

# From the pinhole camera ... to the telescope and ... from the telescope ... to the optical interferometer



<http://galileoscope.org>





## Case of 6 Kits

\$150.00

1

ADD TO CART

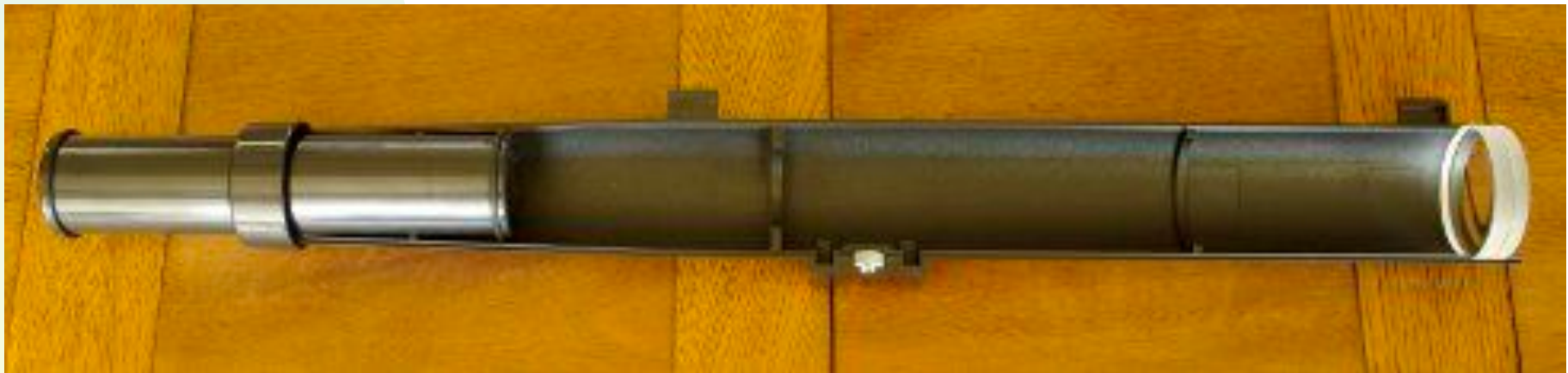
Maximum number of cases per order: 11

SKU: GSCOPE

# Galileoscope



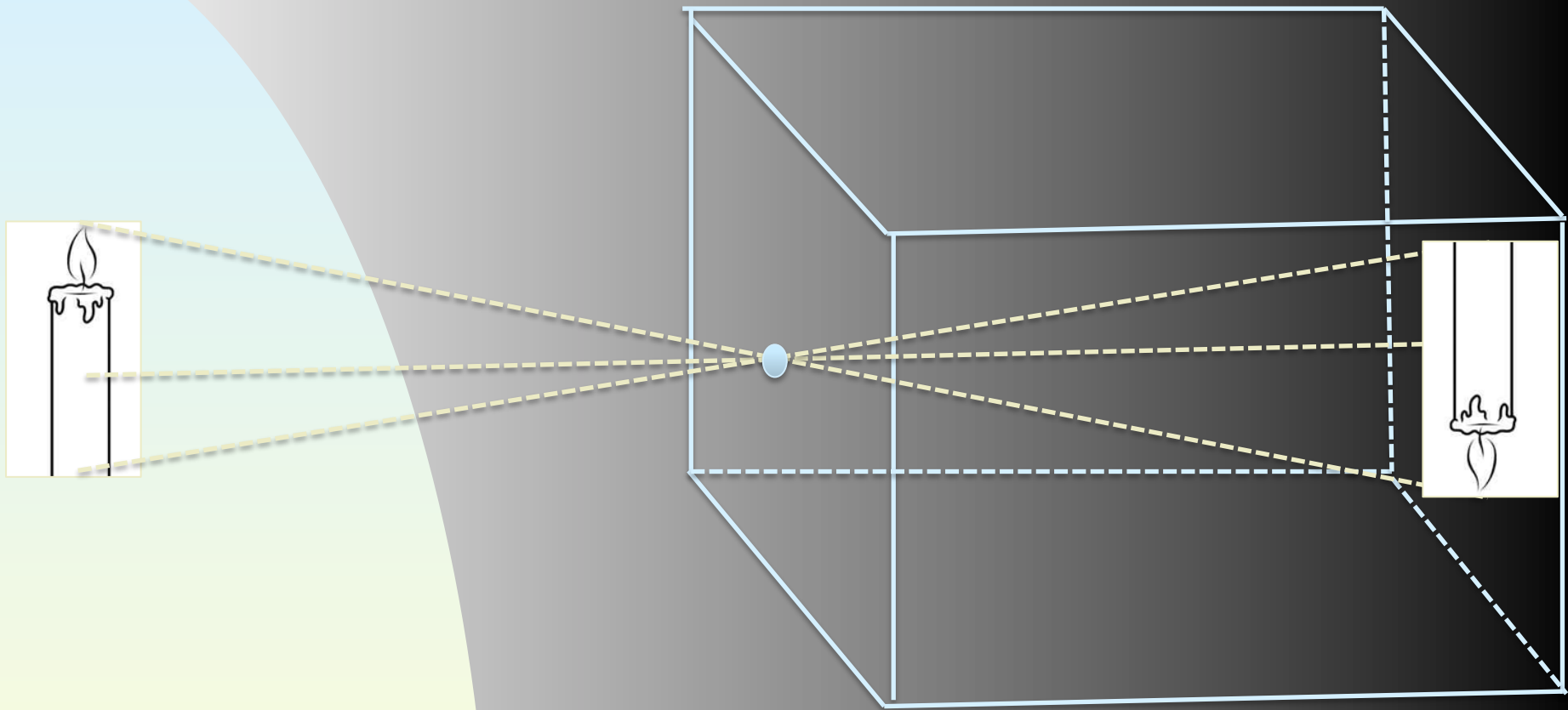
$D = 5\text{cm}$ ,  $F/D = 10$ ,  $G = 17, 25, 50$ ; cost: 18 €





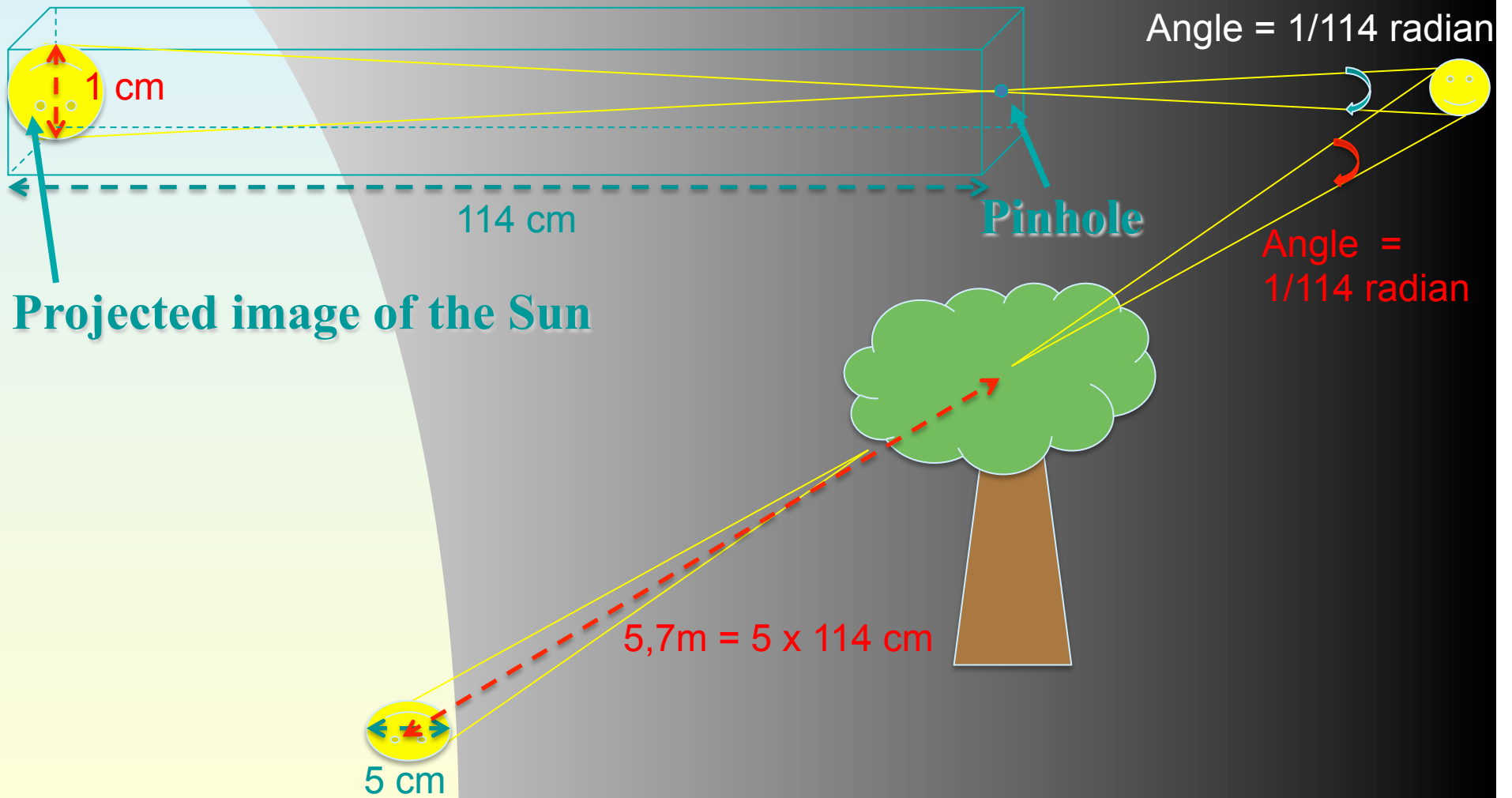
# Deconvolution Theorem

# Camera obscura

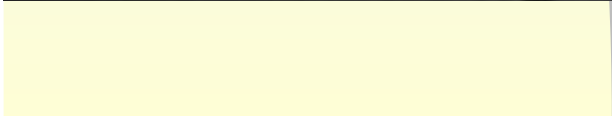


Pinhole camera

## Camera obscura (cf. shoe box)









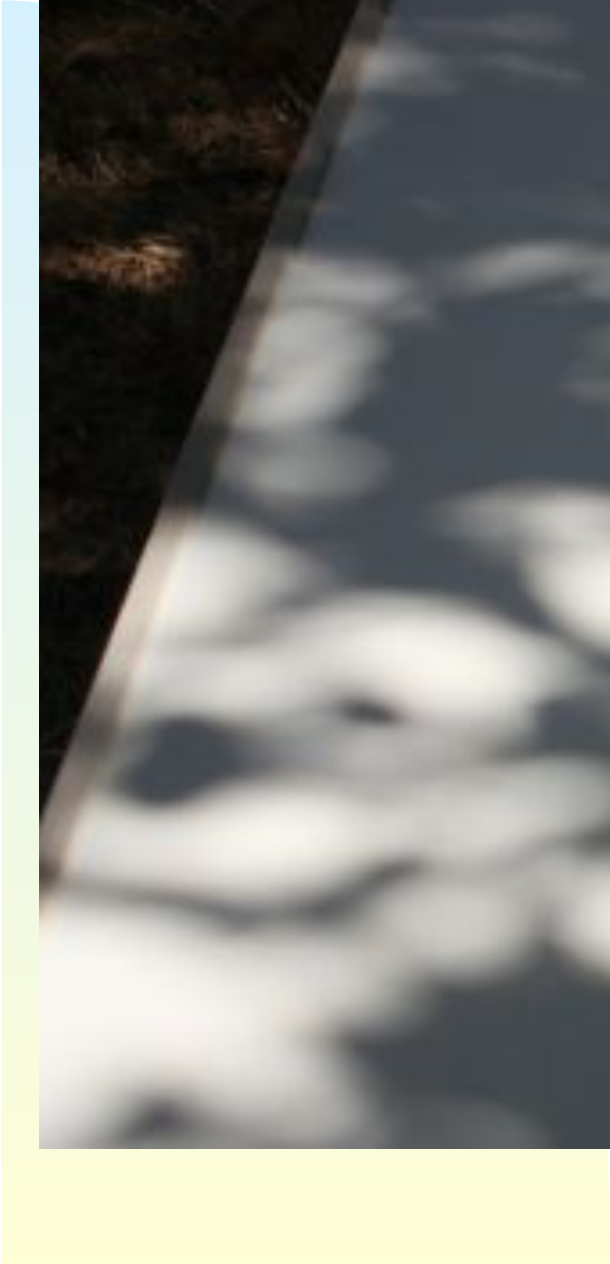














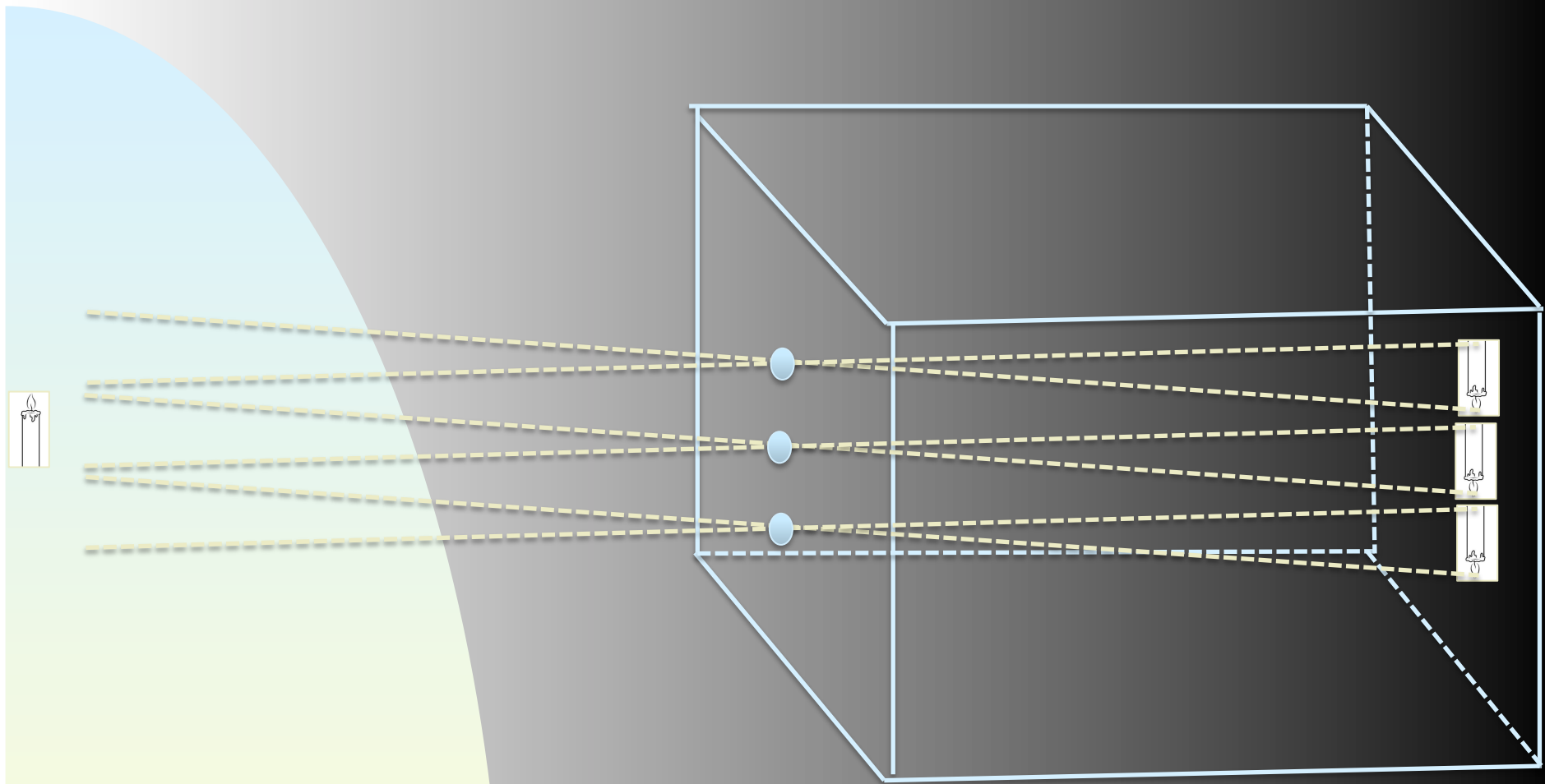






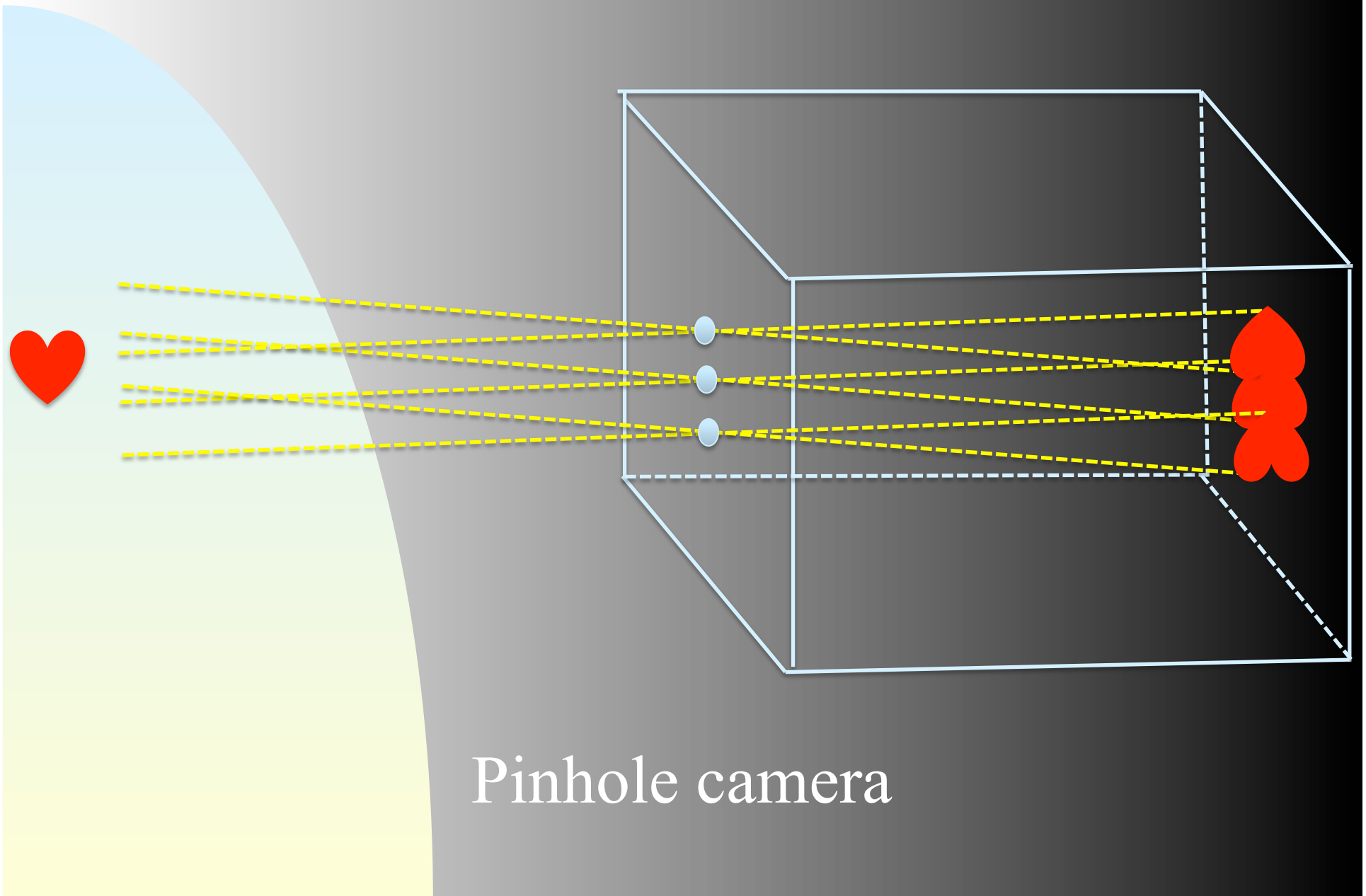
**Du feuillage  
des arbres  
aux grands  
télescopes**

# Camera obscura



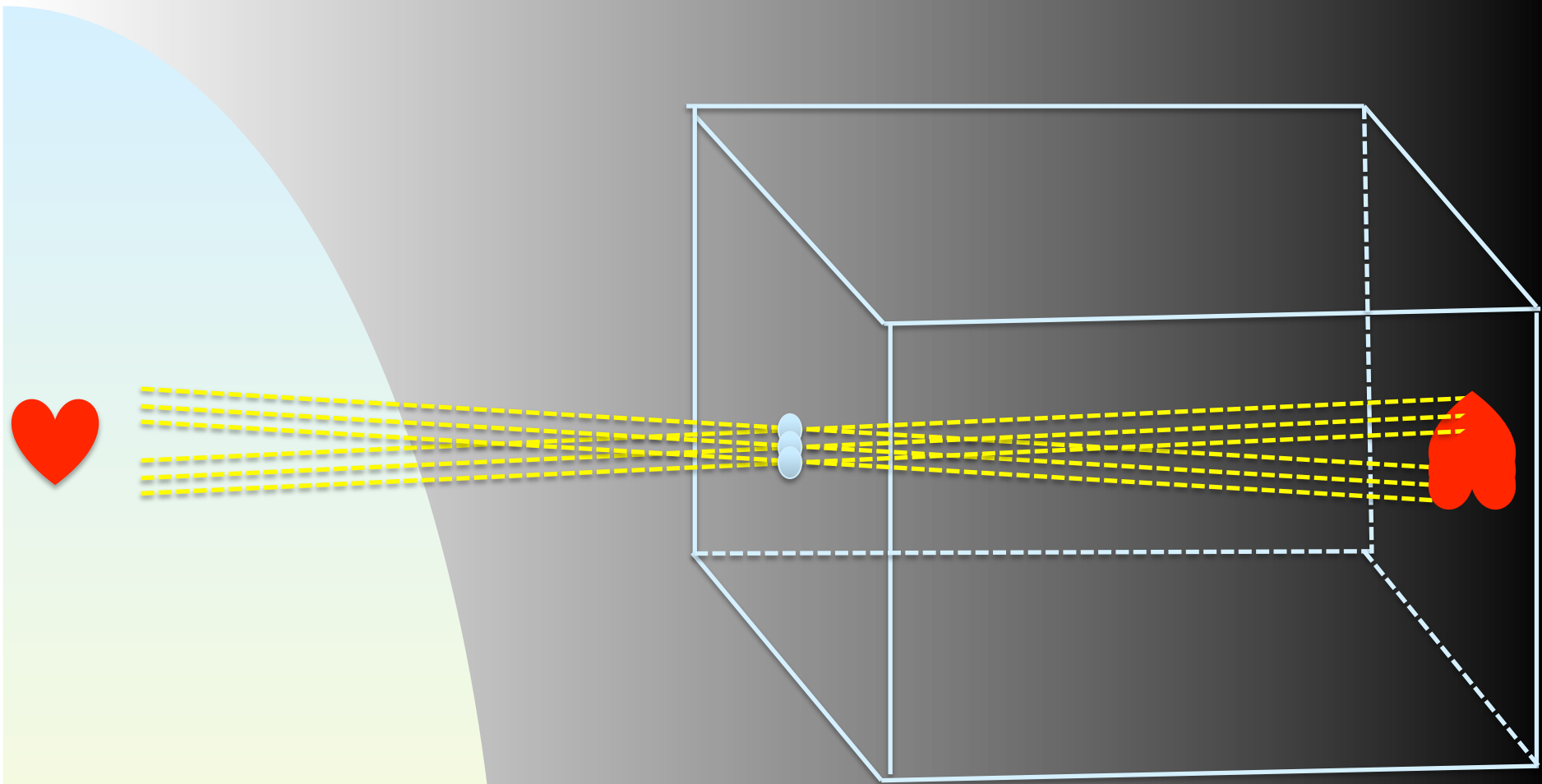
Pinhole camera

# Camera obscura

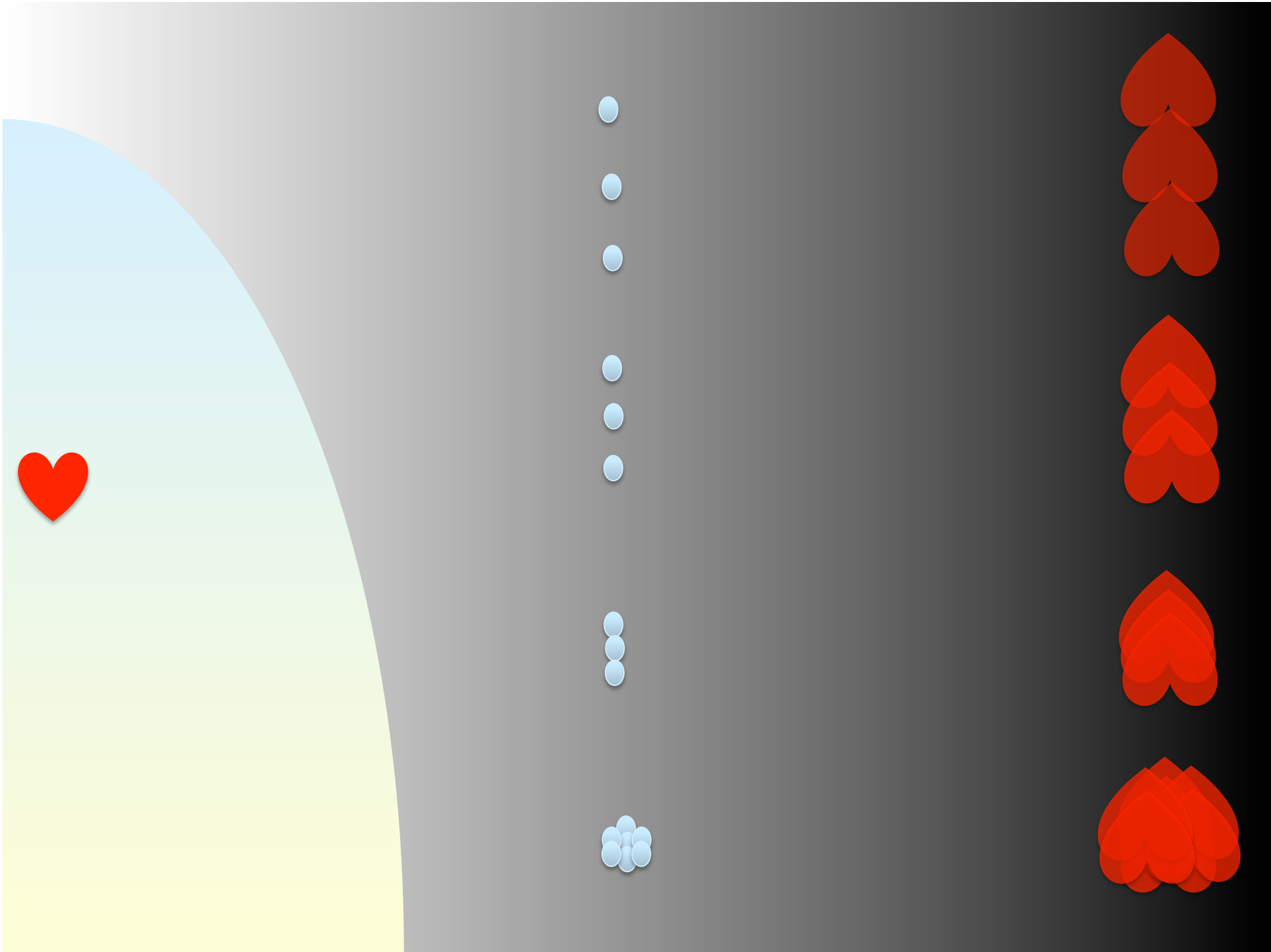


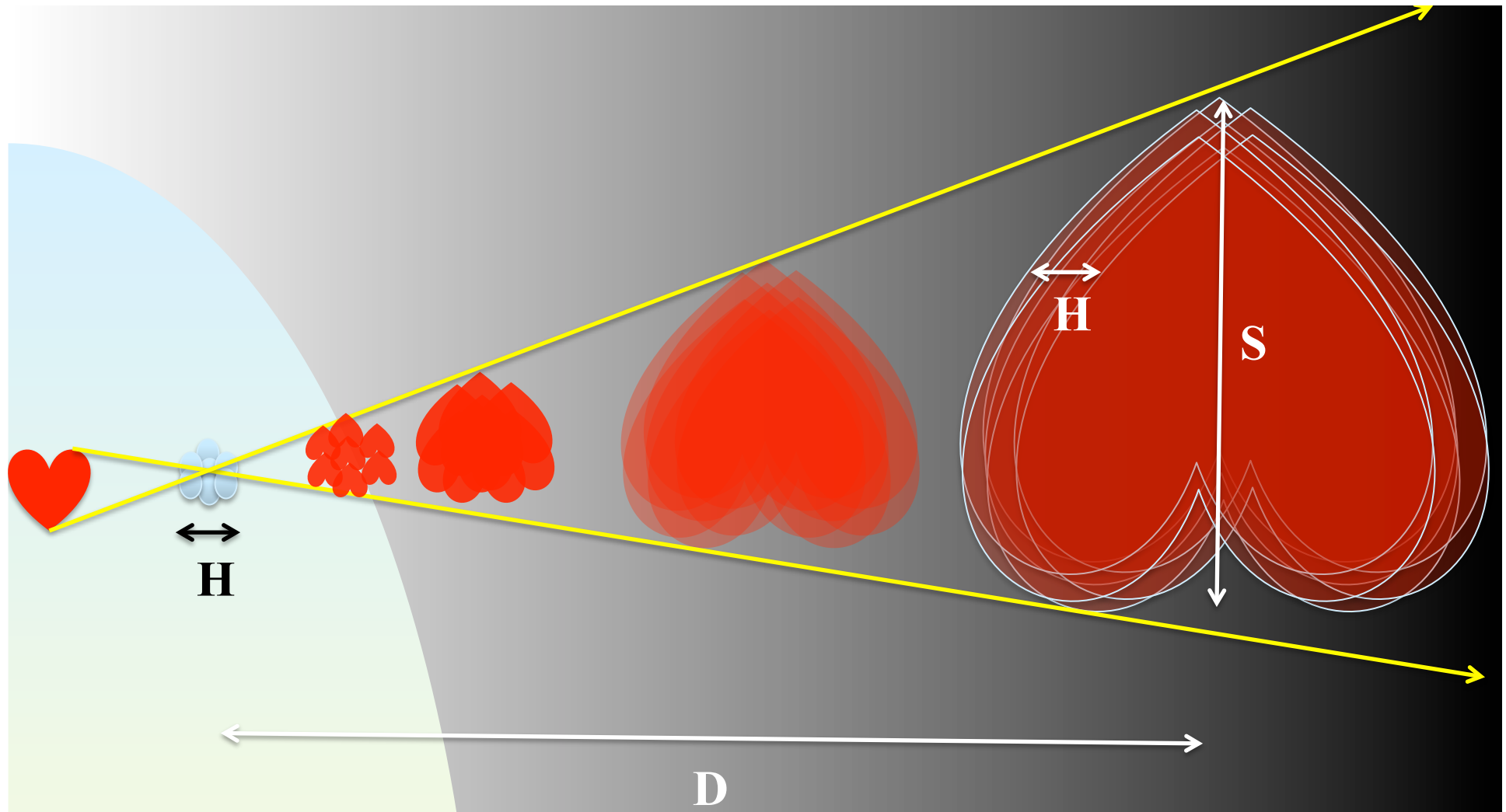
Pinhole camera

# Camera obscura



Pinhole camera

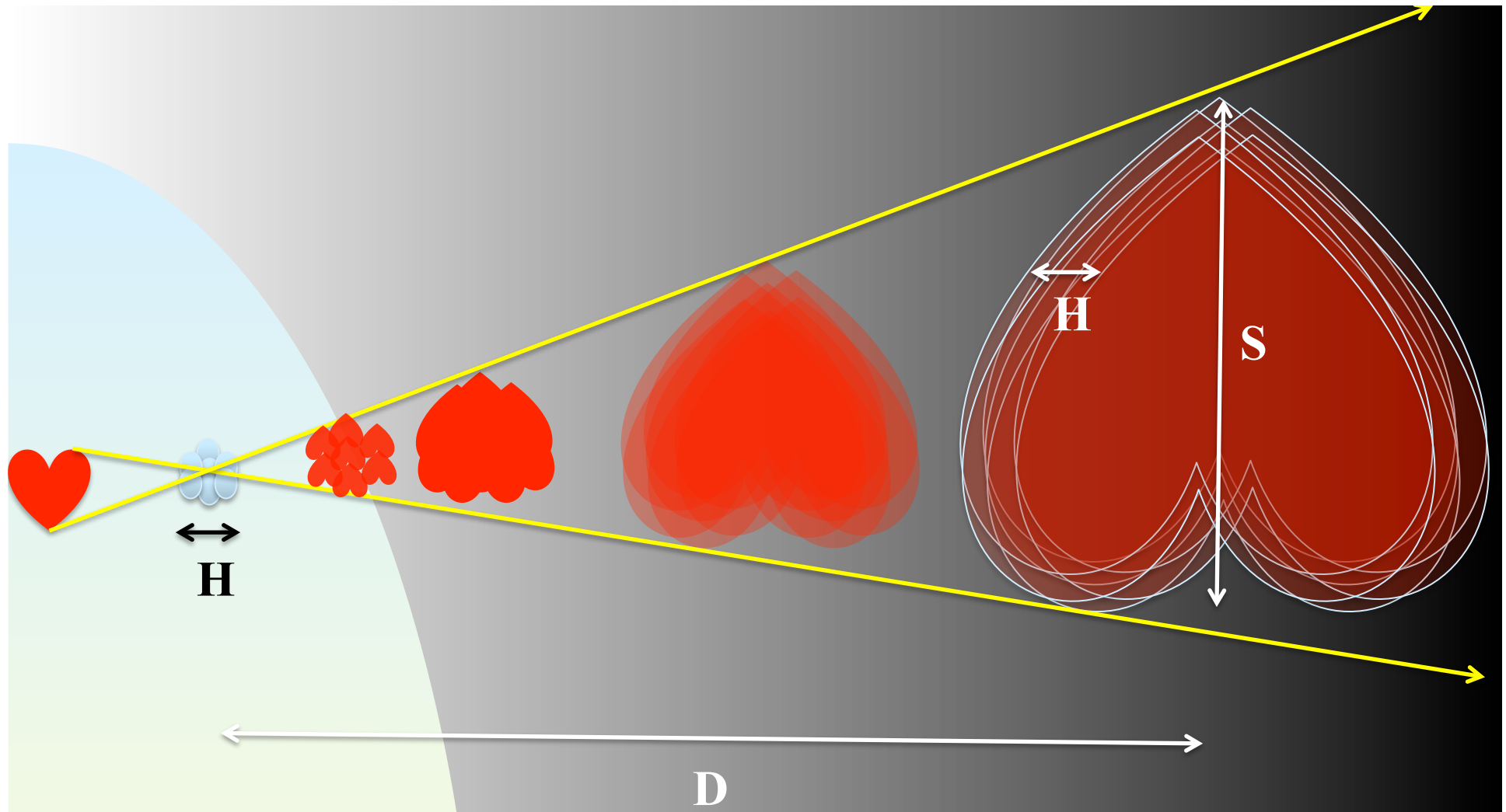




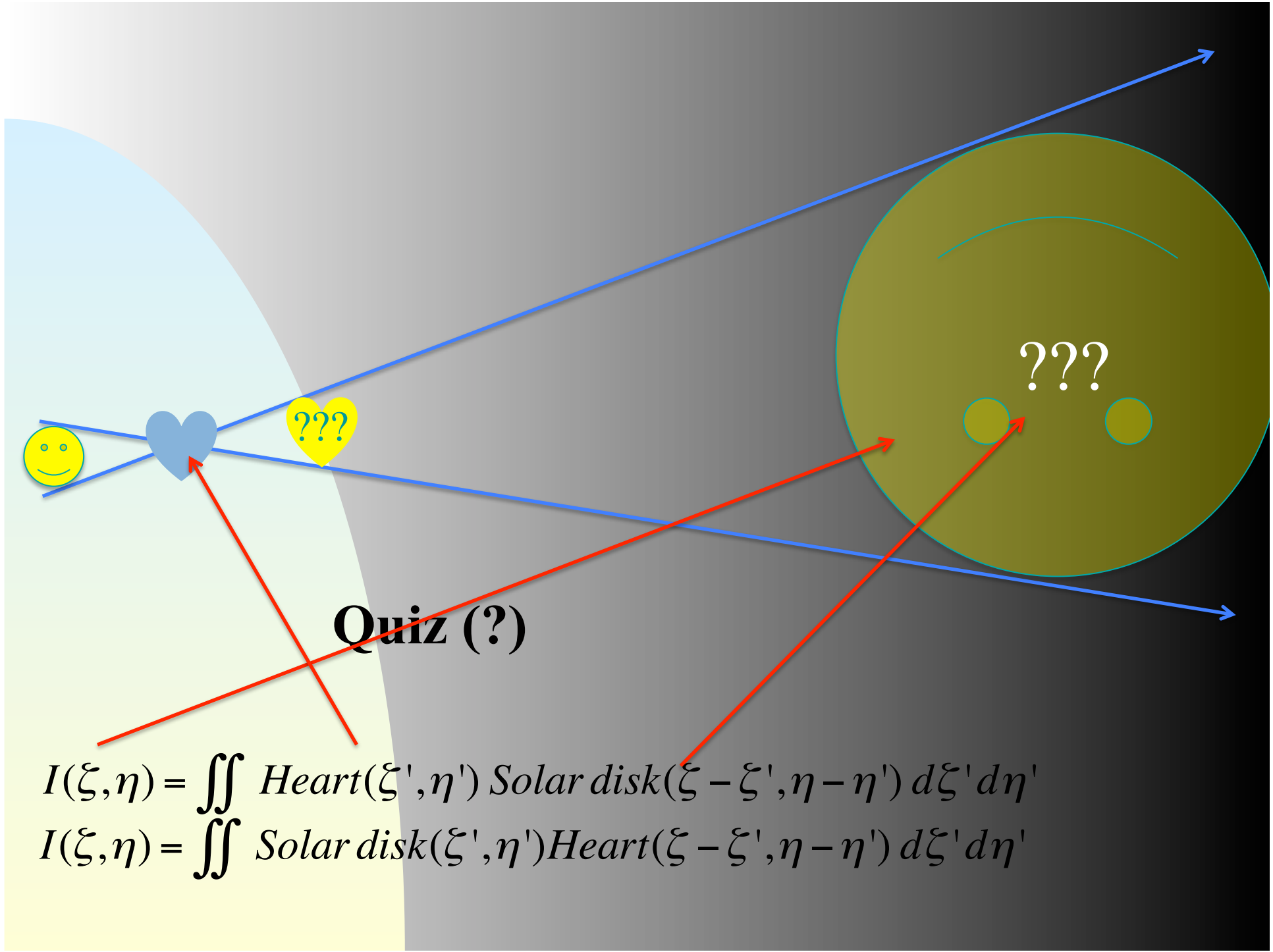
The blur  $B$  of the hearts is proportional to  $H$ , and inversely proportional to  $S$ , which is itself proportional to  $D \rightarrow B \propto H / D$

The angular resolution  $\Phi = H / D$





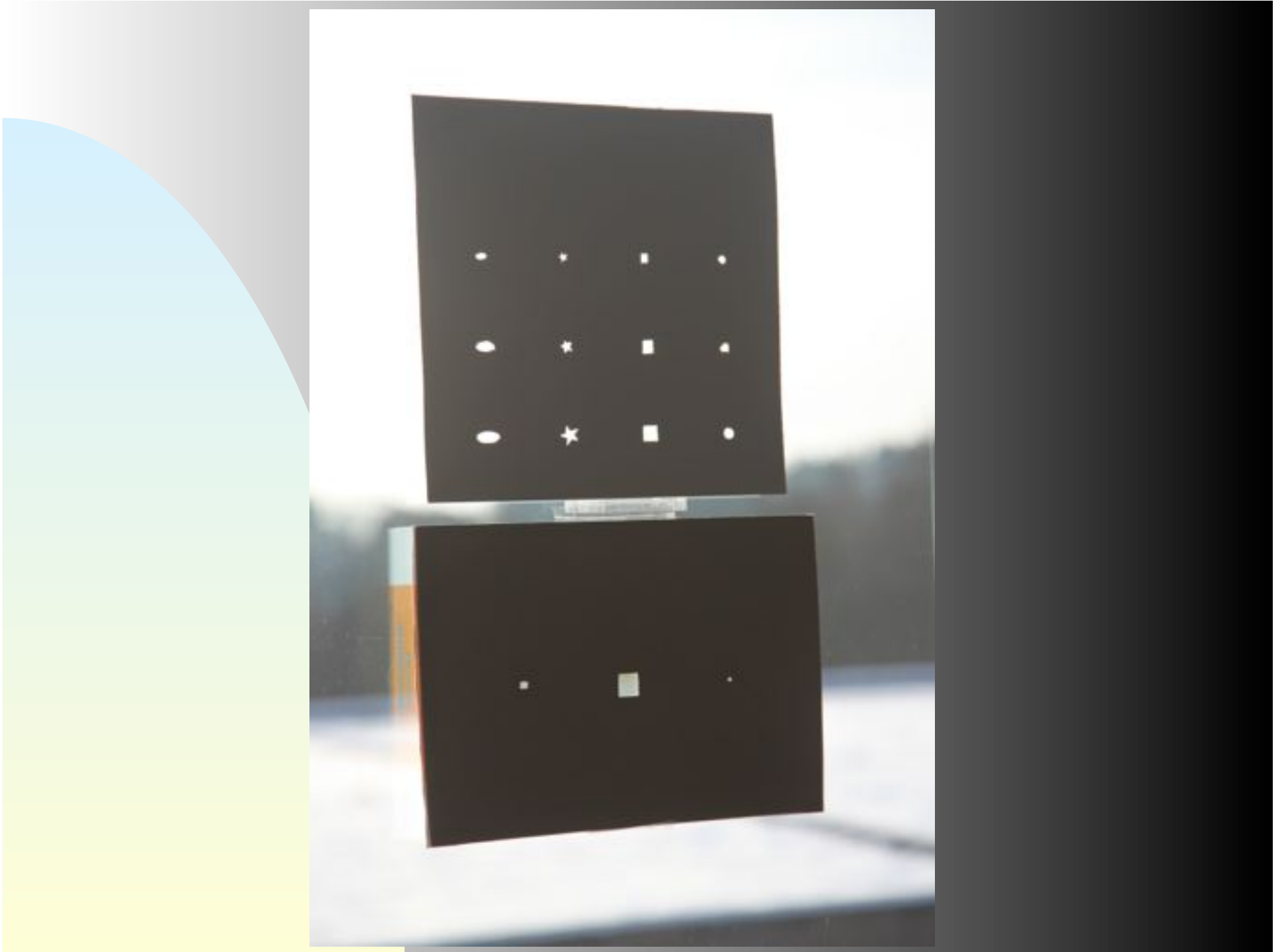
**The surface brightness SB of the hearts is proportional to  $H^2$ , and inversely proportional to  $S^2$ , and thus to  $D^2 \Rightarrow SB \propto (H / D)^2$**

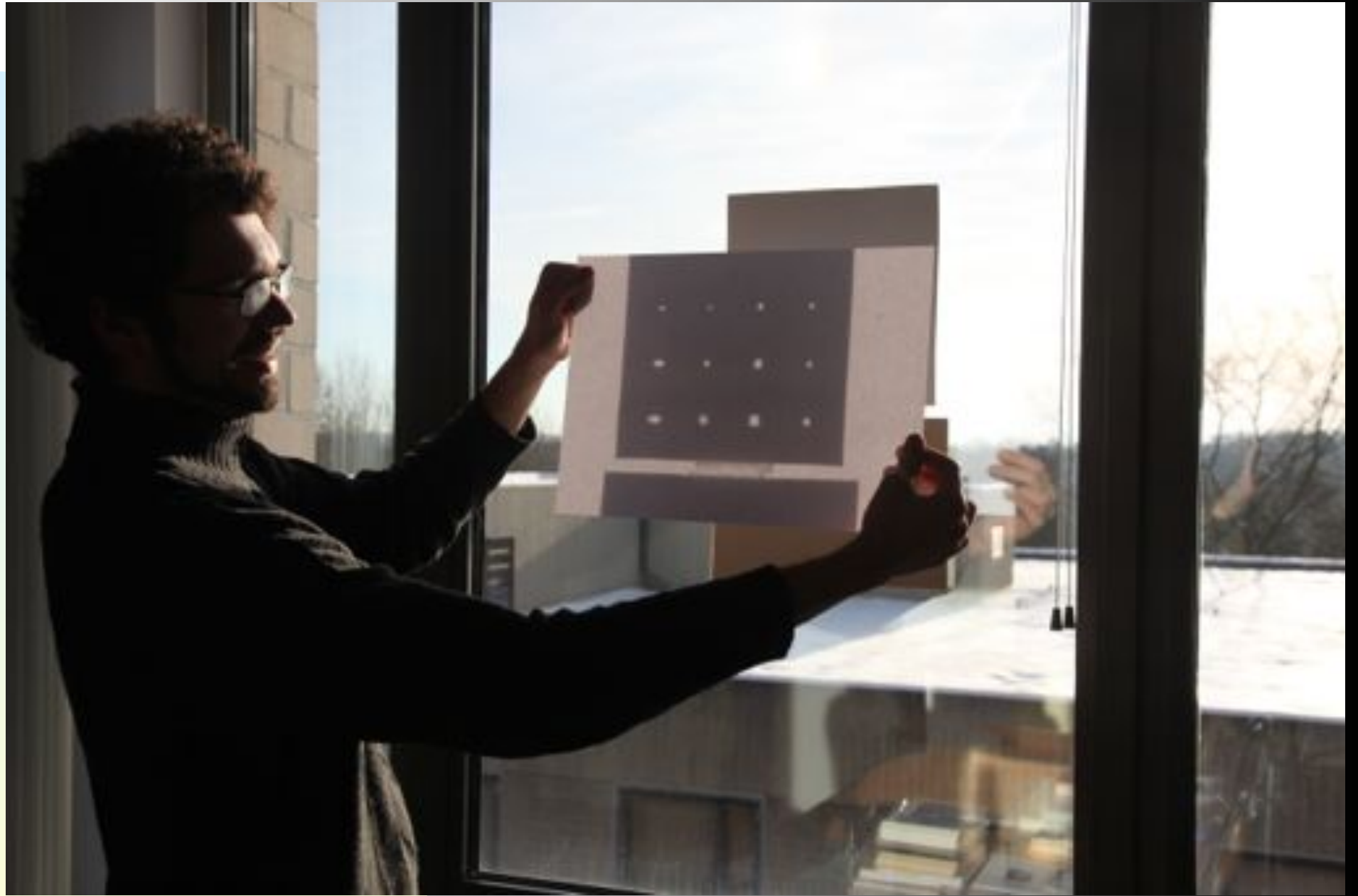


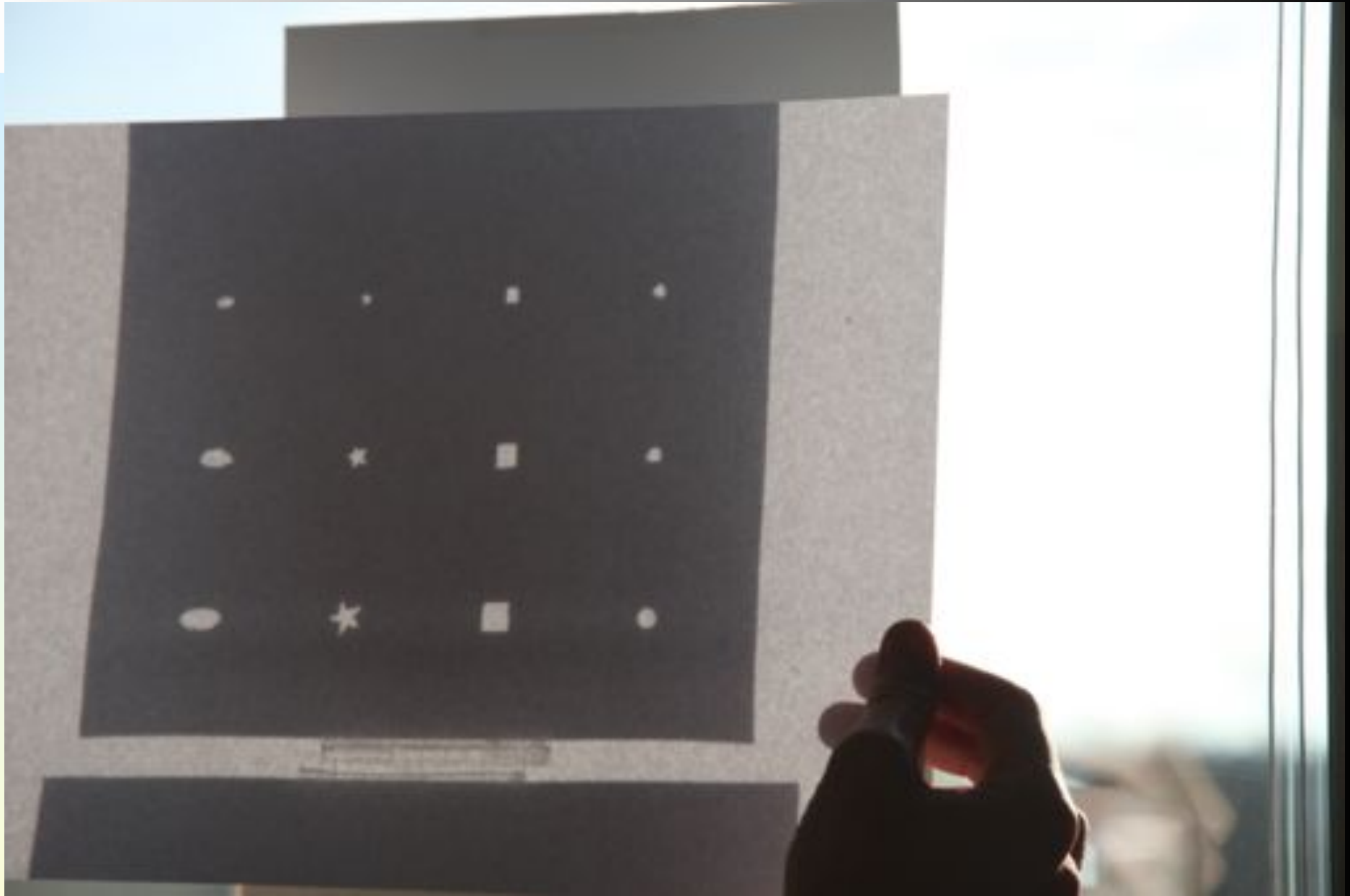
**Quiz (?)**

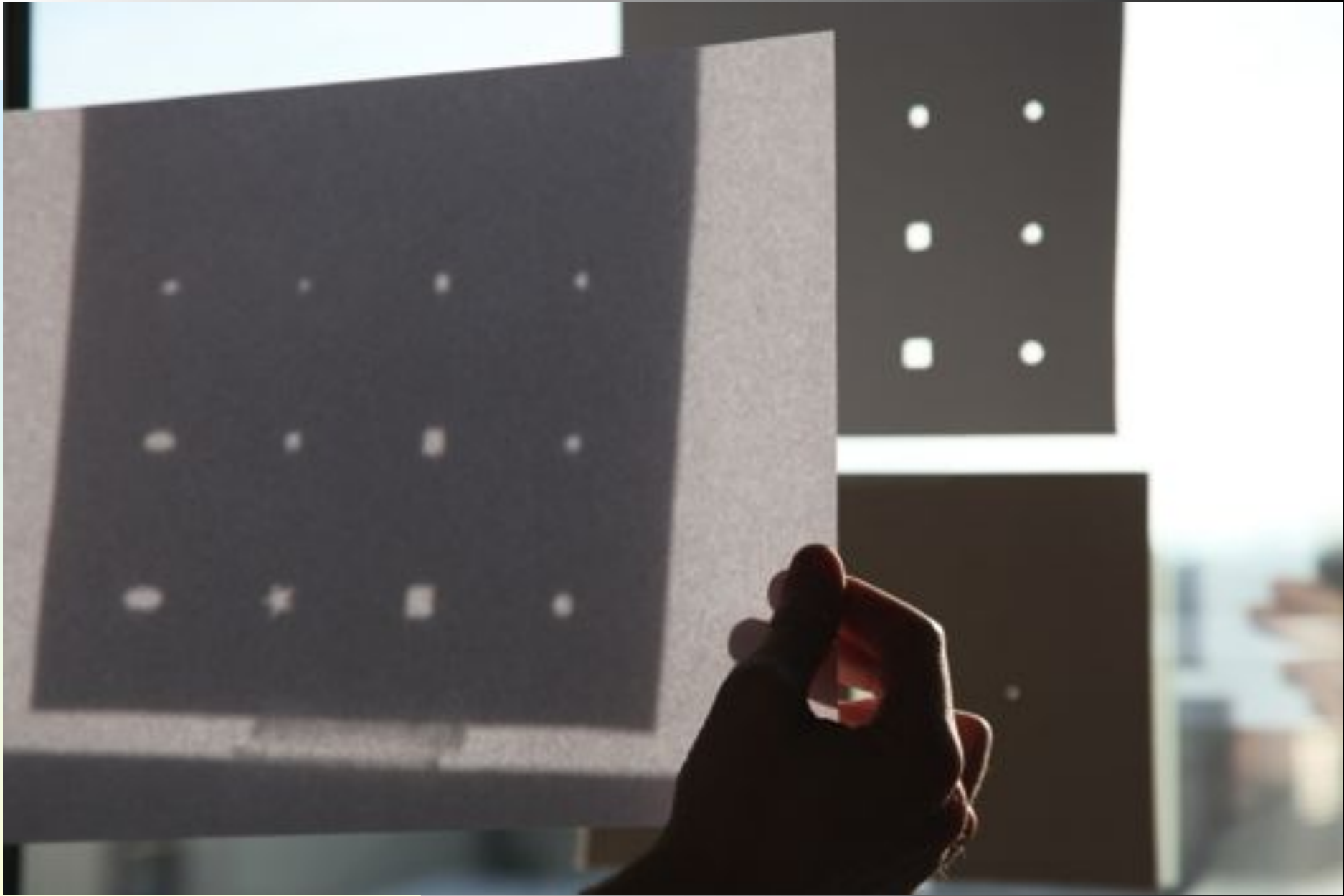
$$I(\xi, \eta) = \iint \text{Heart}(\xi', \eta') \text{Solar disk}(\xi - \xi', \eta - \eta') d\xi' d\eta'$$

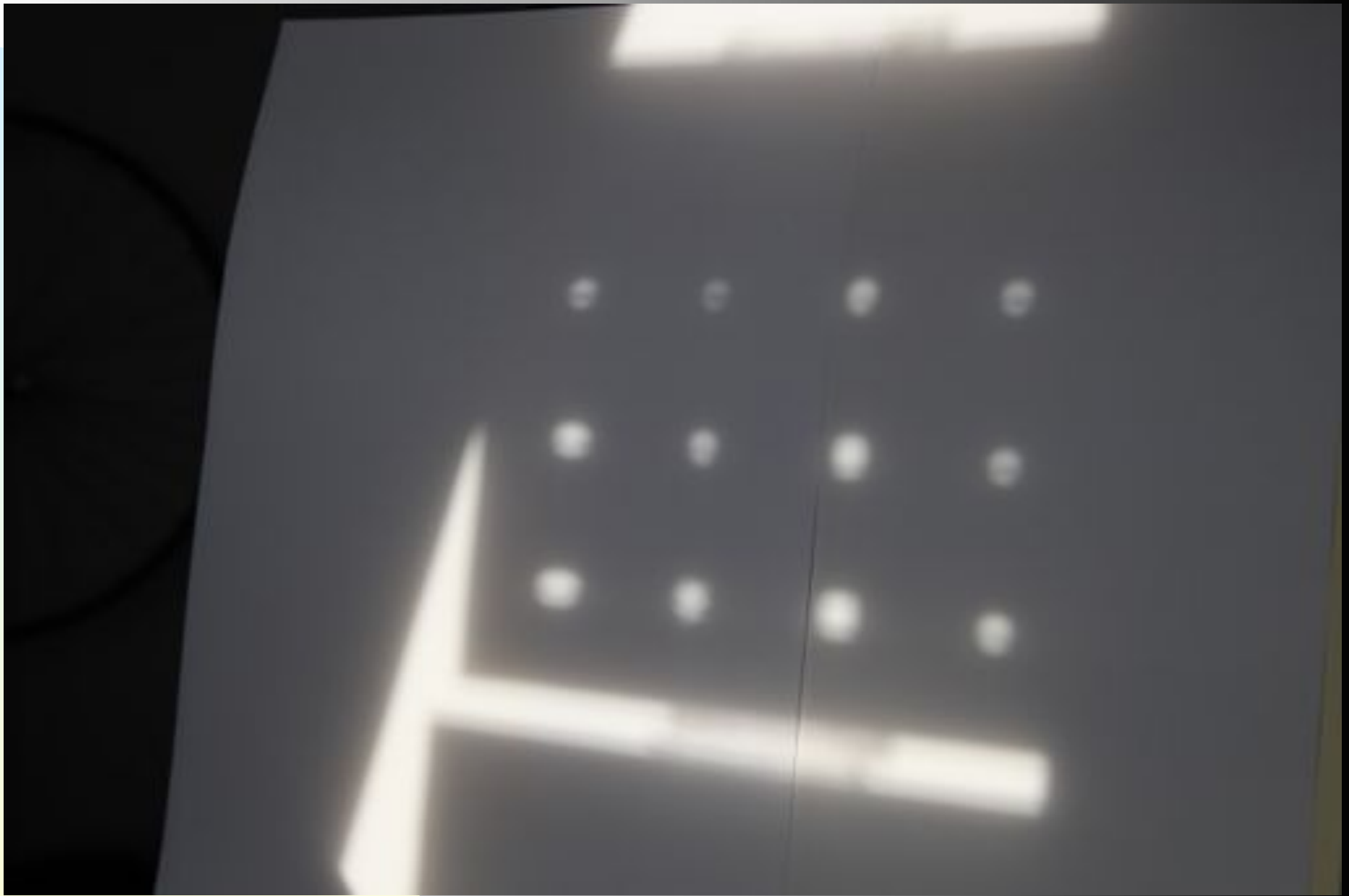
$$I(\xi, \eta) = \iint \text{Solar disk}(\xi', \eta') \text{Heart}(\xi - \xi', \eta - \eta') d\xi' d\eta'$$

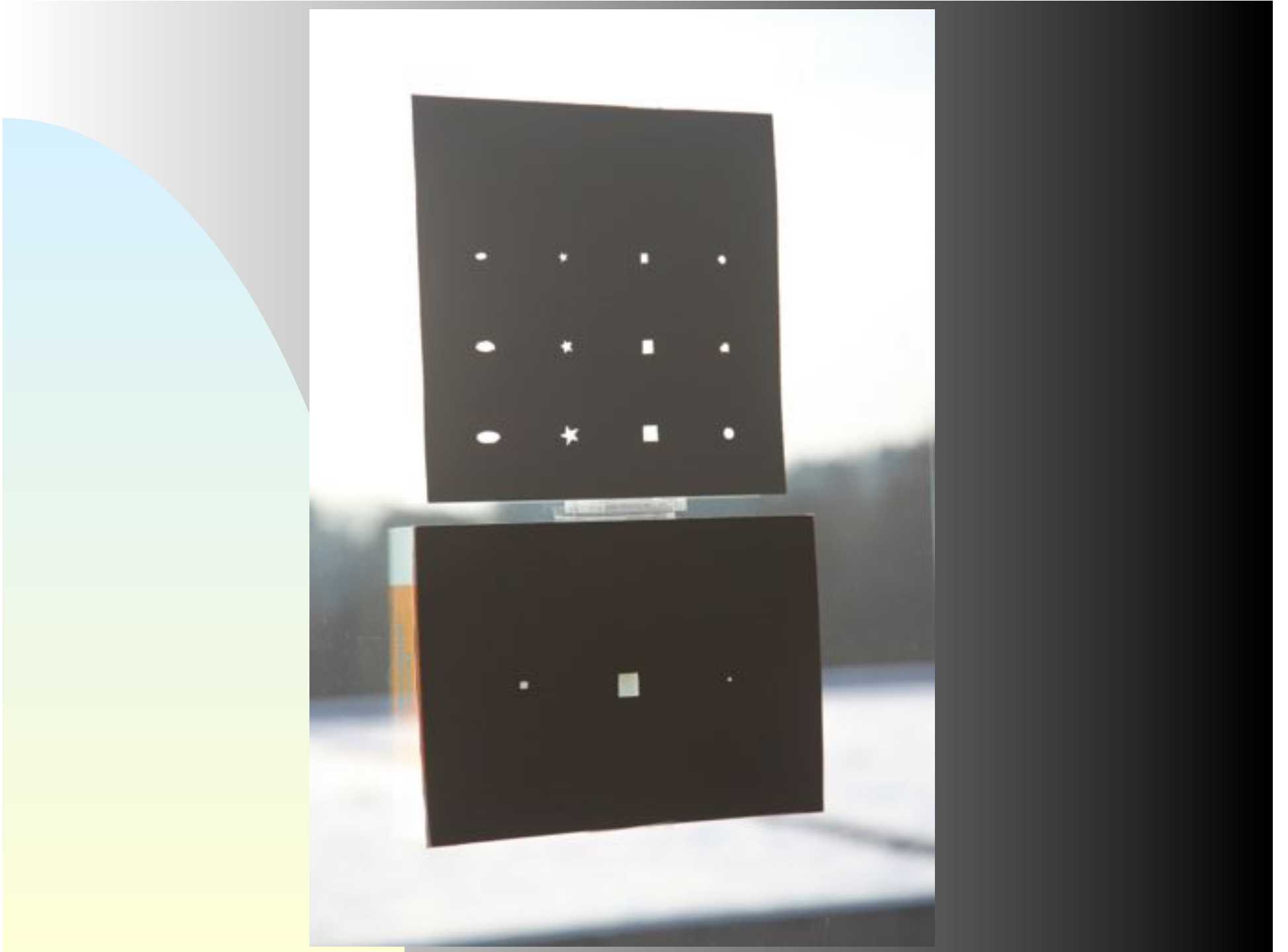




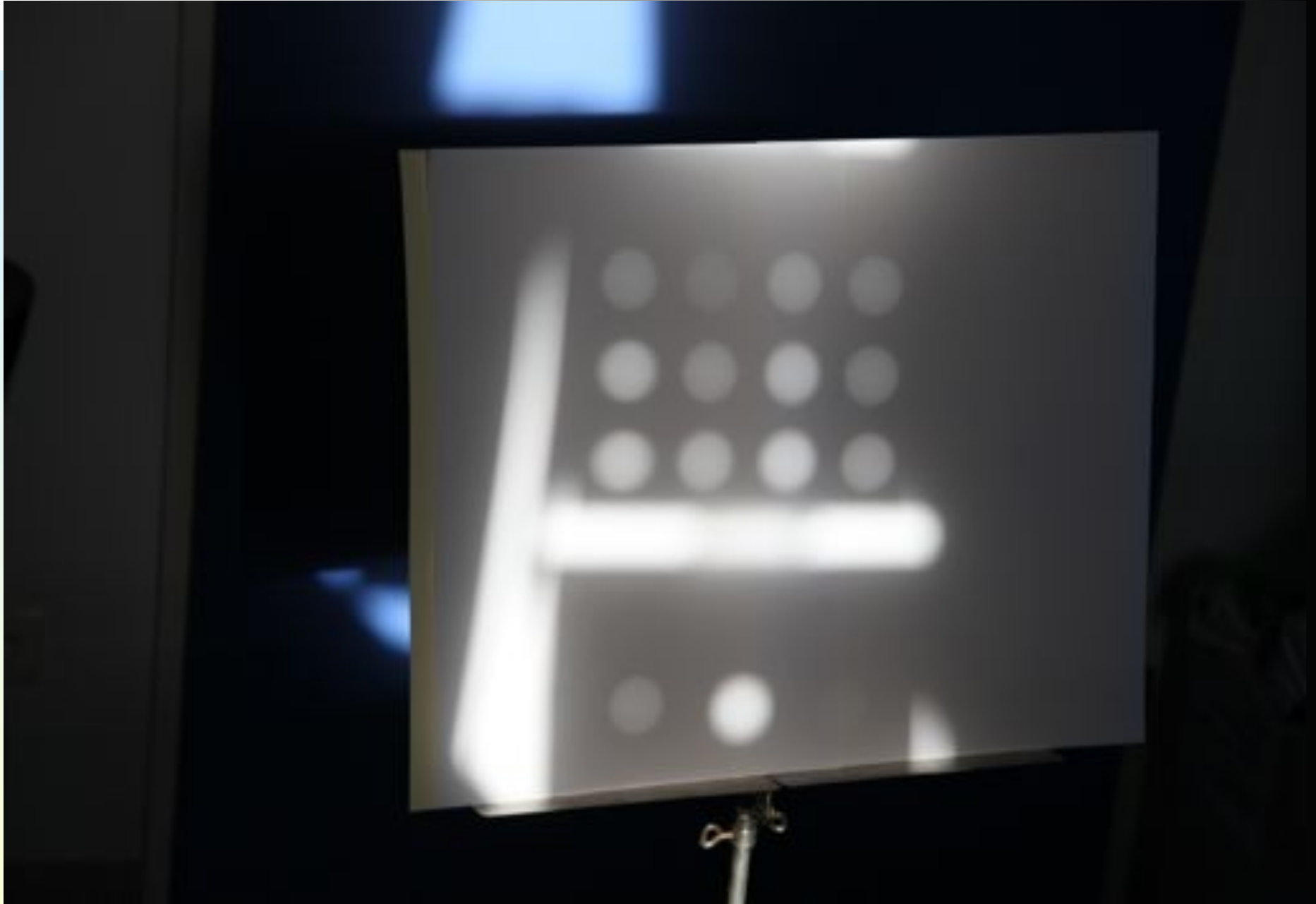


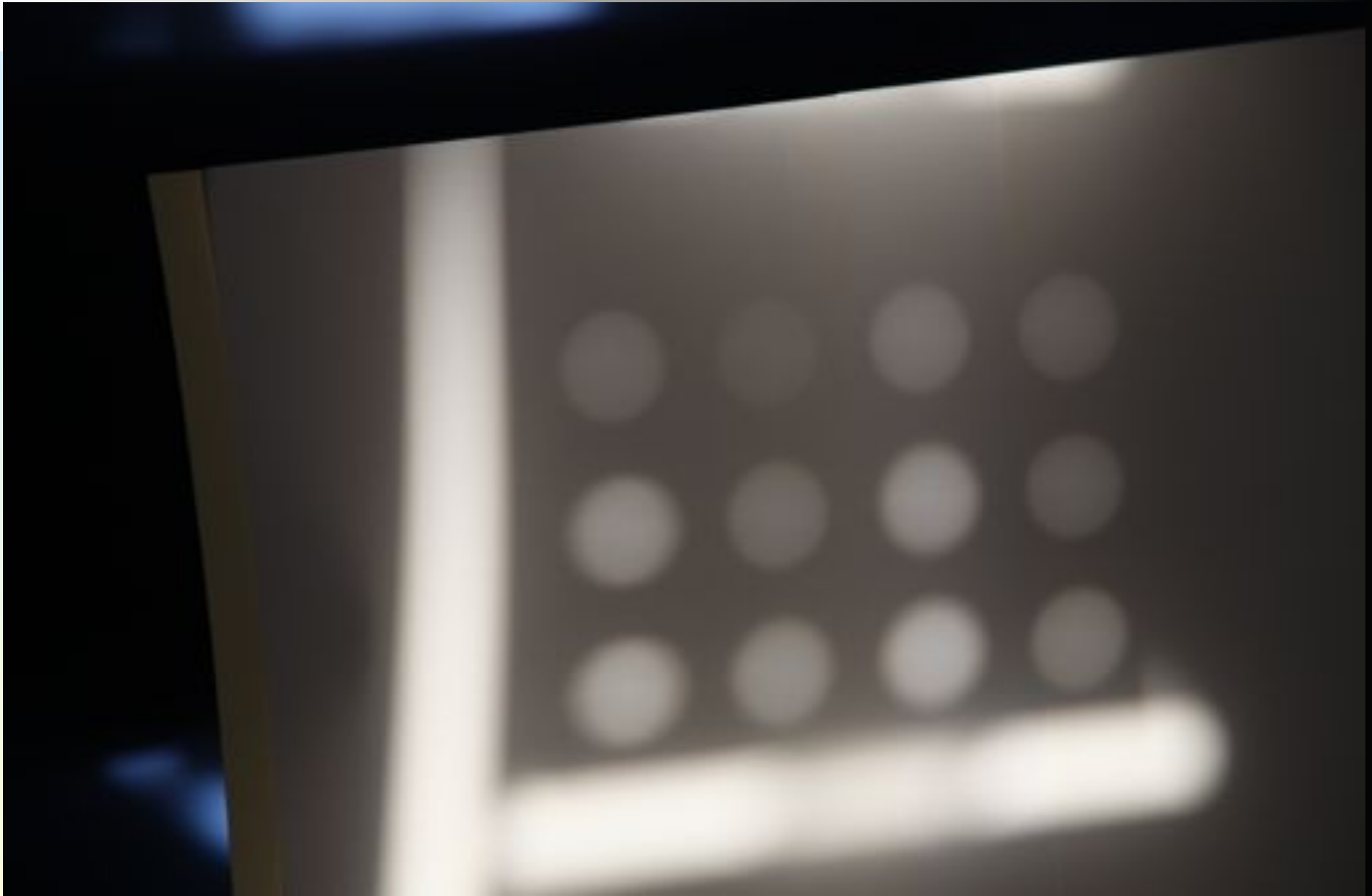




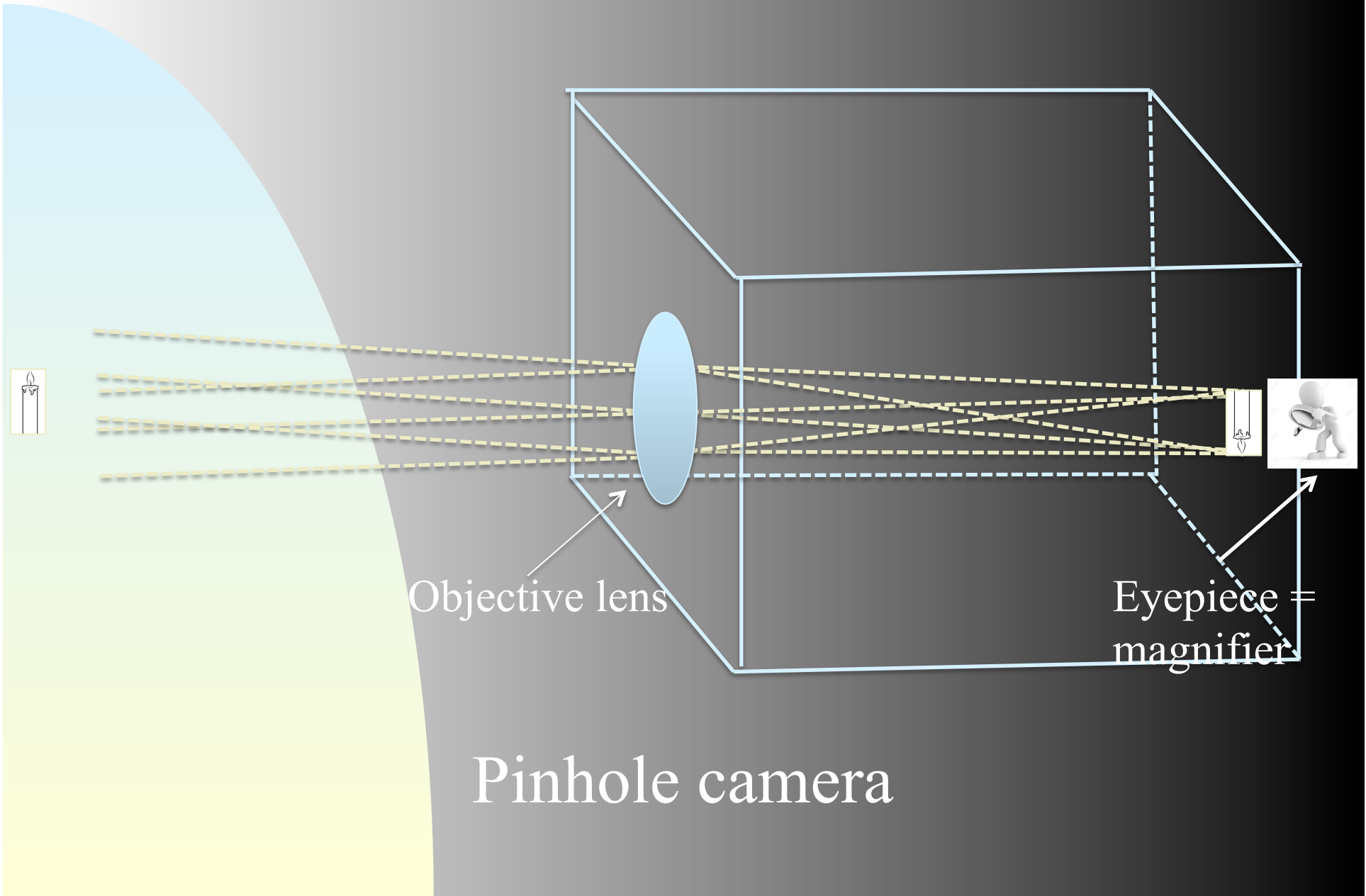








# Camera obscura



Pinhole camera

# 9 Fourier Optical Elements

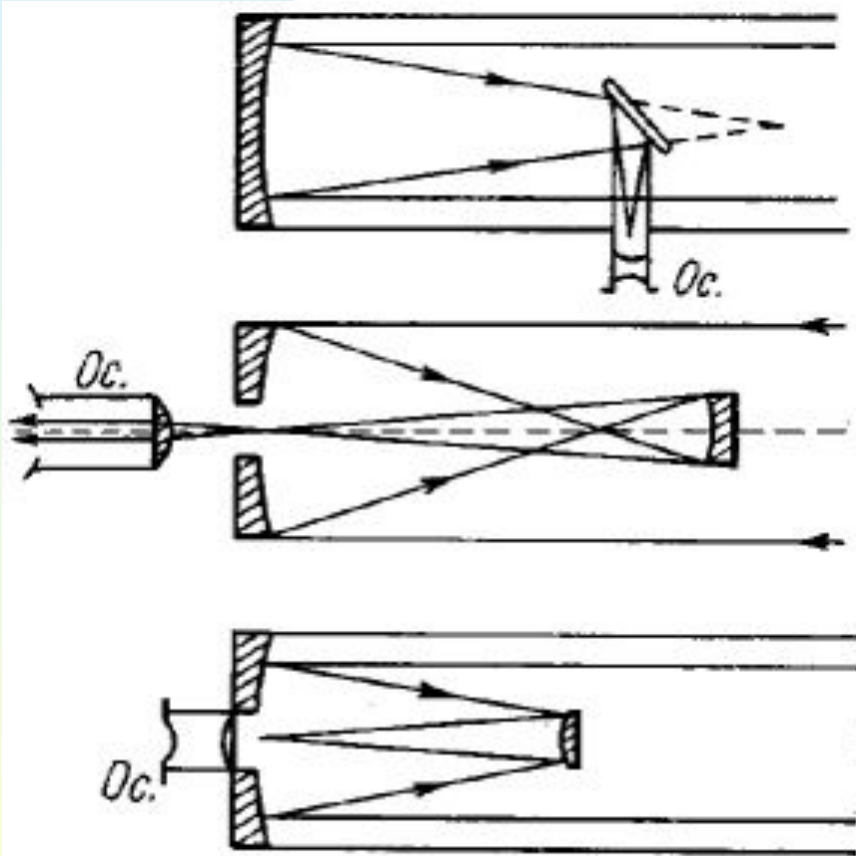
## 9.3 Telescope applications

- **9.3.1 Optical telescopes**
- **9.3.2 Coupled telescopes**
- **9.3.3 X-ray telescopes**
- **9.3.4 Radio-telescopes and radio-interferometers**

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.1 Optical telescopes



(a)



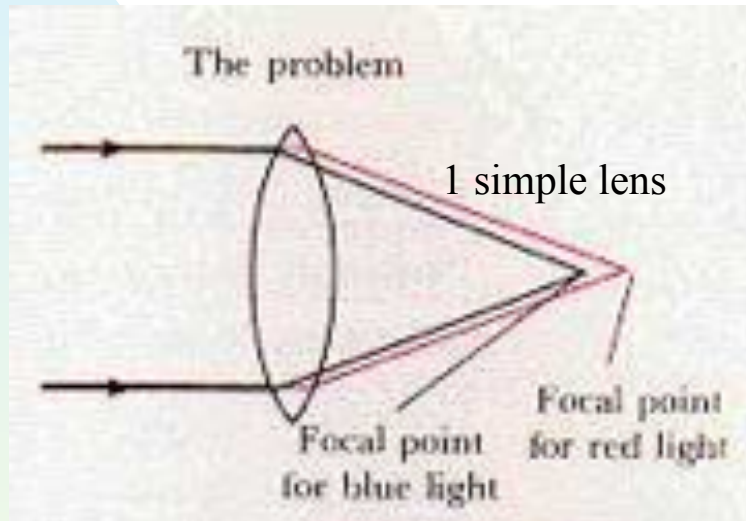
(b)

# 9 Fourier Optical Elements

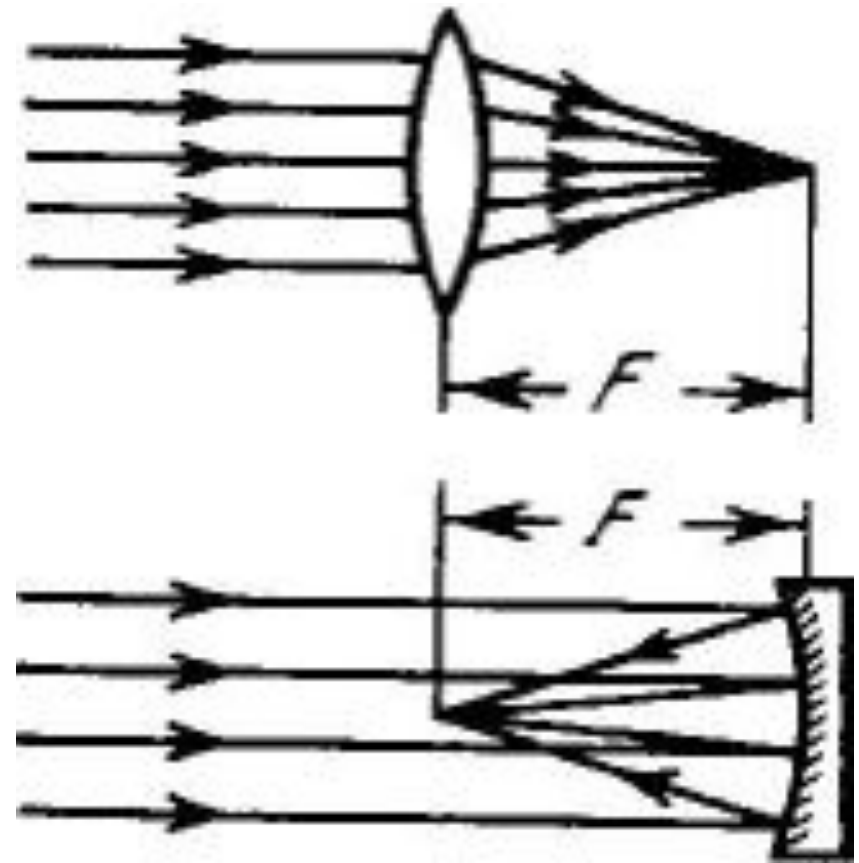
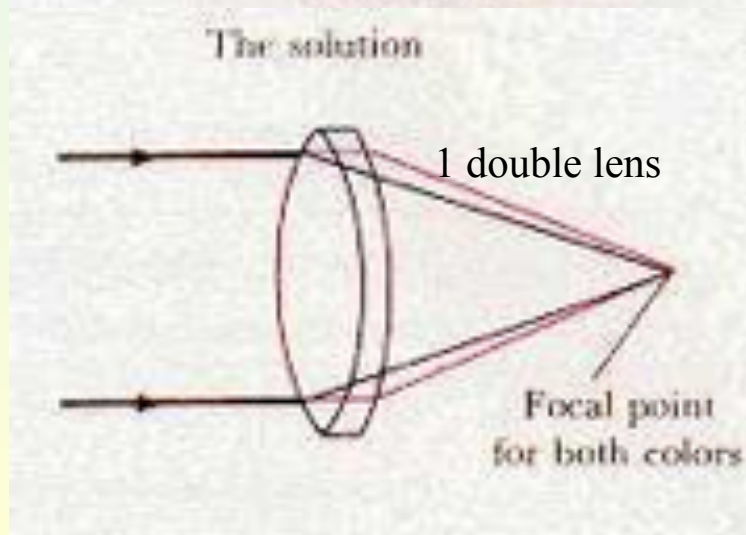
## 9.3 Telescope applications

### 9.3.1 Optical telescopes

(a)



(b)

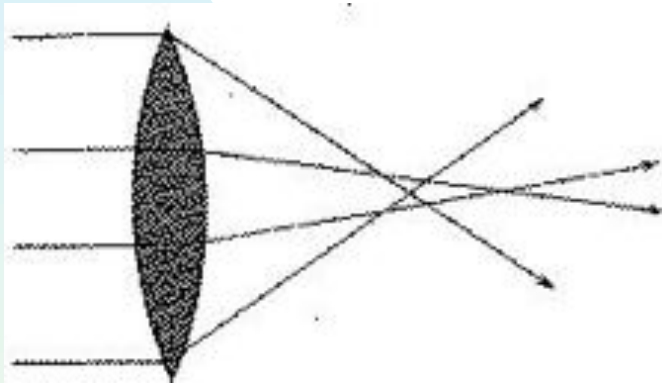


(c)

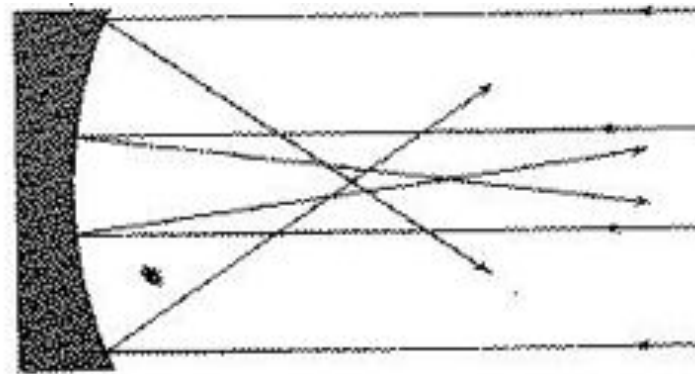
# 9 Fourier Optical Elements

## 9.3 Telescope applications

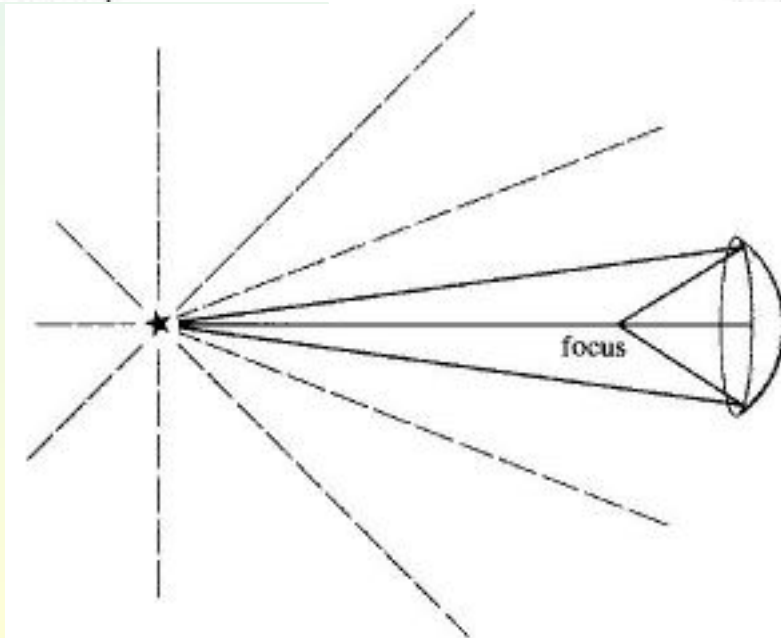
### 9.3.1 Optical telescopes



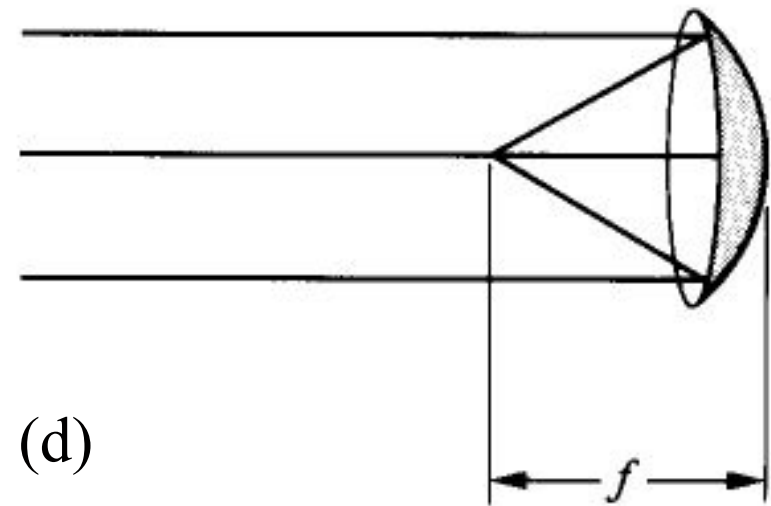
(a)



(b)



(c)



(d)

# 9 Fourier Optical Elements

## 9.3 Telescope applications

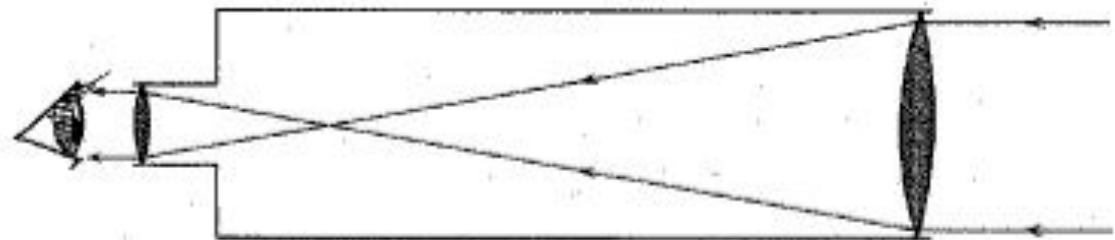
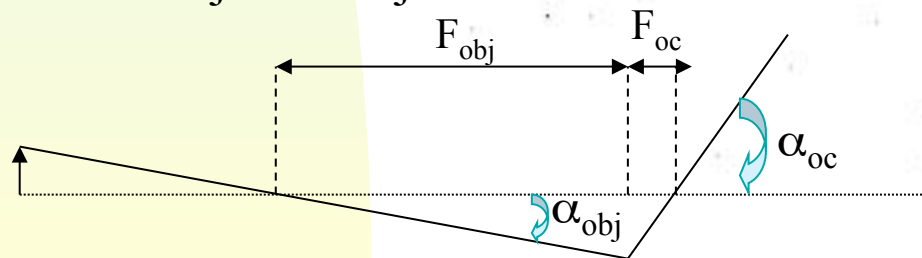
### 9.3.1 Optical telescopes

$$\phi = E S = \pi D^2 E / 4,$$

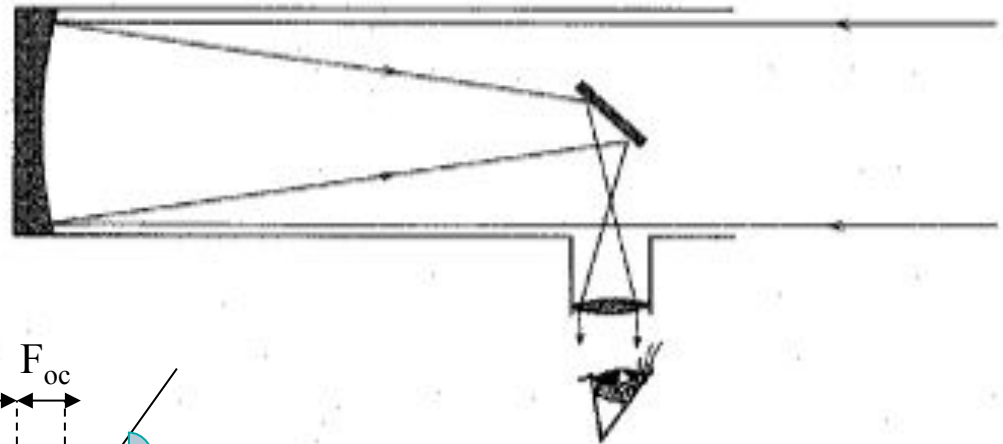
$$f = F / D,$$

$$E' \sim f^2.$$

$$G = \alpha_{oc} / \alpha_{obj} = F_{obj} / F_{oc}.$$



(a)



(b)



# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.1 Optical telescopes

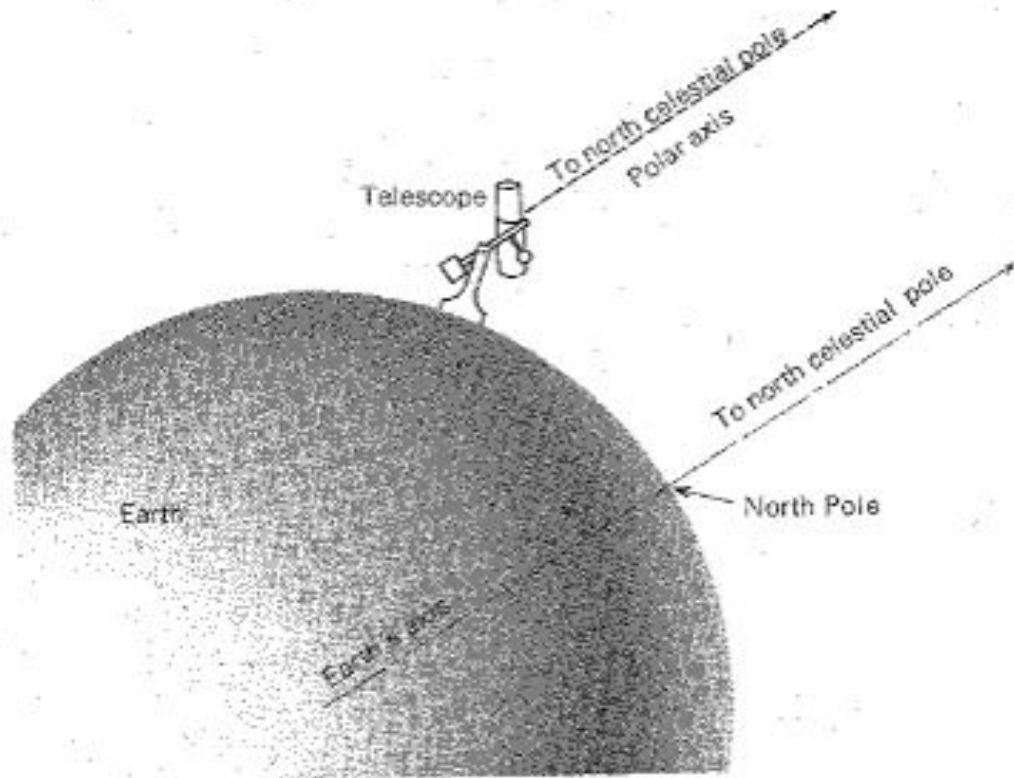
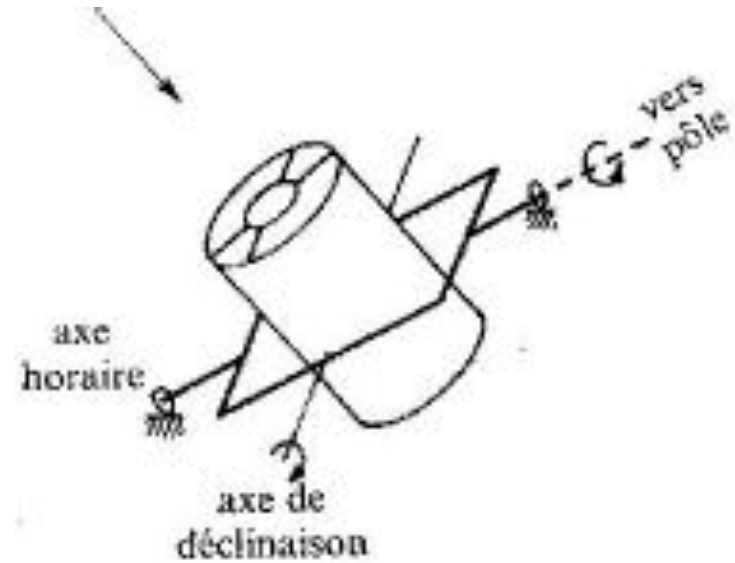
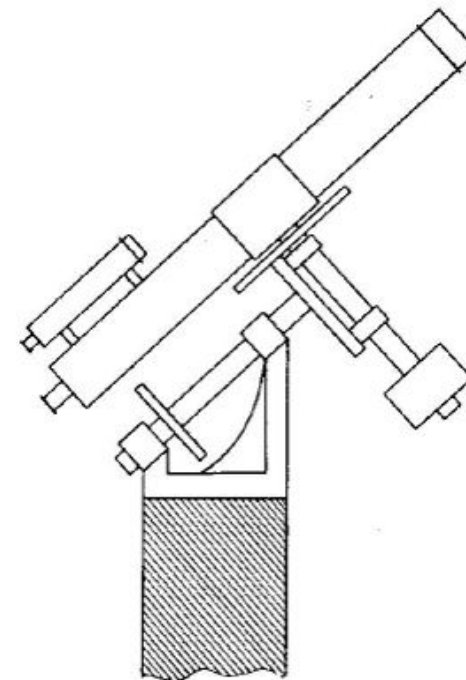


FIGURE 12.14 Equatorial mount.

(a)



(b)

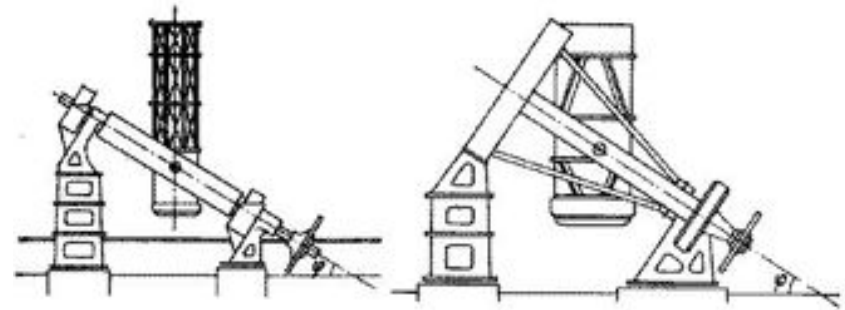


(c)

# 9 Fourier Optical Elements

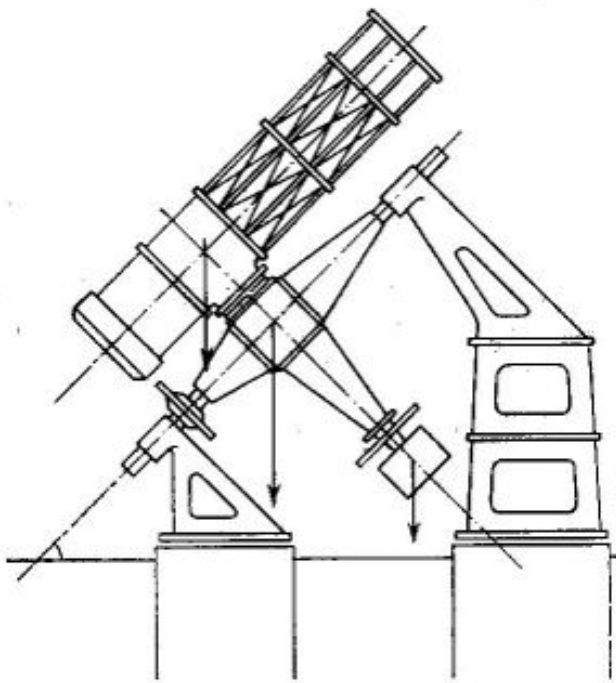
## 9.3 Telescope applications

### 9.3.1 Optical telescopes

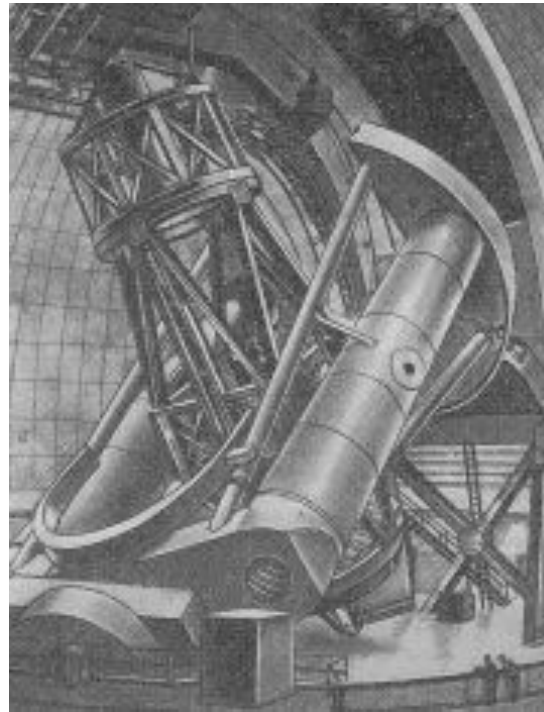


(b)

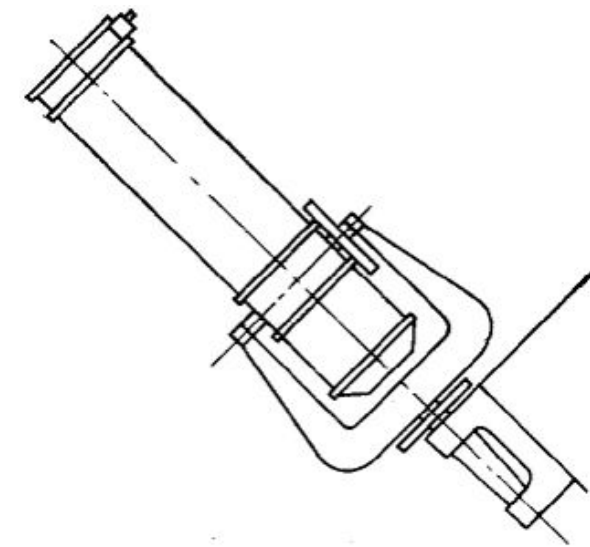
(c)



(a)



(d)

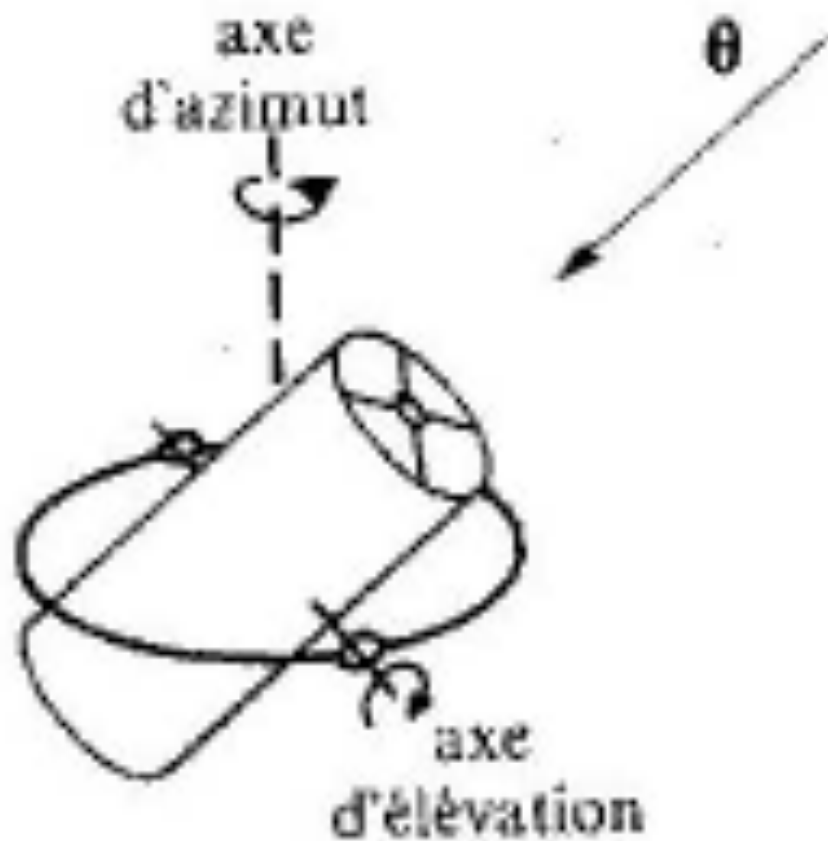


(e)

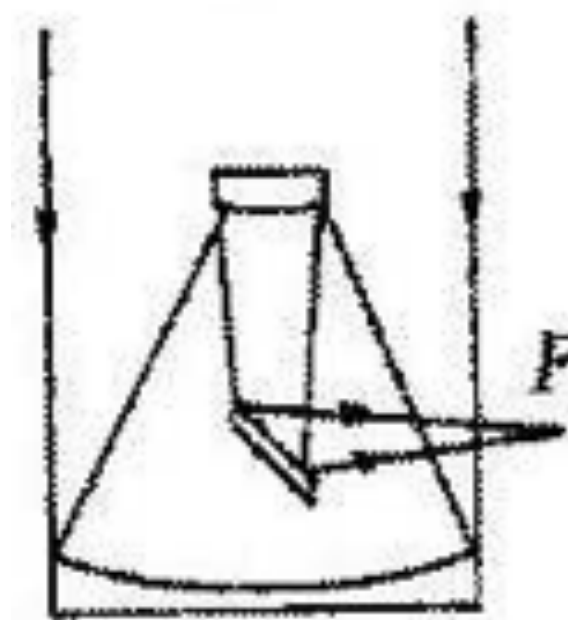
# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.1 Optical telescopes



(a)



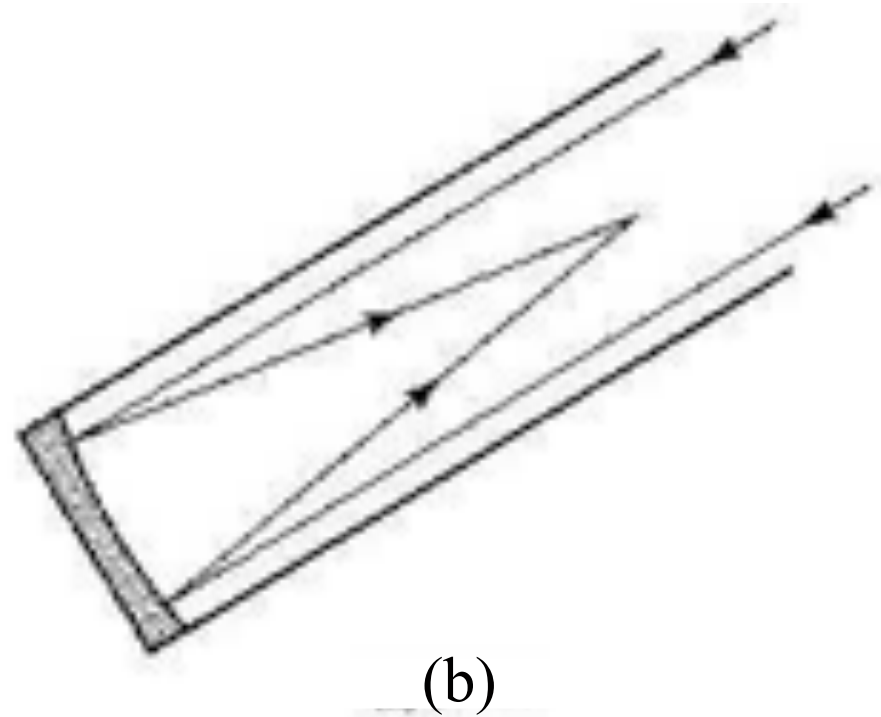
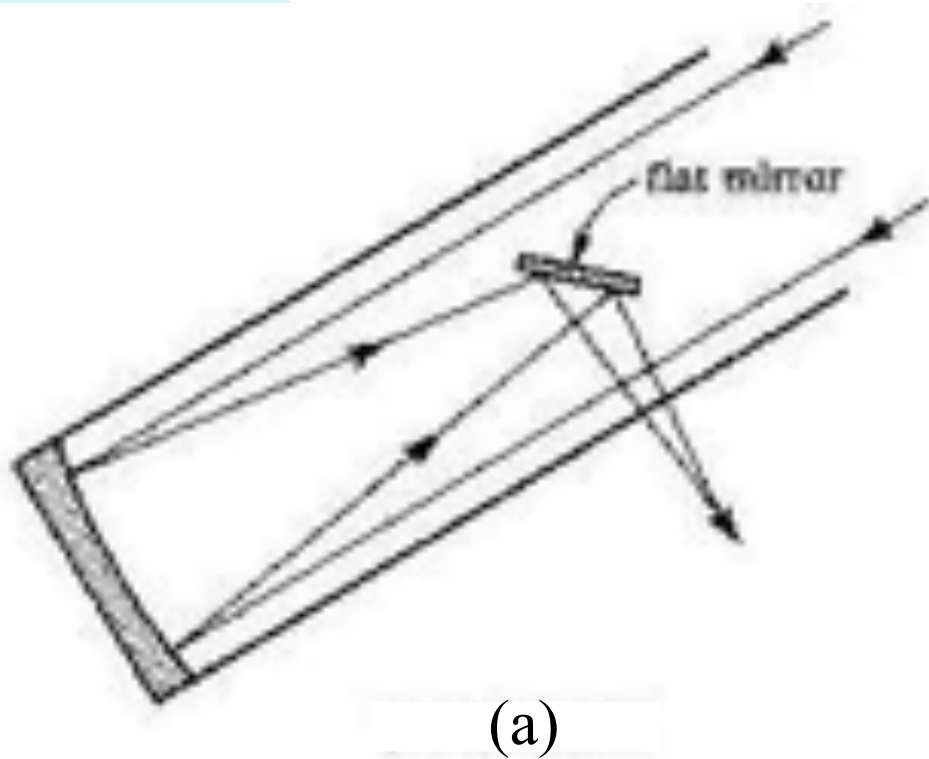
Nasmyth

(b)

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.1 Optical telescopes



Newton focus (a) and Primary focus (b) of optical telescopes

# 9 Fourier Optical Elements

## 9.3 Telescope applications

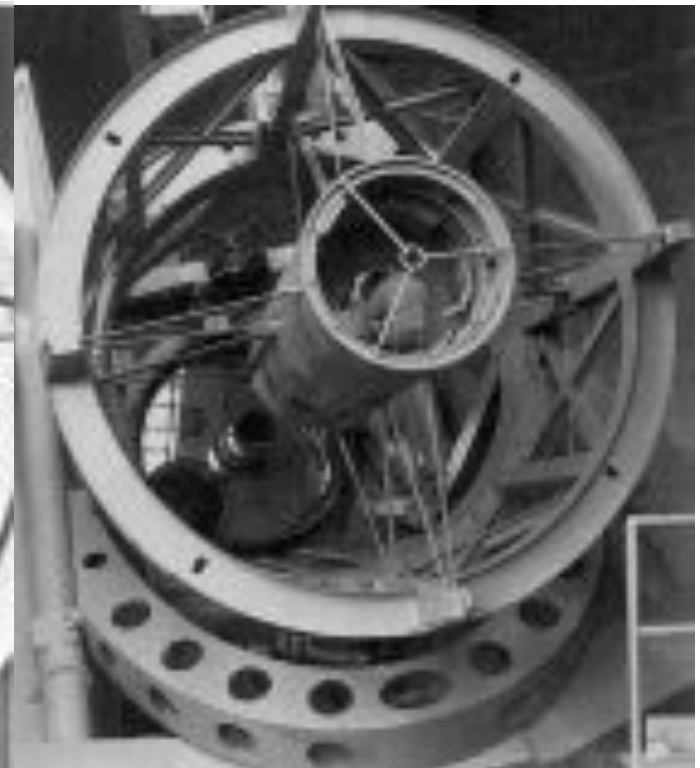
### 9.3.1 Optical telescopes



(a)



(b)



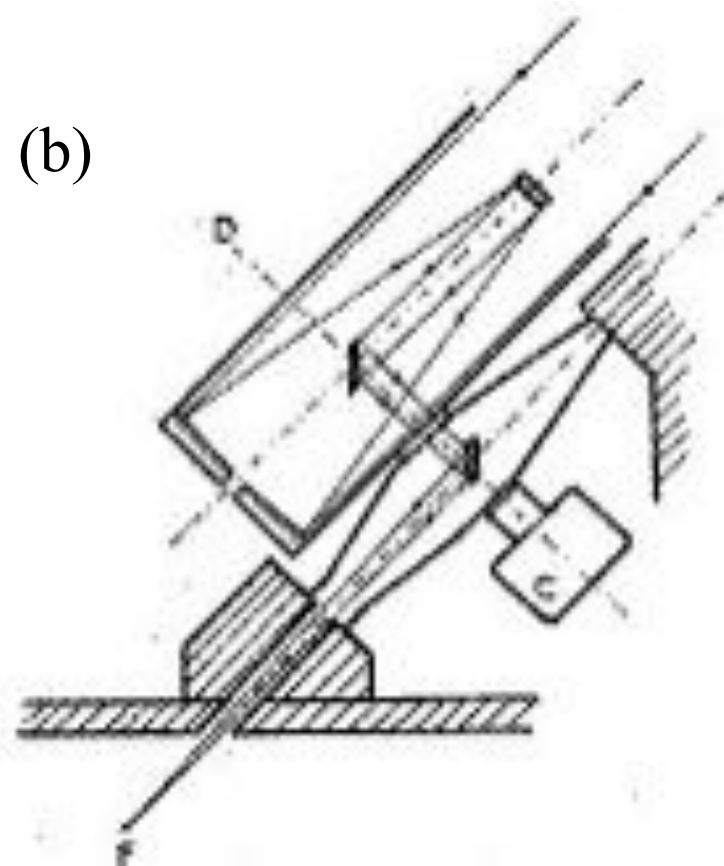
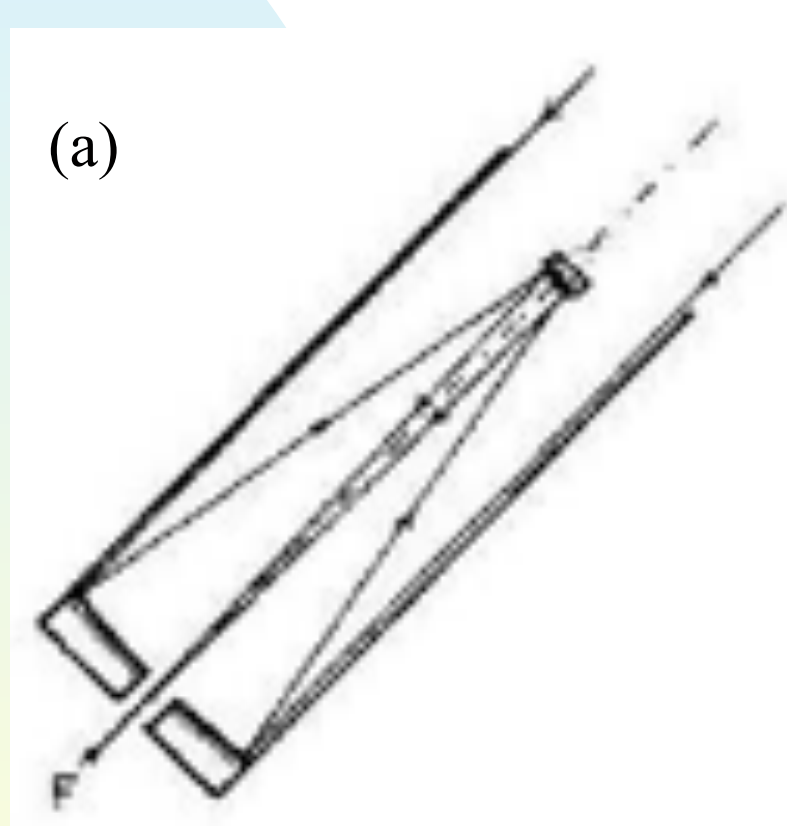
(c)

Observers in the Prime focus cage

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.1 Optical telescopes



(a) Cassegrain, Ritchey-Chrétien or Strand foci of an optical telescope and  
(b) Coudé focus

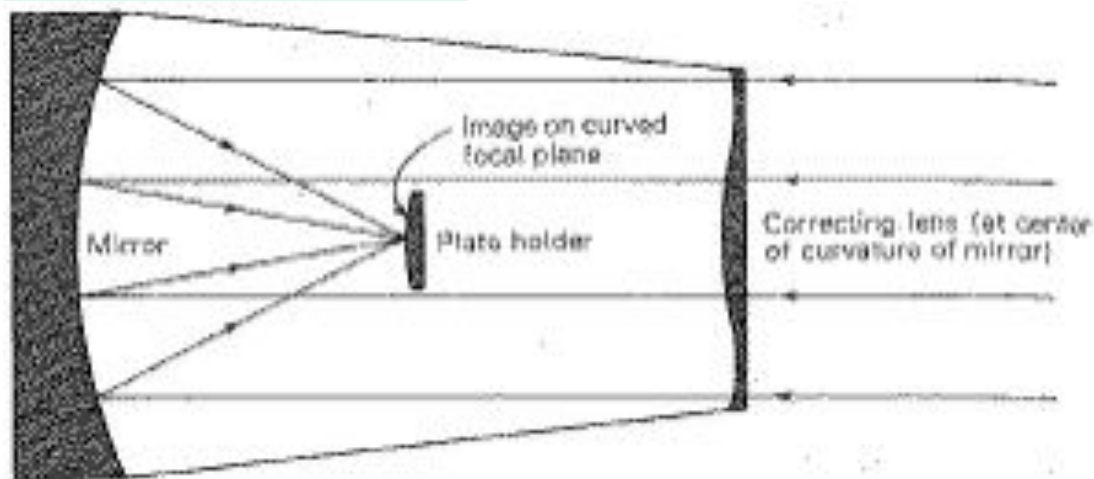
# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.1 Optical telescopes

(b)

(a)



- (a) Optical components of a Schmidt telescope and
- (b) big Schmidt telescope of Mont Palomar

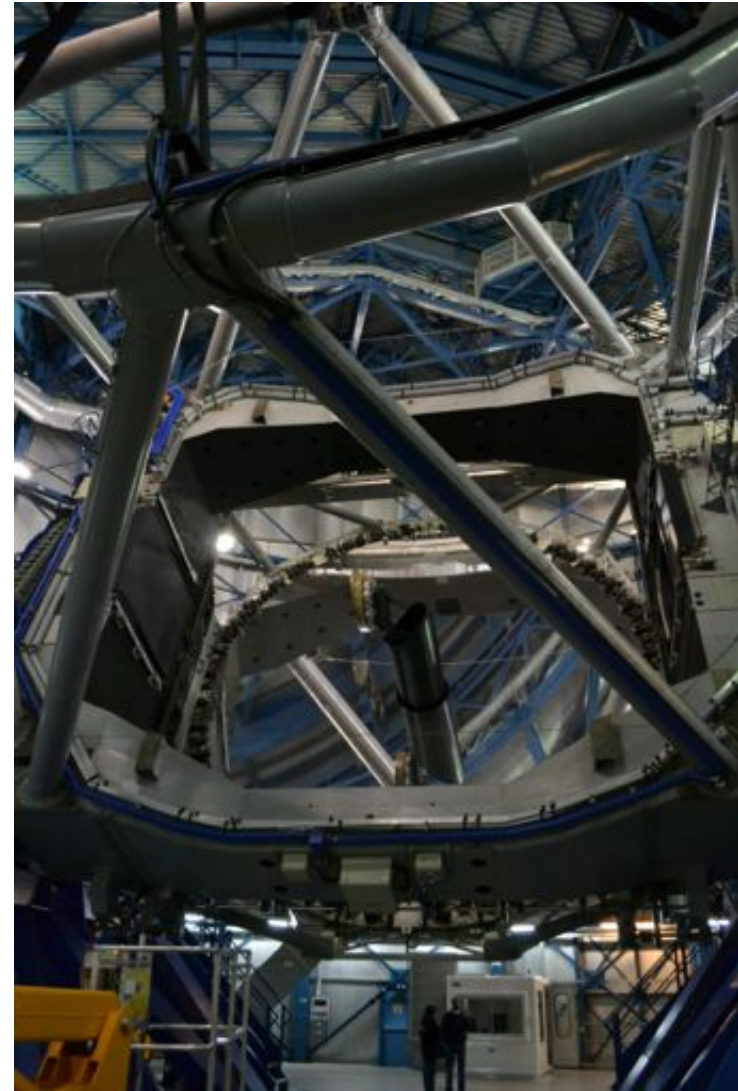
# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.1 Optical telescopes



ESO VLT (Paranal, Chile)



See the URL:

<http://www.eso.org>



# 9 Fourier Optical Elements

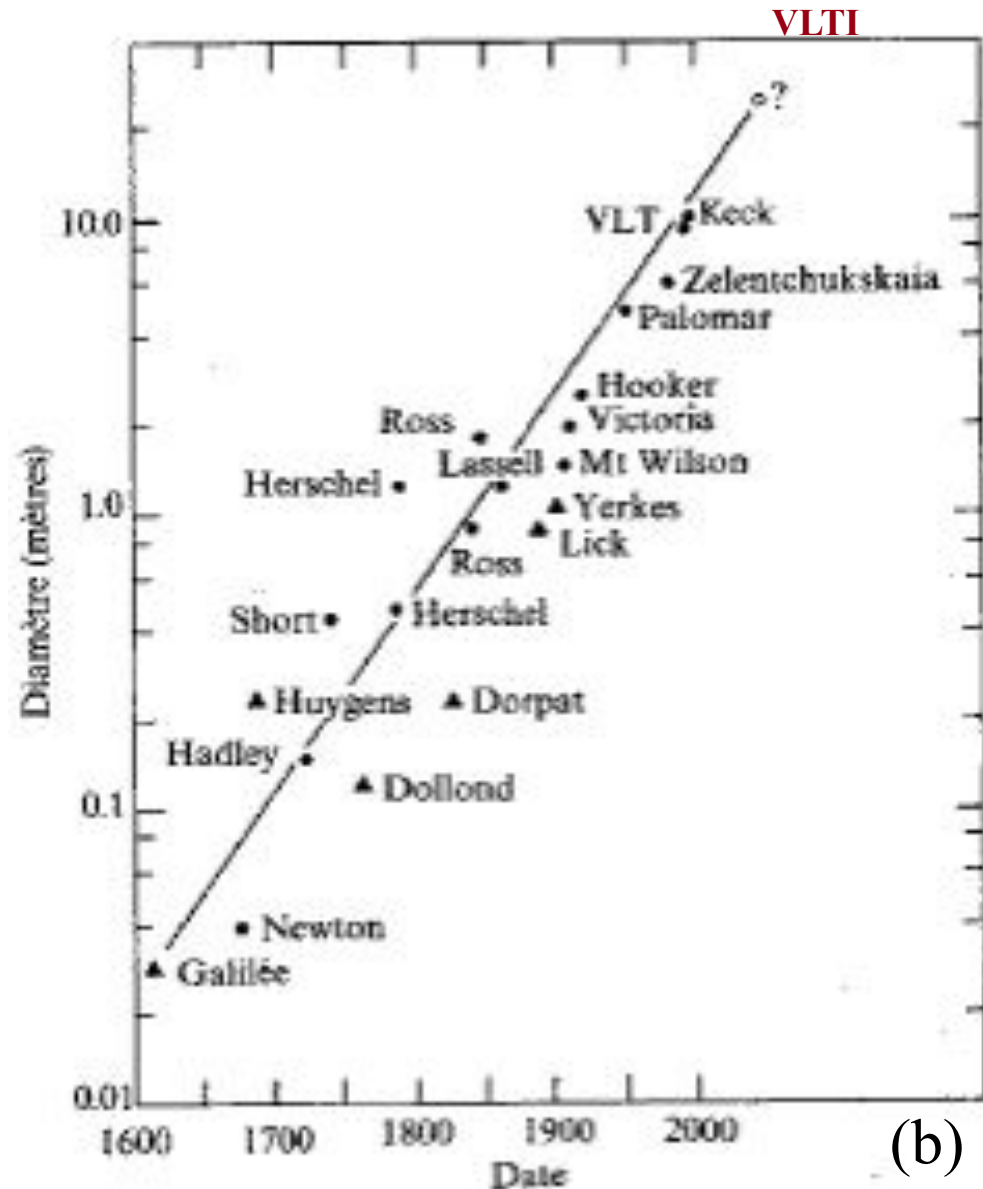
## 9.3 Telescope applications

### 9.3.1 Optical telescopes

<http://www.stsci.edu/>



(a)



(b)

# 9 Fourier Optical Elements

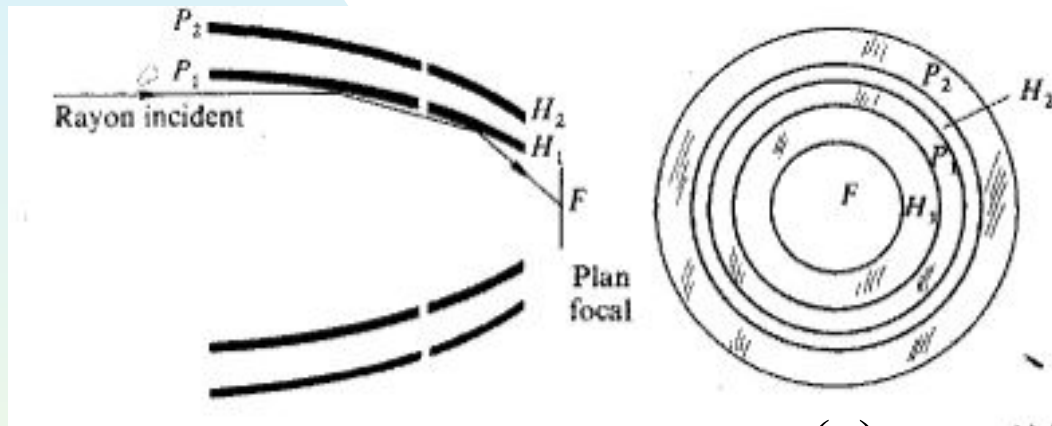
## 9.3 Telescope applications

- **9.3.1 Optical telescopes**
- **9.3.2 Coupled telescopes**
- **9.3.3 X-ray telescopes**
- **9.3.4 Radio-telescopes and radio-interferometers**

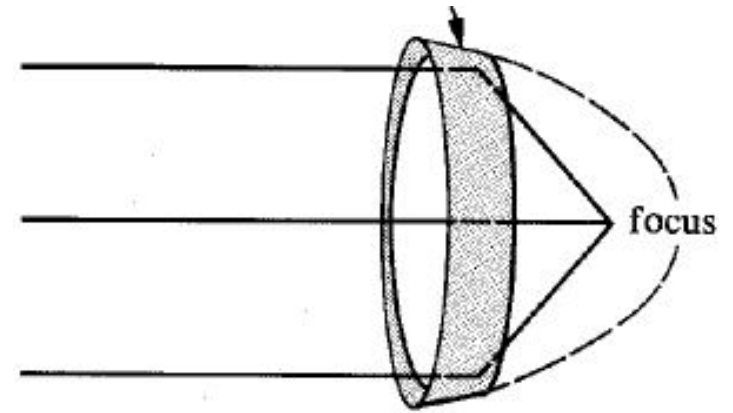
# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.3 X-ray telescopes



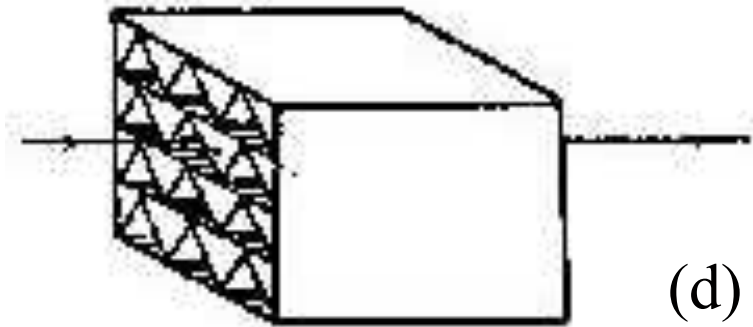
(a)



(b)



(c)



(d)

(a) X-ray telescope with double grazing reflection (P: paraboloid; H: hyperboloid); (b) simple paraboloid; (c) X-ray mirror of the Einstein satellite and (d) Cellular collimator.

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.3 X-ray telescopes



(a)

(b)



(c)

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.3 X-ray telescopes



(a)



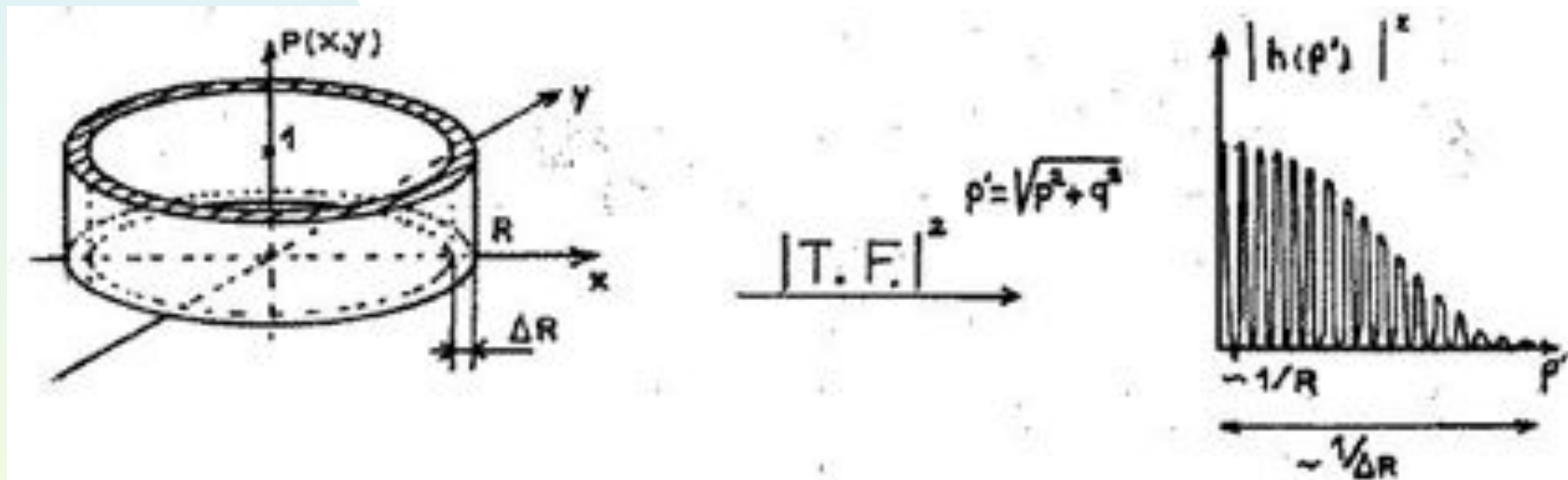
(b)

See the URLs: <http://sci.esa.int/xmm/> and <http://xmm.vilspa.esa.es/>

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.3 X-ray telescopes

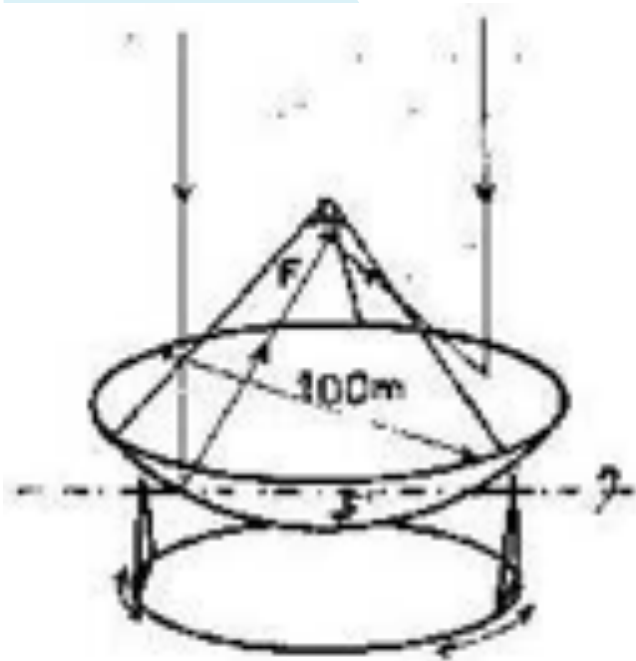


Entrance pupil  $P(x,y)$  and response function  $|h(\rho')|^2$  for an X-ray telescope (grazing light ray incidence).

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers



(a)



(b)



(c)

(a) Effelsberg radio-telescope (F: primary focus; F': Gregory focus).

(b) and (c) Photographs

# 9 Fourier Optical Elements

9.3 Telescope applications

**9.3.4 Radio-telescopes and radio-interferometers**



The Green Bank 300ft (West Virginia) ... before and after 15/11/1988!



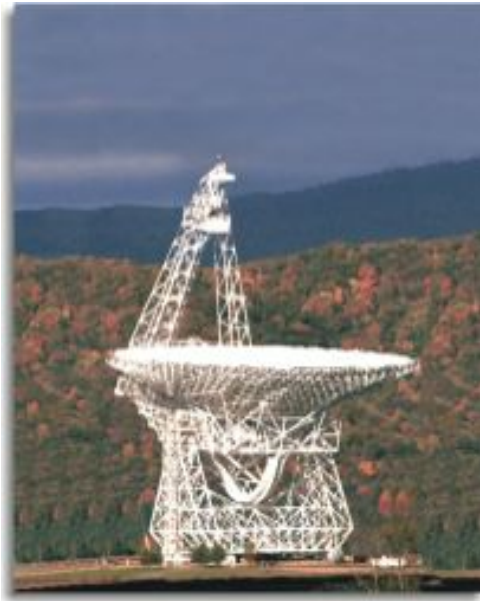
# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers



(a)



(b)



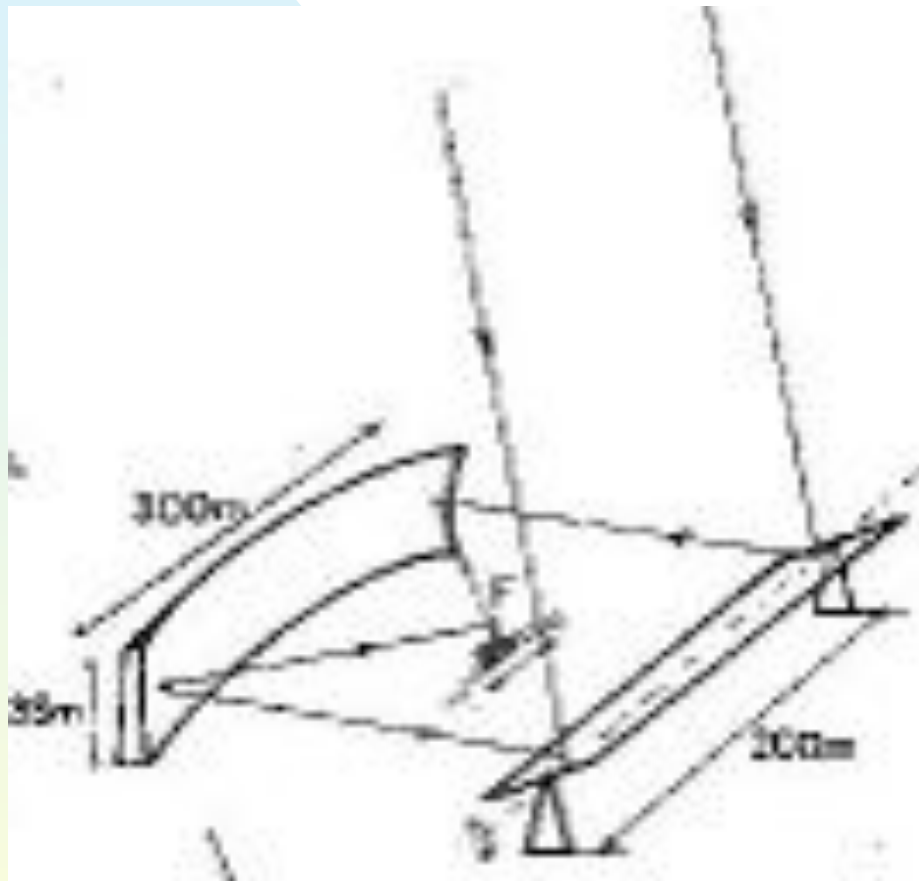
(c)

(a), (b) and (c) : Photographs of the new Green Bank radio-telescope

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers



(a)



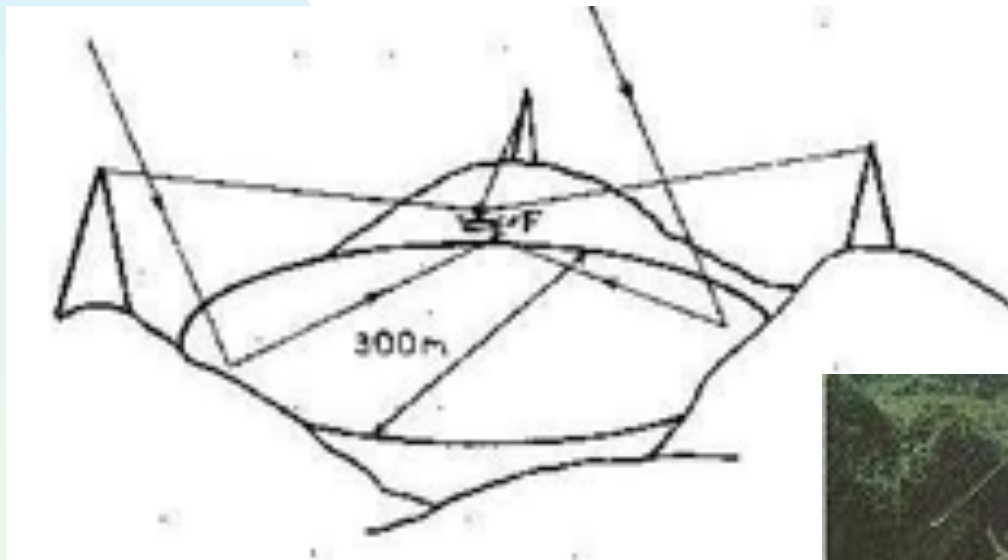
(b)

(a) Nançay radio-telescope

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers



Arecibo radio-telescope



# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers

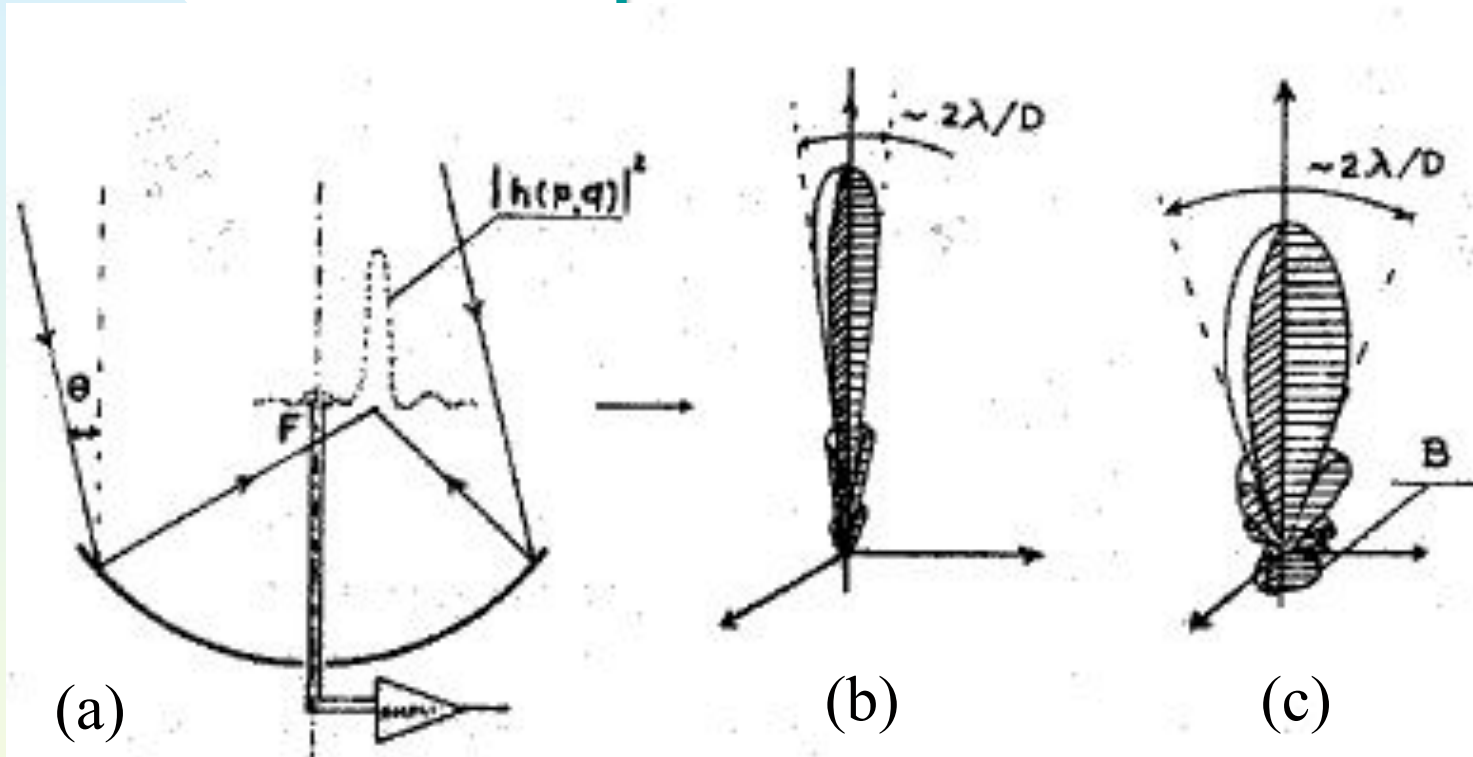
The 500-metre aperture spherical telescope (FAST) in China's Pingtang county.



# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers

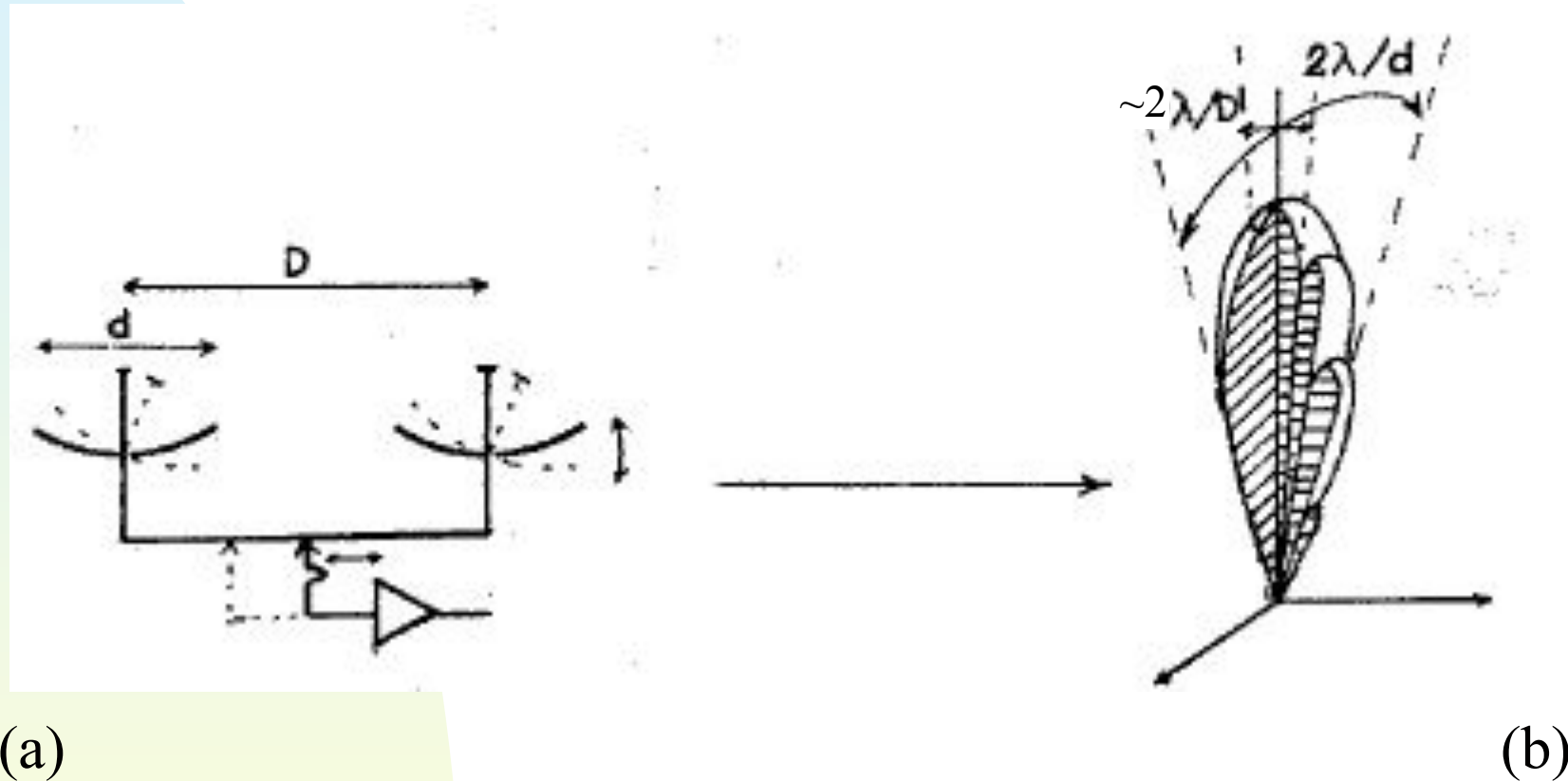


Antenna diagram of a radio-telescope. (a) Excitation of the antenna for a point-like object inclined by an angle  $\theta$  with respect to the central axis; (b) sensitivity of the mirror + antenna in polar coordinates (or graph of the response function in polar coordinates assuming that the antenna is point-like); (c) real diagram corresponding to  $\lambda / D \sim 1 / 10$  and showing the back-side lobe B.

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers



Radio-interferometer: (a) Connection diagram; (b) Antenna diagram (graph in polar coordinates of the response function).

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers

$$e(p) = 2d^2 \left( \frac{\sin(\pi pd)}{\pi pd} \right)^2 \left[ O(p) * \cos^2(\pi pD) \right], \quad (9.3.10)$$

$$e(p) = 2d^2 \left( \frac{\sin(\pi pd)}{\pi pd} \right)^2 \left[ \frac{1}{2} \int_R O(p) dp + \frac{1}{2} O(p) * \cos(2\pi pD) \right], \quad (9.3.11)$$

$$e(p) = A \left[ B + \frac{1}{2} \operatorname{Re} \left( O(p) * \exp(2i\pi pD) \right) \right], \quad (9.3.12)$$

$$A = 2d^2 \left( \frac{\sin(\pi pd)}{\pi pd} \right)^2 \quad \text{and} \quad B = \frac{1}{2} \int_R O(p) dp, \quad (9.3.13)$$

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers

$$e(p) = A \left[ B + \frac{1}{2} \operatorname{Re} \left( \int_R O(r) \exp(2i\pi(p-r)D) dr \right) \right], \quad (9.3.14)$$

$$e(p) = A \left[ B + \frac{1}{2} \cos(2\pi pD) \operatorname{TF}_-(O(r))(D) \right], \quad (9.3.15)$$

$$\gamma(D) = (e_{\max} - e_{\min}) / (e_{\max} + e_{\min}), \quad (9.3.16)$$

$$\gamma(D) = \operatorname{TF}_-(O(r))(D) / (2B) = \operatorname{TF}_-(O(r))(D) / \int O(p) dp. \quad (9.3.17)$$



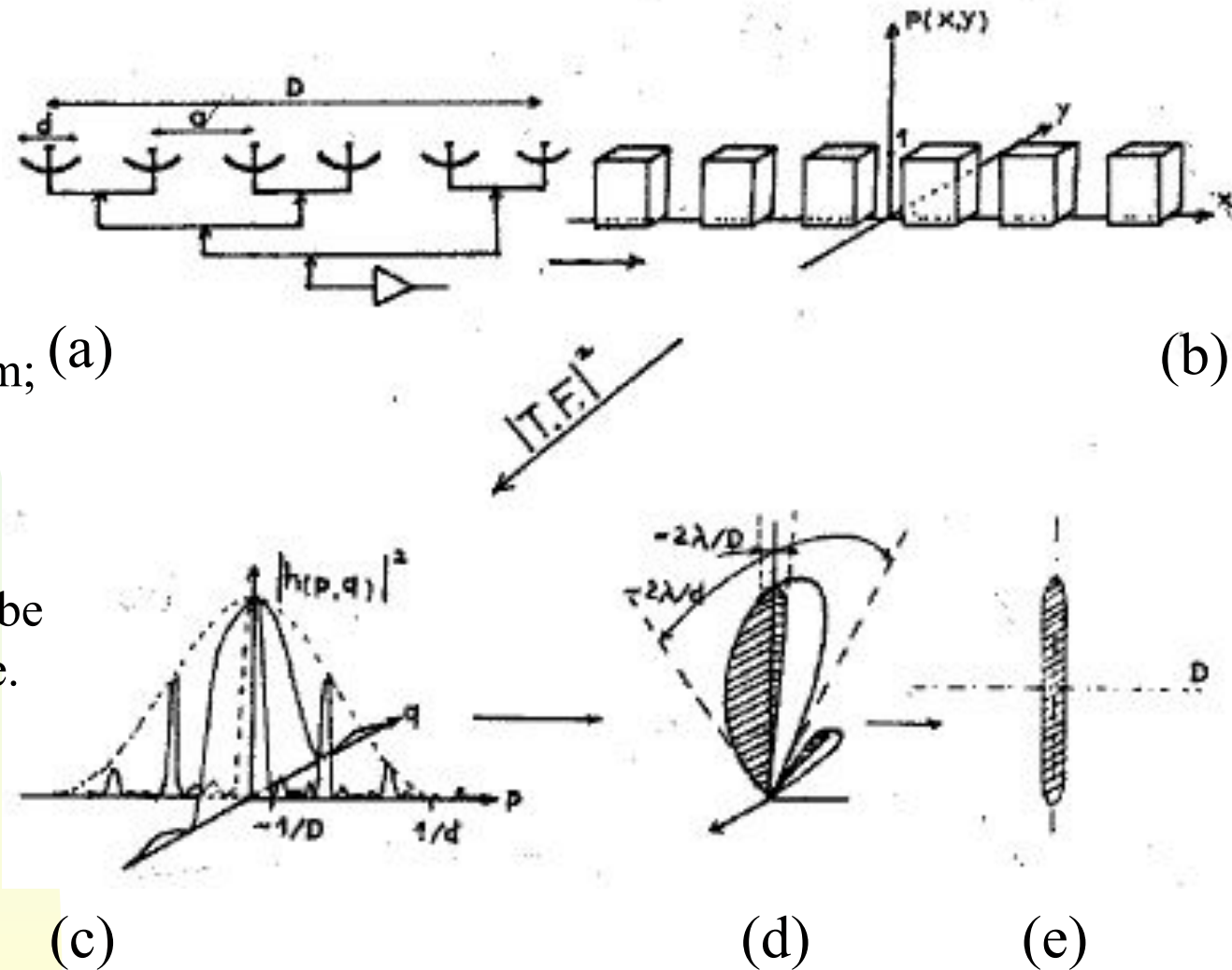
# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers

Radio-telescope  
interferometer

- (a) Connection diagram;
- (b) Entrance pupil;
- (c) Response function;
- (d) Antenna diagram;
- (e) Trace of the main lobe over the celestial sphere.



# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers

$$P_{r,0}(x, y) = \Pi \left[ \frac{y}{d} \right] \sum_{n=0}^{N-1} \Pi \left[ \frac{x + (N-1)\frac{a}{2} - na}{d} \right], \quad (9.3.18)$$

$$h_{r,0}(p, q) = \int_{-d/2}^{d/2} \exp(-i2\pi qy) dy \sum_{n=0}^{N-1} \int_{\frac{-d}{2} - (N-1)\frac{a}{2} + na}^{\frac{d}{2} - (N-1)\frac{a}{2} + na} \exp(-i2\pi px) dx, \quad (9.3.19)$$

$$h_{r,0}(p, q) = d \frac{\sin(\pi qd)}{\pi qd} \sum_{n=0}^{N-1} \int_{\frac{-d}{2} - (N-1)\frac{a}{2} + na}^{\frac{d}{2} - (N-1)\frac{a}{2} + na} \exp(-i2\pi px) dx, \quad (9.3.20)$$

$$h_{r,0}(p, q) = d \frac{\sin(\pi qd)}{\pi qd} \sum_{n=0}^{N-1} \frac{\exp(i\pi p(-d + (N-1)a - 2na)) - \exp(i\pi p(d + (N-1)a - 2na))}{-2i\pi p}, \quad (9.3.21)$$

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers

$$h_{r,0}(p, q) = d^2 \left( \frac{\sin(\pi qd)}{\pi qd} \right) \left( \frac{\sin(\pi pd)}{\pi pd} \right) \exp(i\pi pa(N-1)) \sum_{n=0}^{N-1} \exp(-2i\pi pan) \quad (9.3.22)$$

$$x = i\pi a p \text{ and } r = \exp(-2x), \quad (9.3.23)$$

$$h_{r,0}(p, q) = d^2 \left( \frac{\sin(\pi qd)}{\pi qd} \right) \left( \frac{\sin(\pi pd)}{\pi pd} \right) \exp(x(N-1)) \frac{1 - \exp(-2xN)}{1 - \exp(-2x)}, \quad (9.3.24)$$

$$h_{r,0}(p, q) = d^2 \left( \frac{\sin(\pi qd)}{\pi qd} \right) \left( \frac{\sin(\pi pd)}{\pi pd} \right) \frac{\exp(xN) - \exp(-xN)}{\exp(x) - \exp(-x)}, \quad (9.3.25)$$

$$h_{r,0}(p, q) = d^2 \left( \frac{\sin(\pi qd)}{\pi qd} \right) \left( \frac{\sin(\pi pd)}{\pi pd} \right) \left( \frac{\sin(N\pi pa)}{\sin(\pi pa)} \right) \quad (9.3.26)$$

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers

(9.3.27)

$$|h_{r,0}(p,q)|^2 = (Nd^2)^2 \left( \frac{\sin(\pi qd)}{\pi qd} \right)^2 \left( \frac{\sin(\pi rd)}{\pi rd} \right)^2 \left( \frac{\sin(N\pi ra)}{N\pi ra} \right)^2 \left( \frac{\pi ra}{\sin(\pi ra)} \right)^2.$$



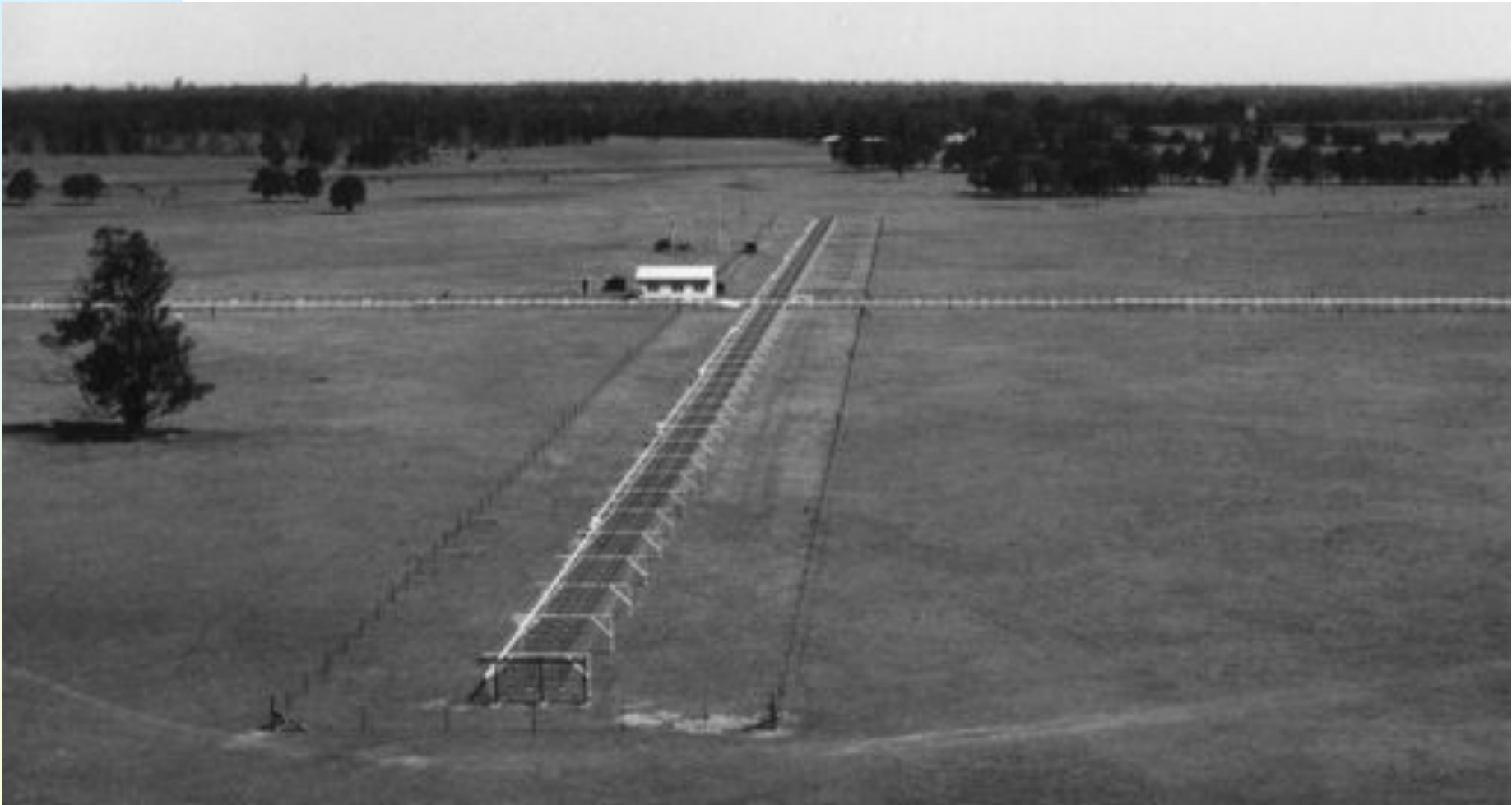
N apertures!

Response function  
of a single aperture

Central peak + intermediate  
peaks

# 9 Fourier Optical Elements

## 9.3 Telescope applications

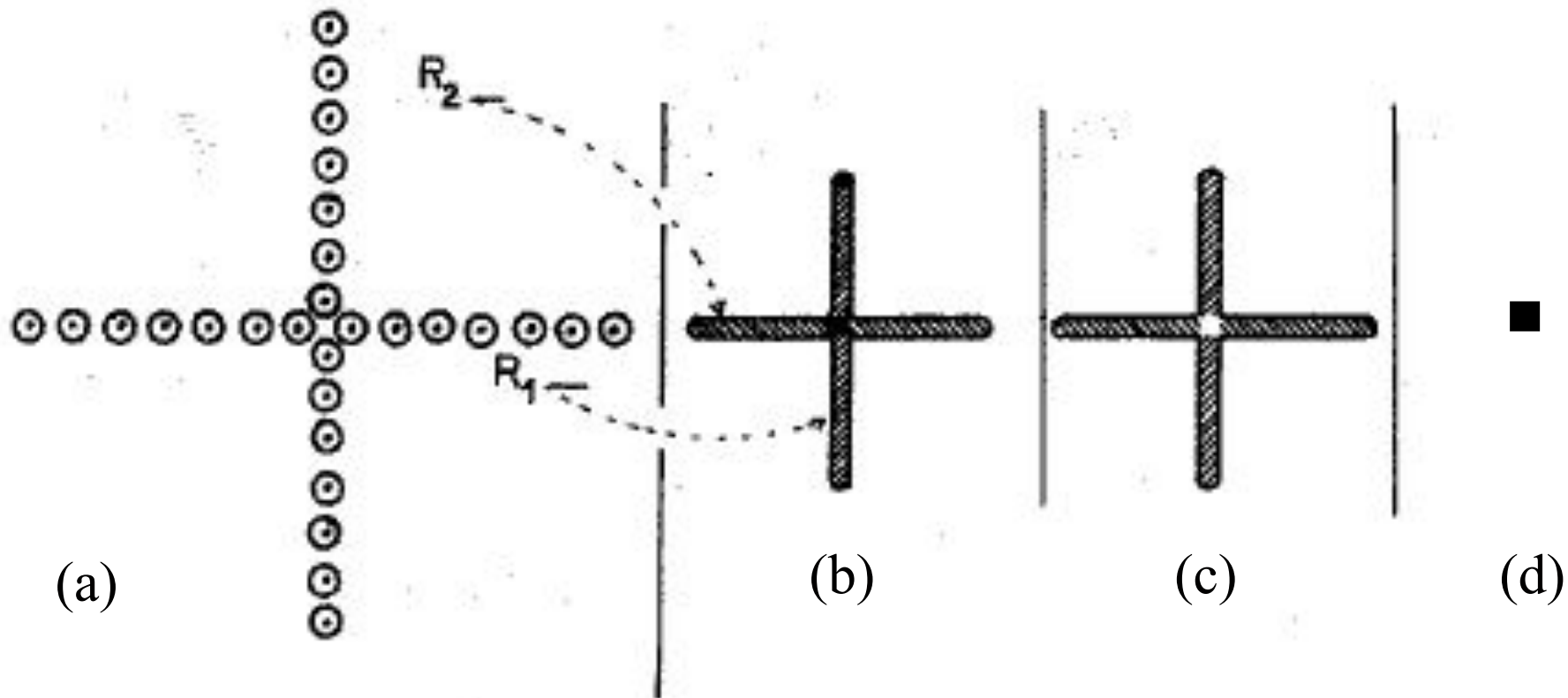


Photograph of the Mills Cross in Australia

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers



Mills cross. (a) Disposition of the elements; (b) and (c) Traces over the celestial sphere of the antenna diagram when the two branches  $R_1$  and  $R_2$  are connected in phase (b) and in phase opposition (c); (d) trace over the celestial sphere of the difference diagram

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers

$$P_{M,0}(x,y) = P_{r,0}(x,y) + P_{r,0}(y,x), \quad (9.3.28)$$

$$P'_{M,0}(x,y) = P_{r,0}(x,y) - P_{r,0}(y,x). \quad (9.3.29)$$

$$h_{M,0}(p,q) = h_{r,0}(p,q) + h_{r,0}(q,p), \quad (9.3.30)$$

$$h'_{M,0}(p,q) = h_{r,0}(p,q) - h_{r,0}(q,p). \quad (9.3.31)$$

# 9 Fourier Optical Elements

## 9.3 Telescope applications

### 9.3.4 Radio-telescopes and radio-interferometers

$$|h_c(p,q)|^2 = |h_{M,0}(p,q)|^2 - |h'_{M,0}(p,q)|^2. \quad (9.3.32)$$

$$|h_c(p,q)|^2 = 2[h_{r,0}(p,q) h_{r,0}^*(q,p) + h_{r,0}^*(p,q) h_{r,0}(q,p)], \quad (9.3.33)$$

$$|h_c(p,q)|^2 = 4 \operatorname{Re} [h_{r,0}(p,q) h_{r,0}^*(q,p)]. \quad (9.3.34)$$

$$|h_c(p,q)|^2 = 4d^4 \left( \frac{\sin(\pi pd)}{\pi pd} \right)^2 \left( \frac{\sin(\pi qd)}{\pi qd} \right)^2 \underbrace{\frac{\sin(N\pi pa)}{\sin(\pi pa)} \frac{\sin(N\pi qa)}{\sin(\pi qa)}}_{\text{Interference terms}}. \quad (9.3.35)$$



# 9 Fourier Optical Elements



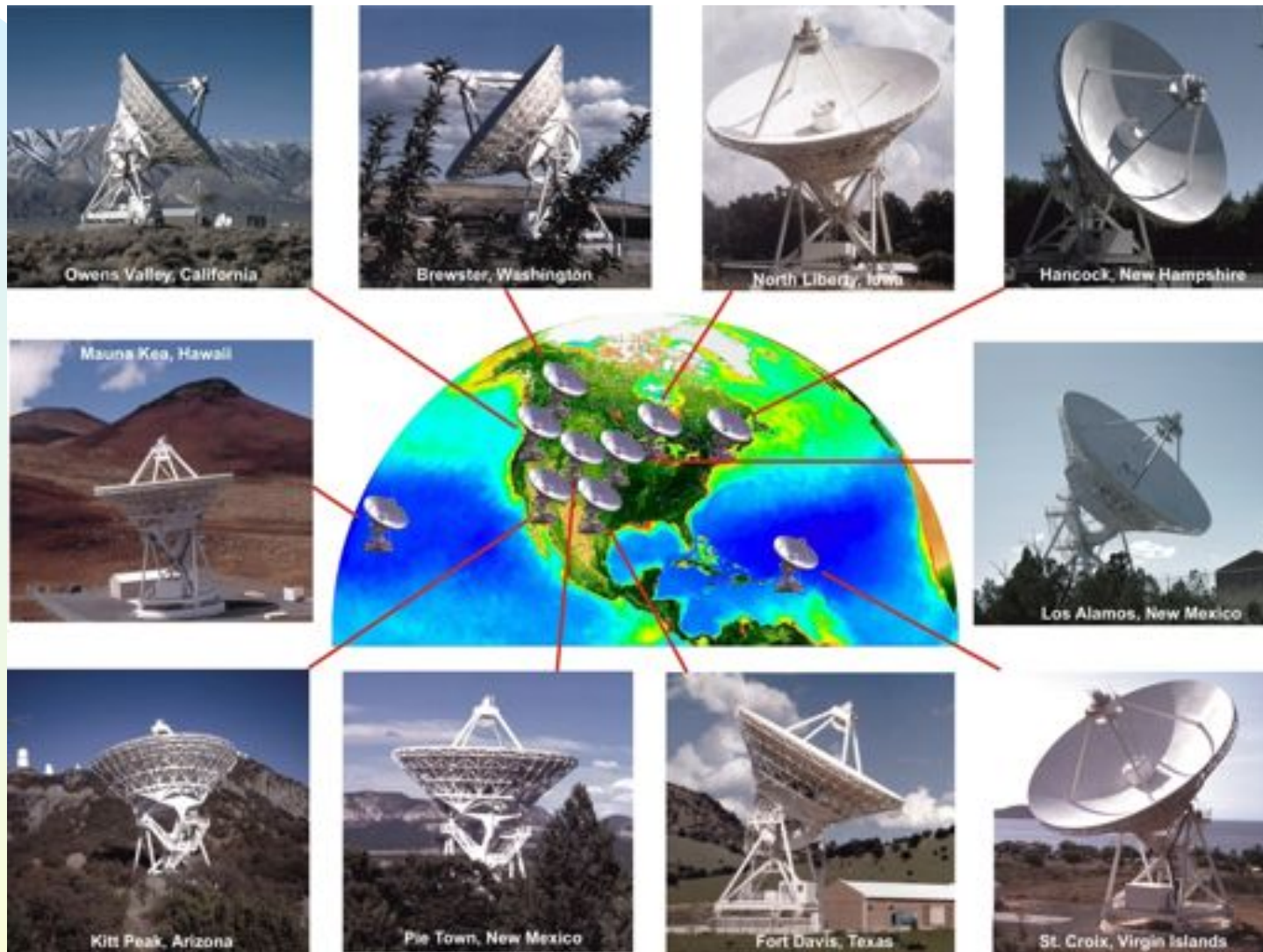
The Very Large Array near Socorro in New Mexico (USA)

# 9 Fourier Optical Elements



The Very Large Array near Socorro in New Mexico (USA)

# 9 Fourier Optical Elements



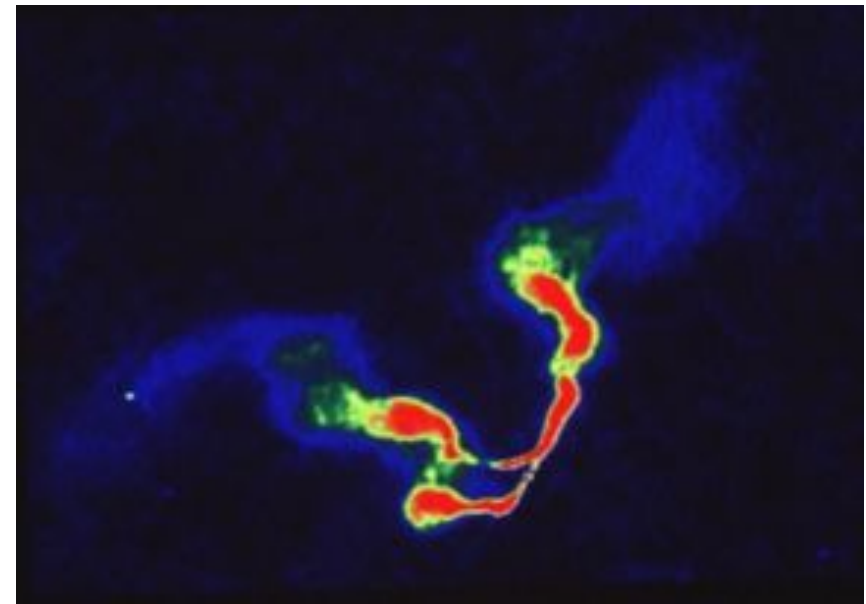
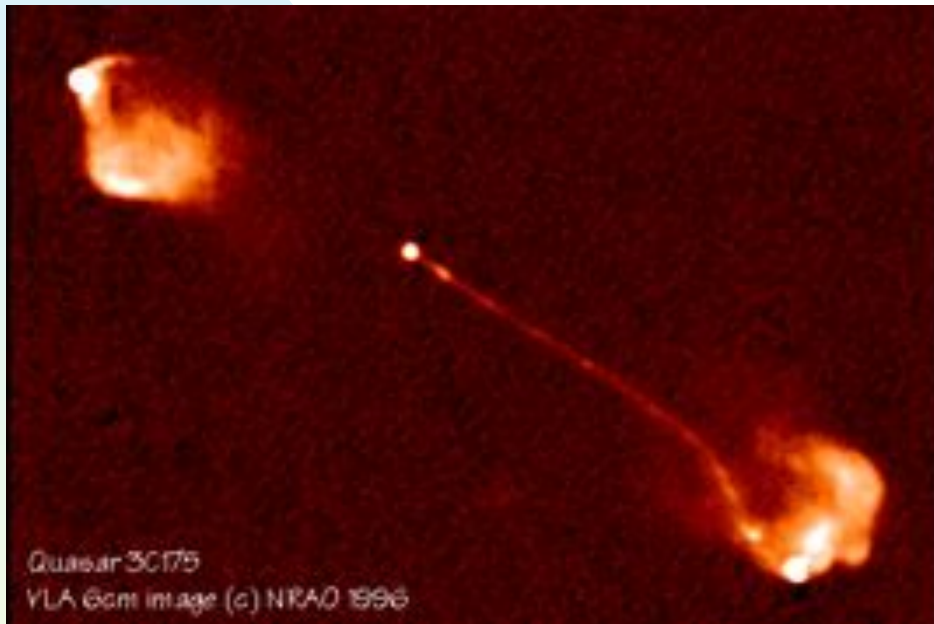
The Very Long Baseline Array (USA)

# 9 Fourier Optical Elements



The Very Long Baseline Array (USA)

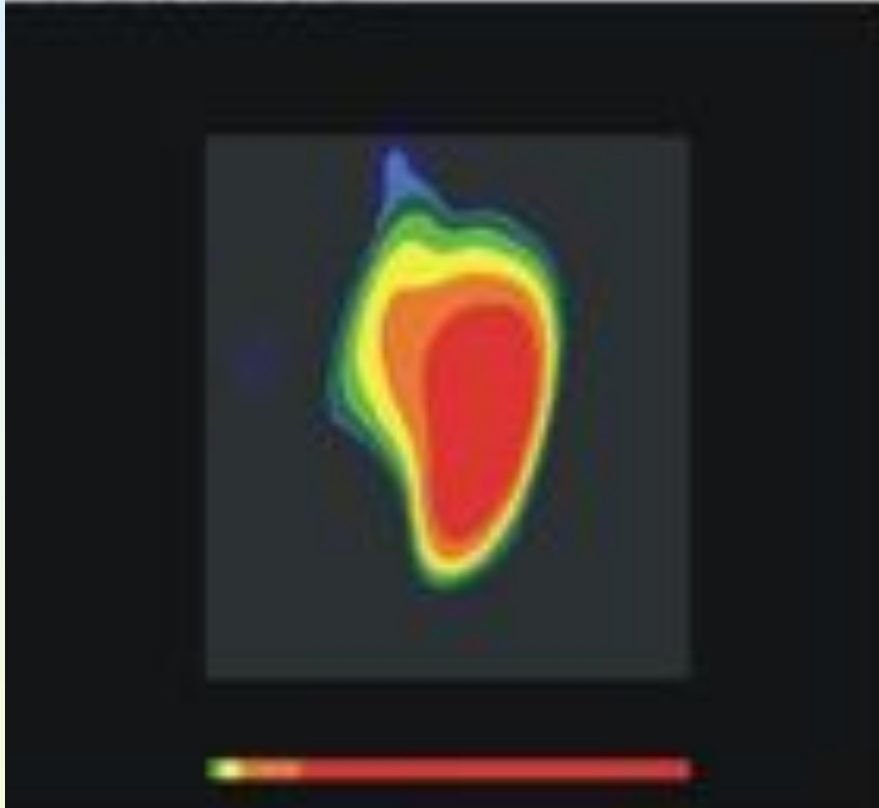
# 9 Fourier Optical Elements



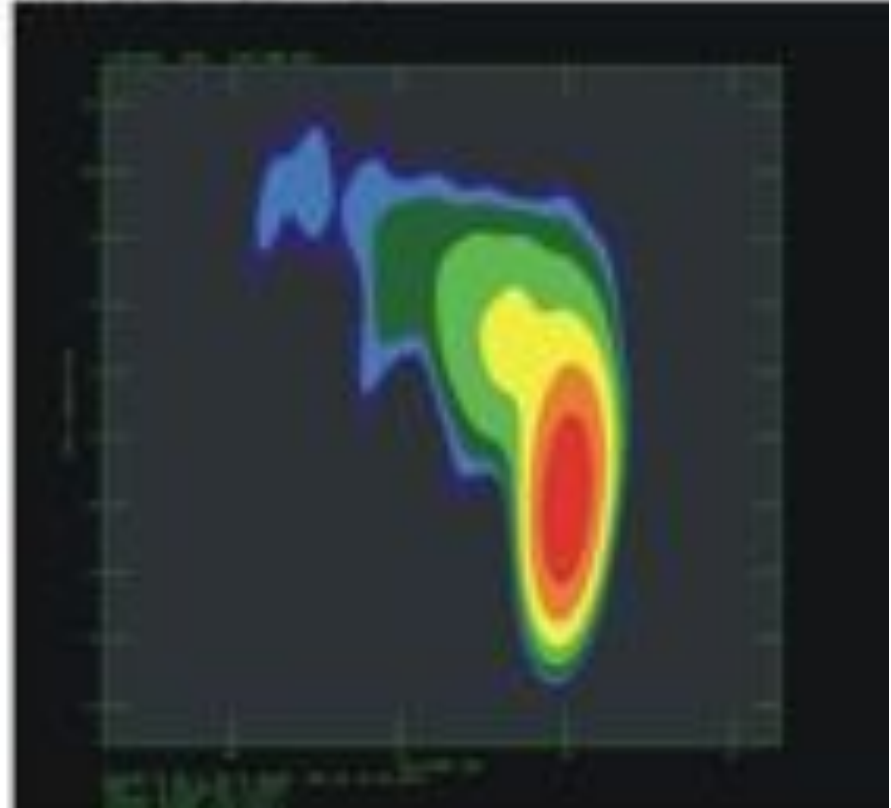
Quasar and AGN (Very Large Array, USA)

# 9 Fourier Optical Elements

1156+295, VLBA ONLY



1156+295, HALCA+VLBA



Quasar and AGN (Very Long Baseline Array, USA)

# 9 Fourier Optical Elements



The LOFAR 'superterp'. View of the heart of the radio-interferometer located near Exloo, Holland (1,3 - 30m, 20 000 antenna,  $B \approx 1000$  km,  $300\,000$  m<sup>2</sup>) .

# 9 Fourier Optical Elements



The 'SKA' (Square Kilometer Array) project: phased radio interferometer (Australia / South Africa, Base  $\approx 3\,000$  km,  $1\,000\,000$  m<sup>2</sup>, 2024).



# 9 Fourier Optical Elements



The Nançay  
radio-helio-  
graphs (France)



See the URL: [http://www.obs-nancay.fr/html\\_an/a\\_rh.htm](http://www.obs-nancay.fr/html_an/a_rh.htm)

# 9 Fourier Optical Elements



View of North of Chile (space shuttle)

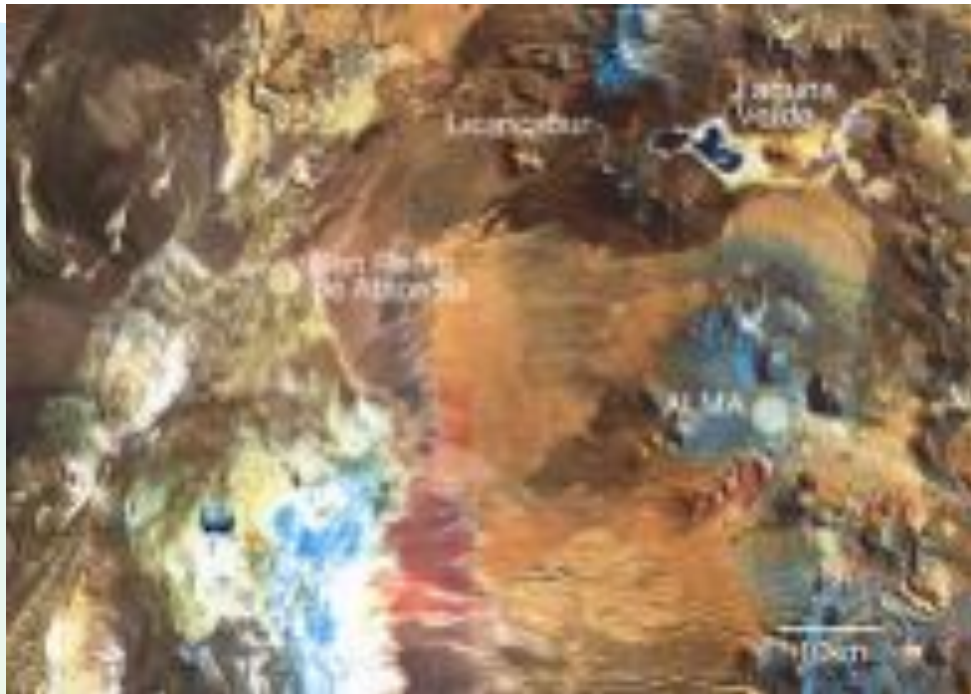


Geographic sites of the VLT and ALMA

Atacama Large Millimeter  
Array (Chile)

See the URL: <http://www.eso.org/projects/alma/>

# 9 Fourier Optical Elements



Aerial view of the ALMA site

Panoramic view of the ALMA site in Chajnantor



See the URL: <http://www.eso.org/projects/alma/>

# 9 Fourier Optical Elements

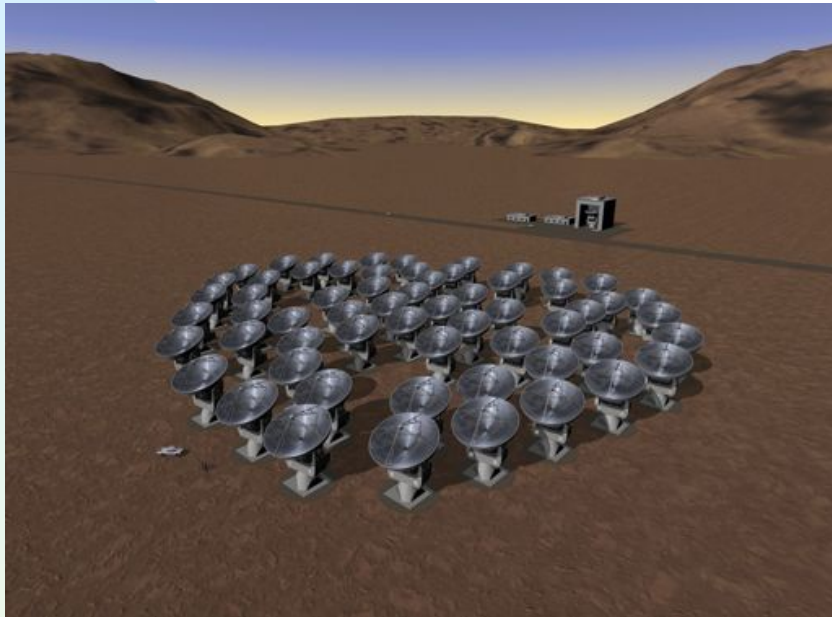


Atacama Large  
Millimeter  
Array (Chile)

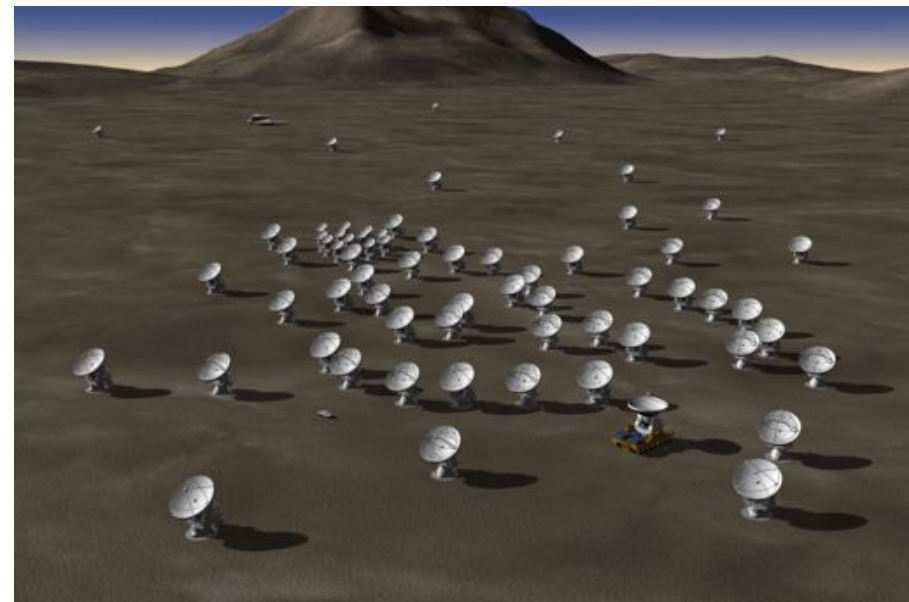
Futuristic model of ALMA

See the URL: <http://www.eso.org/projects/alma/>

# 9 Fourier Optical Elements



Atacama Large  
Millimeter  
Array (Chile)



Futuristic models of ALMA

See the URL: <http://www.eso.org/projects/alma/>

# 9 Fourier Optical Elements



Atacama Large  
Millimeter  
Array (Chile)

See the URL: <http://www.eso.org/projects/alma/>

# 9 Fourier Optical Elements



Atacama Large  
Millimeter  
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See the URL: <http://www.eso.org/projects/alma/>





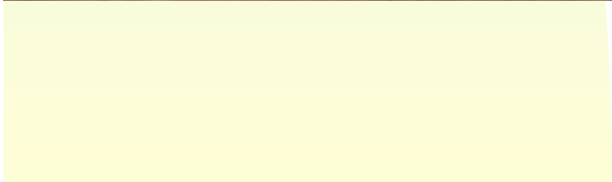




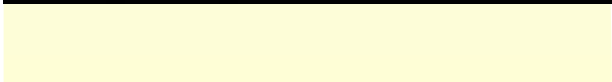






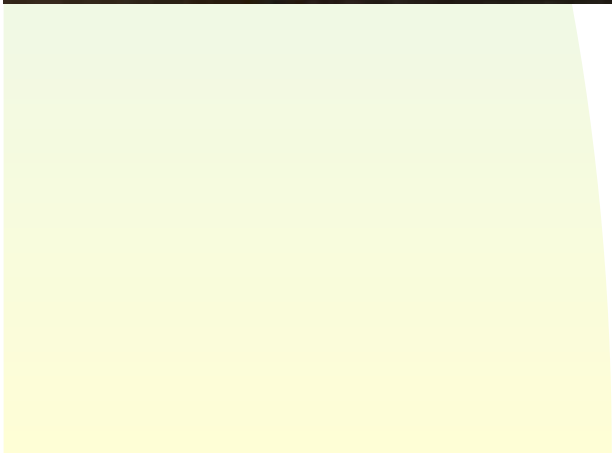








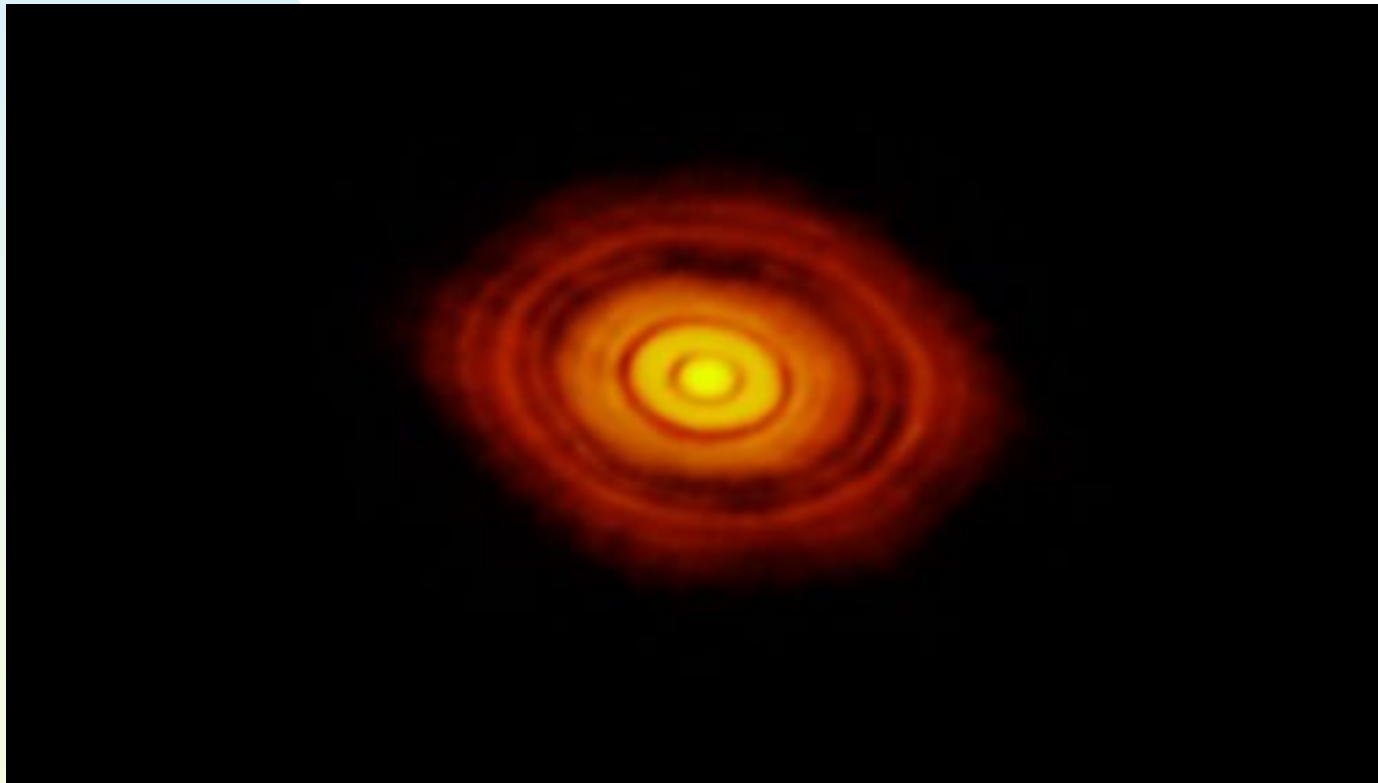








# 9 Fourier Optical Elements



Atacama Large  
Millimeter  
Array (Chile)

HL Tauri, 450  
light years from  
Earth, planetary  
disk made of gas  
and dust, spatial  
resolution is  
approximately  
5 AU

See the URL: <http://www.eso.org/projects/alma/>