Accuracy of Prediction of Gene Content in Large Animal Populations and its Use for Candidate Gene Detection and Genetic Evaluation

N. Gengler,*† S. Abras,*‡ C. Verkenne,* S. Vanderick,* M. Szydlowski,*§ and R. Renaville‡

*Animal Science Unit, Gembloux Agricultural University, B-5030 Gembloux, Belgium
†National Fund for Scientific Research, B-1000 Brussels, Belgium
‡Animal and Microbial Biology Unit, Gembloux Agricultural University, B-5030 Gembloux, Belgium
§Department of Genetics and Animal Breeding, August Cieszkowski Agricultural University of Poznan, Poland

ABSTRACT

To estimate and to use the effects of single genes on quantitative traits, genotypes need to be known. However, in large animal populations, the majority of animals are not genotyped. These missing genotypes have to be estimated. However, currently used methods are impractical for large pedigrees. An alternative method to estimate missing gene content, defined as the number of copies of a particular allele, was recently developed. In this study, the proposed method was tested by assessing its accuracy in estimation and use of gene content in large animal populations. This was done for the bovine transmembrane growth hormone receptor and its effects on first-lactation milk, fat, and protein test-day yields and somatic cell score in Holstein cows. Estimated gene substitution effects of replacing a copy of the phenylalanine-coding allele with a copy of the tyrosine-coding allele were 295 g/d for milk, −8.14 g/d for fat, −1.83 g/d for protein, and −0.022/d for somatic cell score. However, only the gene substitution effect for milk was found to be significant. The accuracy of the estimated effects was evaluated by simulations and permutations. To validate the use of predicted gene content in a mixed inheritance model, a cross-validation study was done. The model with an additional regression of milk, fat, and protein yields and SCS on predicted gene content showed a better capacity to predict breeding values for milk, fat, and protein. Given these results, the estimation and use of allelic effects using this method proved functional and accurate.

Key words: regression on gene content, single gene effect, test-day model

INTRODUCTION

Animal breeding may benefit from the knowledge of single gene effects on quantitative traits under selection. Today there are large data sets for phenotypic records and sparse data sets for genotypes at candidate loci. To allow simple and better use of the available data, the missing genotypes can be replaced with predicted values. Israel and Weller (1998, 2002) showed that useful estimates of candidate gene effects can be calculated under an animal model with regression of milk, fat, and protein yields and SCS on genotype probabilities or predicted gene content, defined as the number of copies of a particular allele in the genotype of an animal (Lynch and Walsh, 1997). In large pedigrees with sparse molecular data, the currently available methods for calculation of genotype probabilities may be impractical. In large animal populations, the convergence of Markov chain Monte Carlo (MCMC) methods cannot be easily monitored, whereas the estimates from iterative peeling and sparse data can strongly depend on the assumed gene frequency, which remains unknown (Gengler et al., 2007). Recently, a more practical method was proposed to approximate gene content in large pedigrees (Gengler et al., 2007). The new method compared very positively to the iterative peeling approach (van Arendonk et al., 1989) applied to a population under selection and with known gene frequency.

The objective of the present study was to evaluate the accuracy of this new method in estimating and, subsequently, using predicted gene content in the context of the estimation of the effects of a candidate gene on first-lactation milk, fat, and protein test-day (TD) yields and SCS in Holstein cows and the estimation of combined breeding values associating single gene effect and polygenic effects.

MATERIALS AND METHODS

Animals and Data

The TD data were provided by the Canadian Dairy Network (Guelph, Canada) for the Holstein breed. We chose to use these data because our molecular data came from Canadian Holstein sires. In the present study, only first-lactation data were analyzed. These
data included 12,858,741 TD records from DIM 4 to DIM 305 for 1,656,599 cows in production born from 1982 through 1999. The mean production per cow per TD was 24.56 kg for milk (SD = 6.4 kg), 903 g for fat (SD = 237 g), 792 g for protein (SD = 192 g), and 2.15 (SD = 1.76) for SCS, which is equal to \( \log_2[(SCC)/100,000] + 3 \). A pedigree file containing 2,755,041 animals (cows with production records and all registered ancestors) born between 1909 and 1999 was also provided by the Canadian Dairy Network.

**Candidate Gene Studied**

The selected gene was the bovine transmembrane growth hormone-receptor (GHR). Indeed, Falaki et al. (1996) found effects of polymorphism of this gene on milk protein percentage. As reported by Arranz et al. (1998) and Blott et al. (2003), other interesting results showed the possible segregation of a QTL on chromosome 20 (therefore close to the GHR gene) that seemed to influence milk yield and composition in Holstein dairy cattle. Semen samples of 961 Canadian Holstein AI bulls, born mostly during the late 1980s and early 1990s, were provided by Semex Alliance (Guelph, ON, Canada) for a previous study (Parmentier, 2004). In that study, bulls were genotyped by a PCR allele-specific method to determine if they had a T→A substitution at the transmembrane domain of the GHR gene, leading to the replacement of a phenylalanine by a tyrosine (Parmentier, 2004). Around 75% of the cows with production records had at least one genotyped sire or grandsire.

**Prediction of Gene Content**

Gene content was approximated using the method described by Gengler et al. (2007). This method computes the conditional expectation of gene contents for nongenotyped animals, given molecular and pedigree data. The Appendix shows an alternative derivation to that given by Gengler et al. (2007), showing the underlying hypotheses.

**Cross Validation of Gene Content Prediction**

The method to predict gene content was used in a preliminary cross-validation study. The aim of this study was to assess the differences between predicted and known genotypes, for animals with known genotypes. For this purpose, a file containing the 961 genotyped sires was used. The sires were removed one by one from the file and their gene content was estimated by the method described above, using the remaining 960 sires and the relationship between the removed sire and the other sires. Results obtained for each sire were stored for later comparison to the true gene contents.

For each real gene content (0, 1, and 2), means and standard deviations (SD) of estimated gene contents, and mean square errors (MSE) between real and estimated gene contents were calculated. Mean square error was computed as

\[
\text{MSE} = \frac{1}{n_q} \sum_{i=1}^{n_q} (q_{ir} - q_{ie})^2
\]

where \( q_{ir} \) is the real gene content (0, 1, or 2) of the \( i \)th animal, \( q_{ie} \) is the estimated gene content of the \( i \)th animal, and \( n_q \) is the number of animals with the same real gene content (0, 1, or 2).

**Analysis Model**

A generic TD model was used; results obtained would have been similar with slightly different models. The analysis model provided flexibility for the fixed portion and a minimum number of parameters for the random portion through the use of polynomials. Random regression effects were modeled using modified Legendre polynomials, to reduce correlations among regression coefficients. The use of third-order polynomials (constant, linear, and quadratic) was considered sufficient for a single yield trait to describe the random variation around the fixed lactation curve (Gengler et al., 1999). The 3 modified Legendre polynomials used were:

\[
I_0 = 1 \\
I_1 = \sqrt{3x} \\
I_2 = \sqrt{5/4(3x^2 - 1)}
\]

where \( x = -1 + 2 [(\text{DIM} - 1) / (305 - 1)] \) and \( \text{DIM} \) = days in milk.

The model used for the estimation of the effects in the first-lactation TD records was the following mixed inheritance model:

\[
y = \text{Htd} + \text{sarc} + \hat{q}_\alpha + W(Zp + Z * a) + e,
\]

where \( y \) is a vector of production data (TD yields or SCS; 12,858,741 records); \( \text{Htd} \) is a vector of herd and TD fixed effects (1,320,824 levels); \( \text{sarc} \) is a vector of season, group of age, region, and class of lactation fixed effects (560 levels); \( \alpha \) is the allelic substitution effect; \( p \) is a vector of permanent environmental random effects.
Validation Through Simulation and Permutations

Obtaining exact standard errors for our estimates of single gene effects would have been impossible. Indirect methods exist, such as those based on mixed model conjugate normal equations (Croquet et al., 2006). However, these methods do not take into account the uncertainty of the gene content used in the mixed model. Therefore, an alternative indirect method based on permutations was used:

Step 1: Genotypes were simulated as described hereafter: a biallelic gene was simulated on all the animals of the pedigree without known parents. If only one parent was known, only one allele of the gene was simulated. Each allele was simulated by sampling once from a uniform distribution. If a value equal or smaller than estimated PA was obtained, the animal received tyrosine-coding allele; phenylalanine-coding allele was received otherwise. Once alleles were attributed to all the animals with unknown parents, they were dropped down the pedigree assuming transmission probability of 1/2.

Step 2: Production records of each cow were modified using the simulated genotypes and the allelic substitution effects previously estimated to give .

Step 3: Only simulated genotypes of the 961 GHR genotyped bulls were supposed known and for the other animals, gene content was estimated by the method described by Gengler et al. (2007).

Step 4: The allelic substitution effect was estimated using the mixed inheritance model described above with the modified production records (step 2) and estimated gene content (step 3).

Steps 1 to 4 were repeated 15 times, which represented a compromise between available time and resources and the natural complexity of a test-day model. Mean, standard deviation, bias, and standard error (Efron and Tibshirani, 1986) were computed from 15 estimates for each production trait using the following definitions. To allow an easy comparison between the different traits, bias and standard errors were computed as relative values of simulated parameters for allele frequency and substitution effects:

\[
\text{relative bias} (%) = \frac{\sum_{i=1}^{n} (\hat{\theta}_i - \theta)}{n} \cdot 100 \quad \text{and} \quad \text{relative standard error} (%) = \left[ \frac{\sum_{i=1}^{n} (\hat{\theta}_i - \theta)^2}{n - 1} \right]^{1/2} \cdot \frac{100}{|\theta|},
\]
where \( n \) is number of repetitions, here 15; \( \hat{\theta} = \hat{\theta}_i \) parameter estimate based on original data; \( \hat{\theta}_i \) = \( i \)th estimate of a parameter based on modified data. To test that allelic effect, \( \alpha \), was significantly different from zero, approximate \( t \)-tests were performed for the substitution effects based on the inverse of the relative standard error associated with 14 degrees of freedom.

**Cross Validation of Mixed Inheritance Model Using Predicted Gene Content**

To validate the use of predicted gene content in a mixed inheritance model, data splitting (cross-validation) was used because it allows evaluation of the predictive ability of a model. Assessing the predictive ability of a model involves leaving out a portion of the data, fitting the model to the remainder of the data, and then testing the model fit on the omitted portion. The strategy proposed by Ramirez-Valverde et al. (2001) was used. According to earlier work by Picard and Cook (1984), optimal cross-validation should be done by splitting data randomly, to imitate a sample of future observations. This is especially true in the setting of genetic evaluations, where we try to predict unknown breeding values from limited knowledge of phenotypes and, in our case, genotypes. Our data splitting technique involved duplicating the data set and randomly discarding TD records for one-half of the cows in one subset with the TD records of the other half of the cows being discarded for the other subset. This strategy was a slight modification of the one proposed by Ramirez-Valverde et al. (2001), who discarded randomly half of the records, rather than the records belonging to half of the cows. Using the original strategy, the lactation curve of a given cow could still be reasonably well predicted from her remaining records. We think that by eliminating all of her records, we are really able to test the predictive ability of the model. The predictive ability of the mixed inheritance model was compared with the one of the model without the regression on predicted gene content. For each model, breeding values were calculated from both subsets. For the mixed inheritance model including the regression on predicted gene content, combined breeding values were defined as the sum of the polygenic effect and the product of the single gene effect and predicted gene content. Correlations among breeding values obtained from the 2 subsets were calculated. Computations were done for all 4 traits. Ten different random samples were created according to the above criteria, and reported correlations were the average of the 10 replicates. For each model, the estimated correlation coefficients provided an estimate of the model performance. Higher correlation estimates between complementary subsets indicate a greater stability of the model to predict breeding values. Correlation coefficients were calculated for all animals, for all cows with records, and for the 961 genotyped sires.

**RESULTS AND DISCUSSION**

**Cross Validation of Gene Content Prediction**

The accuracy of the estimation of the gene content depends strongly on the structure of the pedigree. The purpose of this section was to estimate if the structure of the Canadian Holstein pedigrees could allow us to estimate the gene content precisely. Coefficient of correlation of real with estimated gene contents was very high (0.93). This result is greater than the value of 0.47 found by Gengler et al. (2007) in their simulation study using a similar allele frequency (0.20). This suggests that the knowledge of the Canadian Holstein pedigree is very good and that there are good relationships among the 961 sires. Table 1 shows, for the 3 genotypes, mean estimated gene contents, standard deviations, and MSE of observed vs. estimated genotypes. Observed bias in the estimation was greatest for the rare genotype (real gene content = 2), which could be expected from the fact that only 62 sires (out of 961) were homozygous.

This cross-validation study was done on sires only. However, we can suppose that the estimations would be at least as good for their daughters, because there should be closer relationships of daughters with their genotyped sires (0.5) and maternal grandsires (0.25) than among genotyped sires. Indeed, Van Doormaal et al. (2005) estimated that the average relationship value among Canadian Holsteins was 0.114, which confirmed the value of 0.117 reported by Auvray et al. (2001), also for Canadian sires.

**Estimation of Allelic Substitution Effect and Variance**

Estimated effects of a substitution of a copy of the phenylalanine-coding allele by a copy of the tyrosine-coding allele on production traits were 295 g/d for milk, –8.14 g/d for fat, –1.83 g/d for protein, and –0.022 for SCS (Table 2). The frequency of the tyrosine-coding...
allele estimated by the new method was found to be 23.3% instead of the 23.8% estimated from the genotypes of the 961 sires. The difference is linked to the fact that the method used to estimate allele frequency weights the importance of every sire relative to its relationship to the population. Therefore, the obtained value reflects the allele frequency of the founders. This is an interesting feature of the method because knowledge of this frequency is important in many situations.

Compared with genetic and phenotypic standard deviations, the values in Table 2 show that, expressed as percentage of the average TD genetic ($\sigma_G$) and phenotypic standard deviation ($\sigma_P$), the relative substitution effect decreased from milk, fat, and SCS relative to that for protein.

Estimated allelic substitution variances are also given in Table 2. Based on absolute values and especially values relative to total genetic and phenotypic variances, the allelic effects considered were nearly negligible compared with the overall average TD genetic ($\sigma^2_G$) and phenotypic variances ($\sigma^2_P$).

The estimates of gene frequency and allelic effects are in general agreement with the results reported by Blott et al. (2003) for 2 populations of Holstein-Friesian cattle and 1 of Jersey. The rare tyrosine-coding allele was correlated with greater milk yield. As in Blott et al. (2003), the negative effect of tyrosine-coding allele on fat yield and protein yield was not so pronounced. In the present study, the effect on milk yield was greater than that reported by Blott et al. (2003) for the same polymorphism, but explained a similar portion of trait variability. Our estimate of allelic substitution effect was also greater than the one calculated for other candidate genes under a model with an additive effect of a single SNP (Szyda and Komisarek, 2007).

The larger substitution effect could be explained by the lower range of regressor variable (predicted gene content) because of the fact that no cows were genotyped. In this case, the average predicted content of tyrosine-coding alleles for cows carrying 2 tyrosine-coding alleles is lower than 2 and is greater than 0 for cows carrying 2 phenylalanine-coding alleles. This should be taken into account in the interpretation of the results.

We anticipate that more cows will be genotyped in the future and the tendency to potentially overestimate the single gene effect decreased. Still, single gene effects estimated in this study can be considered to be small to very small if compared with results of the meta-analysis done by Hayes and Goddard (2001). Indeed, in our study, all allelic substitution effects were equal to or below 0.119 and 0.065 of $\sigma_G$ and $\sigma_P$, respectively. Hayes and Goddard (2001) reported that very few single gene effects as small as these were given in the literature.

Validation of Allele Substitution Results

Results of the 15 repetitions, means, SD, relative bias, and relative standard errors for milk, fat, protein and SCS and simulated values for frequency of the tyrosine-coding allele ($F_A$) are in Table 3. Compared with $P_A$, allele frequencies $F_A$ provided by the 15 repetitions of the simulations had similar mean values. It must be remembered here that only the alleles from unknown parents were simulated using $P_A$; the other alleles were simulated with a one-half probability of receiving each paternal allele. The very low relative bias of 0.2% shows that the estimation of $P_A$ based on the method to approximate gene content is consistent with the value used in the simulation, which is the value estimated from the base population. Moreover, the relative standard error was rather small, indicating that the estimation was not only unbiased but had a low sampling error, too. The new method to estimate allele frequencies proved to be rather reliable. The method proved to be resistant to selection, a feature that is directly built into the system. These results confirm the conclusion found by Gengler et al. (2007), which showed that this method computes values that are similar to those obtained by MCMC methods and iterative peeling, methods that are theoretically considered to be the most appropriate for genotype probability calculations.

Compared with the estimated values of gene substitution effects, the means of the 15 repetitions were very similar for milk and fat yields with relative biases of...
Table 3. Results of the 15 repetitions of the validation results, simulated effects, means, standard deviations, relative biases, and relative standard errors for $F_A$ (estimated allele frequency), milk, fat, and protein yields and SCS

<table>
<thead>
<tr>
<th>Value used in simulation</th>
<th>$F_A$ (%)</th>
<th>Milk (g/d)</th>
<th>Fat (g/d)</th>
<th>Protein (g/d)</th>
<th>SCS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Repeated</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>18.2</td>
<td>261</td>
<td>-13.33</td>
<td>-3.45</td>
<td>-0.032</td>
</tr>
<tr>
<td>2</td>
<td>20.3</td>
<td>282</td>
<td>-18.85</td>
<td>-3.82</td>
<td>-0.032</td>
</tr>
<tr>
<td>3</td>
<td>26.9</td>
<td>602</td>
<td>1.37</td>
<td>3.79</td>
<td>0.035</td>
</tr>
<tr>
<td>4</td>
<td>17.3</td>
<td>322</td>
<td>-8.05</td>
<td>-3.44</td>
<td>-0.046</td>
</tr>
<tr>
<td>5</td>
<td>28.4</td>
<td>279</td>
<td>-5.37</td>
<td>-1.11</td>
<td>-0.016</td>
</tr>
<tr>
<td>6</td>
<td>25.8</td>
<td>271</td>
<td>-2.17</td>
<td>-4.19</td>
<td>-0.039</td>
</tr>
<tr>
<td>7</td>
<td>26.0</td>
<td>282</td>
<td>-8.69</td>
<td>-5.82</td>
<td>-0.047</td>
</tr>
<tr>
<td>8</td>
<td>29.9</td>
<td>128</td>
<td>-7.91</td>
<td>-3.14</td>
<td>-0.032</td>
</tr>
<tr>
<td>9</td>
<td>14.7</td>
<td>485</td>
<td>-4.21</td>
<td>-5.96</td>
<td>-0.052</td>
</tr>
<tr>
<td>10</td>
<td>21.0</td>
<td>189</td>
<td>-9.34</td>
<td>-3.82</td>
<td>-0.032</td>
</tr>
<tr>
<td>11</td>
<td>25.8</td>
<td>352</td>
<td>-12.91</td>
<td>-3.04</td>
<td>-0.020</td>
</tr>
<tr>
<td>12</td>
<td>27.1</td>
<td>280</td>
<td>-4.24</td>
<td>-0.88</td>
<td>-0.018</td>
</tr>
<tr>
<td>13</td>
<td>24.4</td>
<td>274</td>
<td>-8.73</td>
<td>-2.02</td>
<td>-0.033</td>
</tr>
<tr>
<td>14</td>
<td>22.4</td>
<td>293</td>
<td>-6.76</td>
<td>-3.73</td>
<td>-0.026</td>
</tr>
<tr>
<td>15</td>
<td>21.9</td>
<td>278</td>
<td>-8.83</td>
<td>-2.01</td>
<td>-0.014</td>
</tr>
</tbody>
</table>

Statistics

<table>
<thead>
<tr>
<th></th>
<th>Milk (g/d)</th>
<th>Fat (g/d)</th>
<th>Protein (g/d)</th>
<th>SCS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean</td>
<td>23.3</td>
<td>306</td>
<td>-7.87</td>
<td>-2.84</td>
</tr>
<tr>
<td>SD</td>
<td>4.4</td>
<td>113</td>
<td>4.87</td>
<td>2.33</td>
</tr>
<tr>
<td>Relative bias (%)</td>
<td>0.2</td>
<td>3.7</td>
<td>3.3</td>
<td>-55.3</td>
</tr>
<tr>
<td>Relative standard error (%)</td>
<td>18.8</td>
<td>38.5</td>
<td>60.0</td>
<td>139.7</td>
</tr>
<tr>
<td>t test values (df = 14)</td>
<td>NA1</td>
<td>2.597</td>
<td>1.667</td>
<td>0.716</td>
</tr>
<tr>
<td>P-value</td>
<td>NA</td>
<td>$P = 0.021$</td>
<td>$P = 0.118$</td>
<td>$P = 0.489$</td>
</tr>
</tbody>
</table>

1NA = not applicable.

only 3.7% and 3.3% of the simulated allelic substitution effects. Relative bias was clearly greater for protein and SCS (−55.3% and −22.4%), showing an important overestimation (in absolute figures). Similarly, relative standard errors were lower for milk (38.5%) and fat (60.0%) compared with SCS (96.4%) and protein (139.7%). Table 3 also has the approximated t-test and P-values for milk, fat, protein, and SCS. The level of significance was greatest for milk ($P = 0.021$), followed by fat ($P = 0.11$).

This study showed that larger effects are, as expected, easier to estimate precisely. Still, the magnitude of the effects that could be detected was surprisingly low (below 0.1σp) compared with the results reported by Hayes and Goddard (2001) and based on a large number of studies. However, our results also showed large relative standard errors, even for the effect on milk that can be considered significant. This result is in line with the results of Hayes and Goddard (2001), who reported that small to medium QTL effects might simply be artifacts of experimental error. We also found the tendency to overestimate the size of the single gene effects as expected from the results reported by these authors (Hayes and Goddard, 2001). Small effects appeared to be most overestimated. However, the results of this simulation study may not prove whether the presented method is superior in its detection power to traditional methods such as that used by Szyda et al. (2005). Using the same data and a very similar approach to that of Szyda et al. (2005), the results obtained were nearly identical with this method (results not shown). However, the present method is easier and more general because it accepts genotypes from any genotyped animal and integrates smoothly into existing genetic evaluation models of any size and kind. Moreover, it allows genetic evaluations for traits where mixed inheritance models combining polygenic and single gene effects are required. Traditional methods using only some sires that are genotyped are unable to be used directly in this context because they relate more to QTL detection than to genetic evaluation. This method has a much larger scope.

In this study, the simulation approach was based on a real-life situation and compared, under the hypothesis that the effect exists, the estimated value to the simulated one. This method has merit in that it is as close as possible to the expected situation. The weak point is that this simulation is done under the hypothesis of a total independence of the simulated gene with the rest of the genome. This hypothesis is obviously far from reality. However, it is at the root of the mixed inheritance model, which does not consider interactions between the gene and the rest of the genome.
TABLE 4. Mean correlations over 10 independent repetitions between breeding values obtained from 2 random subsets representing the data for half of the cows with the 2 models (without or with regression on gene content) and for the 3 studied traits (milk, fat, and protein yields, and SCS)

<table>
<thead>
<tr>
<th>Group of animals</th>
<th>Milk Without</th>
<th>Milk With</th>
<th>Fat Without</th>
<th>Fat With</th>
<th>Protein Without</th>
<th>Protein With</th>
<th>SCS Without</th>
<th>SCS With</th>
</tr>
</thead>
<tbody>
<tr>
<td>All animals</td>
<td>0.870</td>
<td>0.875</td>
<td>0.893</td>
<td>0.895</td>
<td>0.915</td>
<td>0.919</td>
<td>0.752</td>
<td>0.751</td>
</tr>
<tr>
<td>Genotyped sires</td>
<td>0.836</td>
<td>0.841</td>
<td>0.854</td>
<td>0.855</td>
<td>0.853</td>
<td>0.856</td>
<td>0.712</td>
<td>0.712</td>
</tr>
<tr>
<td>Cows with records</td>
<td>0.776</td>
<td>0.780</td>
<td>0.786</td>
<td>0.787</td>
<td>0.841</td>
<td>0.843</td>
<td>0.748</td>
<td>0.748</td>
</tr>
</tbody>
</table>

Cross Validation of Mixed Inheritance Model Using Predicted Gene Content

Results of this cross-validation are summarized in Table 4. The correlation coefficients for breeding values for milk, fat, and protein estimated between the 2 subsets were slightly higher for the model with an additional regression on predicted gene content, the greatest difference being observed for milk, and then protein and fat. For SCS, correlation coefficients were similar for the 2 models. These results were expected, except for the inversion of the rank of fat and protein, given the results presented earlier and given the fact that small effects are more difficult to estimate precisely.

These results indicate that the model with a regression on predicted gene content has a greater capacity to predict breeding values, at least when single gene effects are sufficiently large (e.g., for milk). Results for fat and especially protein remained positive even when effects were previously found to be insignificant.

CONCLUSIONS

Theoretically, optimal algorithms to estimate missing gene contents are difficult to implement on large pedigrees and potentially not robust enough. Recently, a method was described by Gengler et al. (2007) that has the potential to be used in very large populations. The results reported by these authors were promising compared with currently available alternative methods. In the present study, the accuracy of the estimation and the use of gene content calculated by this method were tested using a different approach. Estimated gene content was used in the context of a mixed inheritance model linking GHR polymorphism to milk, fat, and protein yields and SCS. The validation of the method through simulations and permutations showed that the estimation of allele frequencies and of large allelic effects (e.g., milk) were reliable. Small effects (as for protein in our case) are still difficult to estimate precisely. Nevertheless, the results showed the expected pattern reported from a meta-analysis done by Hayes and Goddard (2001), with a tendency to show large relative standard errors and to overestimate the single gene effects. Integration of predicted gene content in genetic evaluation models was shown to be functional and has the potential to increase the accuracy of the estimation of breeding values. The method to approximate gene content could be used for detection of candidate gene effects but also in genetic evaluations for traits where mixed inheritance models are required, as long as single gene effects are sufficiently large, which was the case in this study for all traits except SCS.

ACKNOWLEDGMENTS

The authors acknowledge the Canadian Dairy Network (Guelph, Canada) and Semex Alliance (Guelph, Canada) for the provision of data and semen samples. Nicolas Gengler who is Research Associate of the National Fund for Scientific Research (Brussels, Belgium), acknowledges his support. Computations were facilitated by the grants 2.4.507.02 F and F.4552.05 of the National Fund for Scientific Research. This research was supported by the Federal Belgian Ministry of Small Enterprises, Traders and Agriculture-DGVI (Brussels, Belgium) (grant # S5983) and by Ministry of Agriculture of the Walloon Region of Belgium (MRW-DGA) (Namur, Belgium) (grant # D31–1112).

REFERENCES


APPENDIX

An alternative derivation of the conditional expectation of gene contents for nongenotyped animals given molecular and pedigree data method given by Gengler et al. (2007) can be based on its analogy to the prediction of unknown breeding values from known breeding values and pedigree data as:

$$\hat{\mathbf{g}}_x = (1 - \mathbf{A}_{xy} \mathbf{A}_y^{-1}) \left[ \begin{array}{c} \mu_g \\ \mathbf{g}_y - 
\mu_y \end{array} \right]$$

where $\hat{\mathbf{g}}_x$ is a vector of unknown breeding values, $1$ is a vector of ones, $\mathbf{g}_x$ is a vector of known breeding values, $\mathbf{A}_{xy}$ is the additive relationship matrix between individuals with unknown breeding values and their relatives with known breeding values, $\mathbf{A}_y$ is the additive relationship matrix among individuals with breeding values and $\mu_y$ is the average breeding value and could also be a genetic group estimate.

We can then rewrite breeding values as the sum of single gene effects for every biallelic locus $i$. By doing this we obtain the following prediction equations:

$$\begin{align*}
\hat{\mathbf{g}}_x &= \sum_i \hat{\alpha}_i \mathbf{q}_{yi} = (1 - \mathbf{A}_{xy} \mathbf{A}_y^{-1}) \left[ \sum_i \hat{\alpha}_i \mu_i \right] \\
&\quad \times \left[ \sum_i \hat{\alpha}_i \mathbf{q}_{yi} - \sum_i \hat{\alpha}_i \mu_i \right],
\end{align*}$$

where $\hat{\mathbf{g}}_x = \sum_i \hat{\alpha}_i \mathbf{q}_{yi}$, $\mu_y = \sum_i \hat{\alpha}_i \mu_i$, $\hat{\alpha}_i$ is the allele substitution effect for locus $i$, $\mathbf{q}_{yi}$ is a vector of known gene contents (genotyped animals) for locus $i$, $\mathbf{q}_i$ is a vector of unknown gene contents (unogenotyped animals) for locus $i$, $\mu_i$ is the average allele content for locus $i$ which is also equal to the allele frequency $\times 2$. Under certain hypotheses, such as the normality of the contributions of single gene effects to breeding values, we can write for a given locus $i$:

$$\begin{align*}
\hat{\mathbf{q}}_{xi} &= (1 - \mathbf{A}_{xy} \mathbf{A}_y^{-1}) \left[ \hat{\alpha}_i \mu_i \right] \\
\hat{\mathbf{q}}_{yi} &= (1 - \mathbf{A}_{xy} \mathbf{A}_y^{-1}) \left[ \hat{\alpha}_i \mathbf{q}_{yi} - \hat{\alpha}_i \mu_i \right].
\end{align*}$$

The conditional expectation of gene contents for nongenotyped animals, given molecular and pedigree data, are then simply derived by dividing both sides of the equation by the allele substitution effect $\hat{\alpha}_i$:

$$\mathbf{q}_s = (1 - \mathbf{A}_{xy} \mathbf{A}_y^{-1}) \left[ \hat{\alpha}_i \mathbf{q}_{yi} - \hat{\alpha}_i \mu_i \right].$$