expected, the shear-ellipticity degeneracy induces a significant correlation between the parameters (γ, θ_γ) and (q, θ_q). In Fig. 5, we represent the lensed image configuration, labelled from A to D, on top of a few predicted lensing quantities for the SIEg model reported in Table 2. The predicted mass within a circular aperture of radius θ_E is estimated to be in

Table 2. The best-fit model parameters obtained for the three complexity levels of the SPEMD plus external shear. The confidence intervals of the SIEg parameters, inferred from the MCMC sampling, are also reported at the bottom.

| Model | χ^2_{red} | θ_E | a | q | θ_q | γ | θ_γ | β_1 | β_2 | $\theta_{\text{gal},1}$ | $\theta_{\text{gal},2}$ |
|--------|-----------------------|--|--------------|---|--|---|---------------------------------------|-----------|-----------|-------------------------|-------------------------|
| SISg | 90.6/4 | 0′.851 | $\equiv 1.0$ | $\equiv 1.0$ | – | 0.048 | –3′.7 | –0′.445 | –0′.705 | –0′.427 | –0′.737 |
| SIEg | 1.2/2 | 0′.851 | $\equiv 1.0$ | 0.915 | 150′.7 | 0.044 | 11′.5 | –0′.447 | –0′.704 | –0′.424 | –0′.744 |
| SPEMDg | 1.1/1 | 0′.853 | 1.299 | 0.885 | 2′.0 | 0.023 | 0′.6 | –0′.440 | –0′.719 | –0′.422 | –0′.752 |
| C.I. | | 0′.851 ^{+0.002} _{–0.001} | $\equiv 1.0$ | 0.914 ^{+0.007} _{–0.008} | 151′.4 ^{+2.5} _{–3.0} | 0.044 ^{+0.002} _{–0.002} | 11′.7 ^{+1.4} _{–1.1} | –0′.447 | –0′.704 | –0′.426 | –0′.743 |

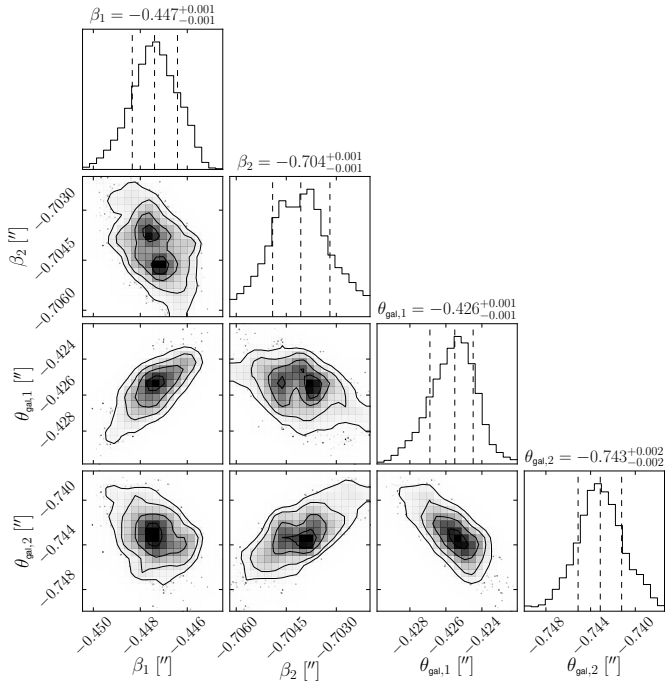


Fig. 4. Results of the MCMC sampling for the source position and lens galaxy centroid. The diagonal panels illustrate the posterior pdfs while the off-axis ones illustrate the correlation between the parameters. The vertical dashed lines locate the 16– and 84–th percentiles.

the range $M(\leq \theta_E) = 2.498 \pm 0.003 \times 10^{11} M_\odot$ for $z_1 = 0.5$ and $M(\leq \theta_E) = 1.119 \pm 0.002 \times 10^{12} M_\odot$ for $z_1 = 0.9$.

4. Model-predicted time delays

From the set of highly probable lens models obtained from the MCMC sampling, we computed the predicted time delays Δt_{ij} between pairs of images (θ_i, θ_j) , which are defined by

$$\Delta t_{ij} = \frac{D_{\Delta t}}{c} \left[\frac{1}{2} (|\alpha(\theta_i)|^2 - |\alpha(\theta_j)|^2) - (\psi(\theta_i) - \psi(\theta_j)) \right], \quad (3)$$

where $D_{\Delta t} = (1 + z_l)D_l D_s / D_{ls} \propto H_0^{-1}$ is the time-delay distance, with D the angular diameter distance between the observer and lens (D_l), observer and source (D_s), and lens and source (D_{ls}). The angular diameter distance depends only on the redshift and the cosmology. From the Keck/LRIS spectra, the redshift of the source was found to be $z_s = 1.09$. However, as there is no clear evidence of the lensing galaxy in the Keck/LRIS spectral data, we were prevented from determining its redshift z_1 (see Sect. 2.2). We thus computed the time-delay distance, hence the time delays, for a set of lens redshifts in the plausible

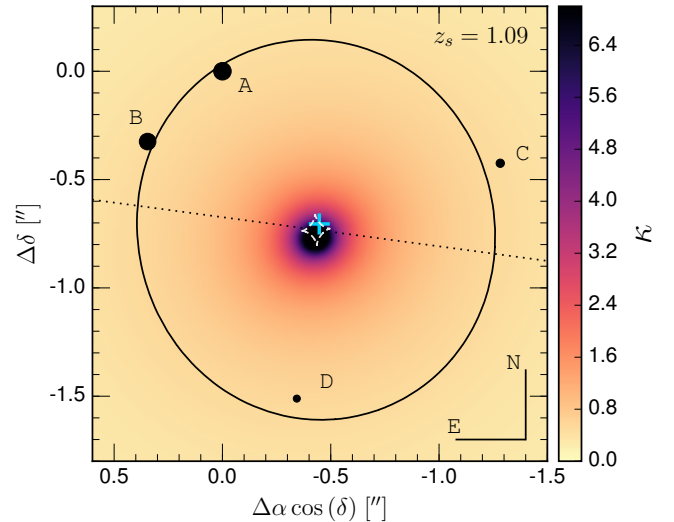


Fig. 5. The GRAL113100-441959 image configuration. The black dots locate the image positions, and their size mimics the associated flux, as reported in the *Gaia* DR2. The solid line represents the tangential critical line, the diamond-shaped dashed line represents the corresponding caustic line, and the dotted line defines the direction of the external shear. Finally, the color map shows how the surface mass density κ is distributed.

range $z_1 \in [0.5, 0.9]$. We adopted the Λ CDM model along with the final Planck 2018 results (Planck Collaboration et al. 2018). The normalized $\Delta t_{ij} h^{-1}$ against the lens redshift z_1 is shown in Fig. 6, where the factor h is used to calibrate the Hubble constant $H_0 = 100 h \text{ km s}^{-1} \text{ Mpc}^{-1}$.

The error budget associated with Δt_{ij} was estimated by considering three sources of uncertainties. First, we propagated the statistical error inferred from the MCMC sampling. This was simply done by constructing histograms for $\Delta t_{ij} h^{-1}$ from the independent samples of SIEg model parameters reported in Figs. 3 and 4. An example of these histograms is illustrated in Fig. 7 for the case of $z_1 = 0.7$. Secondly, we considered the impact of hypothetical massive objects lying on the line-of-sight by scaling the theoretical time-delay distance with an external convergence term κ_{ext} such that $D_{\Delta t} = D_{\Delta t}^{\text{theory}} / (1 - \kappa_{\text{ext}})$ (see, e.g., Keeton 2003). We applied a different scaling for each set of model parameters used to construct the histograms (see Fig. 7). The κ_{ext} values were randomly drawn from a zero mean normal distribution and characterized by a conservative standard deviation $\sigma_\kappa = 0.03$ (see, e.g., Wong et al. 2017). When combined, the typical errors are $\sim 7.7\%$ for Δt_{CB} , $\sim 7.8\%$ for Δt_{CA} , and $\sim 7.6\%$ for Δt_{CD} , compared to the median values. Thirdly, we considered the impact of the Source Position Transformation (SPT), a degeneracy existing between different lens density profiles that reproduce equally well the lensing observables, except for the

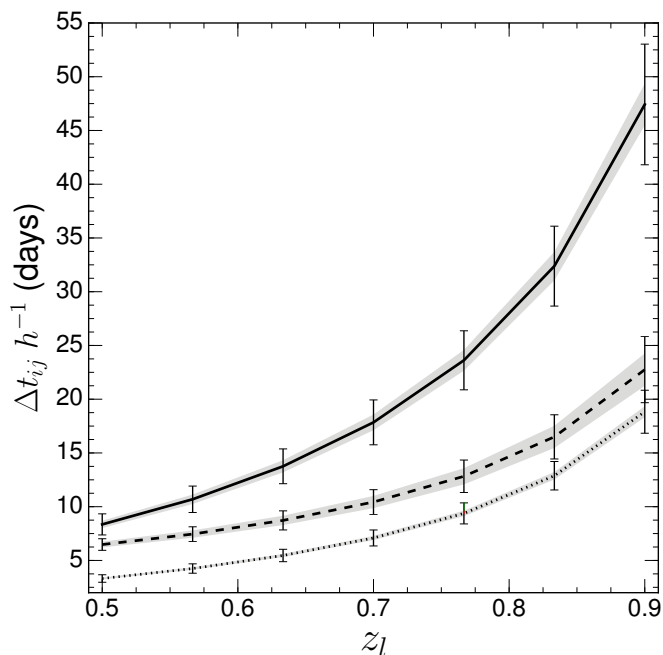


Fig. 6. Model-predicted time delays scaled with h . The error bars combine the three sources of uncertainties described in the text. The grayshaded regions depict the contribution of the SPT to the error budget. The solid line corresponds to images C–D, the dashed line to C–A, and the dotted line to C–B. For the sake of clarity, we shifted upwards the time delays between images C–A (dashed line) by a 3 day offset.

product $\Delta t H_0$ (Schneider & Sluse 2013, 2014). A short summary is given in Appendix A. We SPT-transformed the SIEg model using the modified deflection law $\hat{\alpha} = \alpha_{\text{SIEg}} + \beta - \hat{\beta}(\beta)$ along with a radial stretching of the source plane defined by $\hat{\beta}(\beta) = [1 + f_2|\beta|^2/(2\theta_E)]\beta$, where f_2 is named the deformation factor. As defined, $\hat{\alpha}$ is not a curl-free field, and hence does not correspond to the deflection produced by a gravitational lens.

To overcome this hurdle, one can (i) derive the closest curl-free approximation to $\hat{\alpha}$ in a circular region of the lens plane as proposed in Unruh et al. (2017) and applied in Wertz et al. (2018) and Wertz & Orthen (2018), or (ii) extract the curl-free part from $\hat{\alpha}$ using an Helmholtz-Hodge decomposition (Helmholtz 1858). In both cases, the new deflection law is denoted $\tilde{\alpha}$. We adopted the Helmholtz-Hodge decomposition strategy, given that the region of interest can be straightforwardly reduced to the annulus that includes all four images, leading to higher predicted time delay deviations than found with the first approach (Wertz & Schneider, in prep.). The higher the value of f_2 , the larger deformation of the source plane along with the deflection law $\tilde{\alpha}$, hence the larger deviations of the predicted image positions in comparison with the observations. For each set of the SIEg model parameters, we thus computed the highest acceptable f_2 value, which guarantees the corresponding SPT-transformed model to produce an image configuration identical to the one observed by *Gaia*, within the astrometric and photometric error bars. For the best fit SIEg model reported in Table 2, we found $|f_2| = 1.67$, which is representative of the values we obtained for the entire sample. We then repeated the process for the different lens redshifts. Finally, the impact of the SPT results in additional time delay deviations of 2.7% for Δt_{CB} , 7.7% for Δt_{CA} , and 4.1% for Δt_{CD} . This contribution corresponds to a significant fraction of the time delay error budget, in particular for Δt_{CA} where the SPT

input reaches the same level as the statistical errors. We finally combined the three different sources of uncertainties to obtain the error bars of Fig. 6.

As a result, the model-predicted time delays vary from (for $z_l = 0.5$) $\Delta t_{\text{CA}}h^{-1} = 3.48 \pm 0.54$ days, $\Delta t_{\text{CB}}h^{-1} = 3.32 \pm 0.35$ days, and $\Delta t_{\text{CD}}h^{-1} = 8.35 \pm 0.98$ days, to ($z_l = 0.9$) $\Delta t_{\text{CA}}h^{-1} = 19.75 \pm 3.07$ days, $\Delta t_{\text{CB}}h^{-1} = 18.83 \pm 2.00$ days, and $\Delta t_{\text{CD}}h^{-1} = 47.42 \pm 5.61$ days.

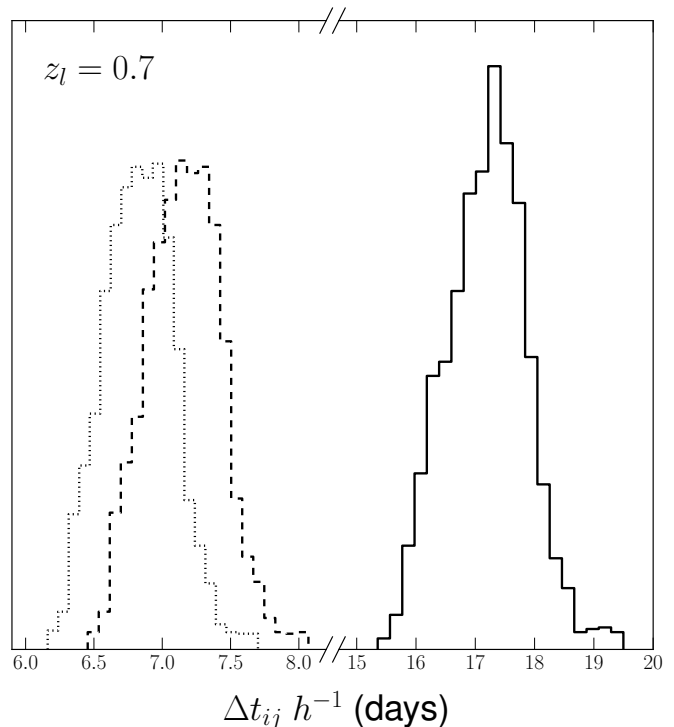


Fig. 7. Example of histograms for $\Delta t_{ij} h^{-1}$ constructed for $z_l = 0.7$ from the MCMC results. The solid line corresponds to images C–D, the dashed line to C–A, and the dotted line to C–B.

5. Conclusions

This paper presents the spectroscopic confirmation of the gravitationally lensed quasar GRAL113100-441959, previously identified in paper I as a highly probable GL candidate hidden in the *Gaia* DR2. We obtained Keck/LRIS spectroscopy on the night of UT 2018 May 13, revealing similar spectra for the combinations of sources A+B and C+D, for the slit at a position angle of 60° , and A+B and C+D for the slit at a position angle of 135° . We confirmed the lensing nature of GRAL113100-441959 by clearly identifying several similar emission spectral lines between the images (A+B) and (C+D), and measured redshifts for these combination of lensed images of the quasar as $z_s = 1.09$.

We modeled the main lens galaxy with a SPEMD plus external shear, and explored different levels of model complexity. This study indicates that the SIEg model (which is equivalent to SPEMD with $a = 1$) is the best choice in terms of goodness of the fit and statistical significance, given the available observational data. We inferred the confidence intervals for each model parameter using a Bayesian inference method based on a MCMC sampling. We found $\theta_E = -0'851 \pm 0.001$ for the Einstein radius. The lens galaxy ellipticity is inferred to have an axis ratio of $q = 0.914_{-0.008}^{+0.007}$ pointing to $151^\circ4_{-3.0}^{+2.5}$ east of north.

The shear strength is found to be moderate, $\gamma = 0.044 \pm 0.002$, pointing $11^{\circ}7_{-1.4}^{+1.4}$ east of north. This suggests that the ellipticity captures most of the source of angular structure. Finally, we predict the lensing galaxy to lie at $(\Delta\alpha \cos(\delta), \Delta\delta) = (-0^{\circ}.426 \pm 0.001, -0^{\circ}.743 \pm 0.002)$ from image A.

We also used the MCMC results to predict the three independent time delays between pairs of images. As the redshift z_1 of the lensing galaxy is still unknown, we provide the model-predicted time delays for a range of physically plausible z_1 , between 0.5 and 0.9. Finally, we assessed the error affecting our estimation, and in particular quantified the impact of the SPT. We found that the contribution of the SPT to the error budget cannot be ignored for precise applications of strongly lensed systems, as it can be as important as the other uncertainty sources. In the case of GRAL113100-441959, SPT is extremely relevant for the time-delay between the C–A images.

GRAL113100-441959 is the first spectroscopically confirmed GL from the Gaia GrAL sample of highly probable candidates recently presented in papers I and III of this series. At the time we release this work, nine additional candidates from Paper III were already observed with the Keck/LRIS in other campaigns, with six of them being very likely lenses; the analysis of these other GL candidates will be presented in a companion paper.

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Appendix A: The Source Position Transformation

In this appendix, we summarize the basic principles of the SPT. For a detailed discussion, we refer the reader to [Schneider & Sluse \(2014\)](#); [Unruh et al. \(2017\)](#); [Wertz et al. \(2018\)](#); [Wertz & Orthen \(2018\)](#).

The relative lensed image positions $\theta_i(\theta_1)$ of a background point-like source located at the unobservable position β constitute the lensing observables that we measure with the highest accuracy and precision. When n images are observed, the mapping $\theta_i(\theta_1)$ only provides the constraints

$$\theta_i - \alpha(\theta_i) = \theta_j - \alpha(\theta_j), \quad \forall 1 \leq i < j \leq n, \quad (\text{A.1})$$

where $\alpha(\theta)$ corresponds to the deflection law caused by a foreground surface mass density $\kappa(\theta)$, the so-called lens. The SPT addresses the following question: can we define an alternative deflection law, denoted as $\hat{\alpha}(\theta)$, that preserves the mapping $\theta_i(\theta_1)$ for a unique source? If such a deflection law exists, the alternative source position $\hat{\beta}$ differs in general from β . Furthermore, it defines the new lens mapping $\hat{\beta} = \theta - \hat{\alpha}(\theta)$, which leads to

$$\theta = \beta + \alpha(\theta) = \hat{\beta} + \hat{\alpha}(\theta). \quad (\text{A.2})$$

An SPT consists in a global transformation of the source plane formally defined by a one-to-one mapping $\hat{\beta}(\beta)$, unrelated to any physical contribution such as the external convergence. To preserve the mapping $\theta_i(\theta_1)$, the alternative deflection law thus reads

$$\hat{\alpha}(\theta) = \alpha(\theta) + \beta - \hat{\beta}(\beta) = \alpha(\theta) + \beta - \hat{\beta}(\theta - \alpha(\theta)), \quad (\text{A.3})$$

where in the first step we used Eq. (A.2) and in the last step we inserted the original lens equation. As defined, the deflection laws $\alpha(\theta)$ and $\hat{\alpha}(\theta)$ yield exactly the same image positions of the source β and $\hat{\beta}$, respectively.

Because $\hat{\alpha}$ is in general not a curl-free field, it cannot be expressed as the gradient of a deflection potential caused by a mass distribution $\hat{\kappa}$. Provided its curl component is sufficiently small, [Unruh et al. \(2017\)](#) have established that one can find a curl-free deflection law $\tilde{\alpha}$ that is similar to $\hat{\alpha}$ in a circular region of the lens plane denoted as \mathcal{U} where multiple images occur. The corresponding similarity criterion reads

$$|\Delta\alpha(\theta)| := |\tilde{\alpha}(\theta) - \hat{\alpha}(\theta)| < \varepsilon_{\text{acc}}, \quad (\text{A.4})$$

for $\theta \in \mathcal{U}$. In [Wertz et al. \(2018\)](#), the authors highlight the limitation of this approach and provide two alternative solutions.