



# Transport and interaction blockade of cold bosonic atoms in a triple-well potential

Peter Schlagheck\*, Francesc Malet, Jonas C. Cremon, and Stephanie M. Reimann

Division of Mathematical Physics, LTH, Lund University, Sweden

\*Département de Physique, Université de Liège, Belgium



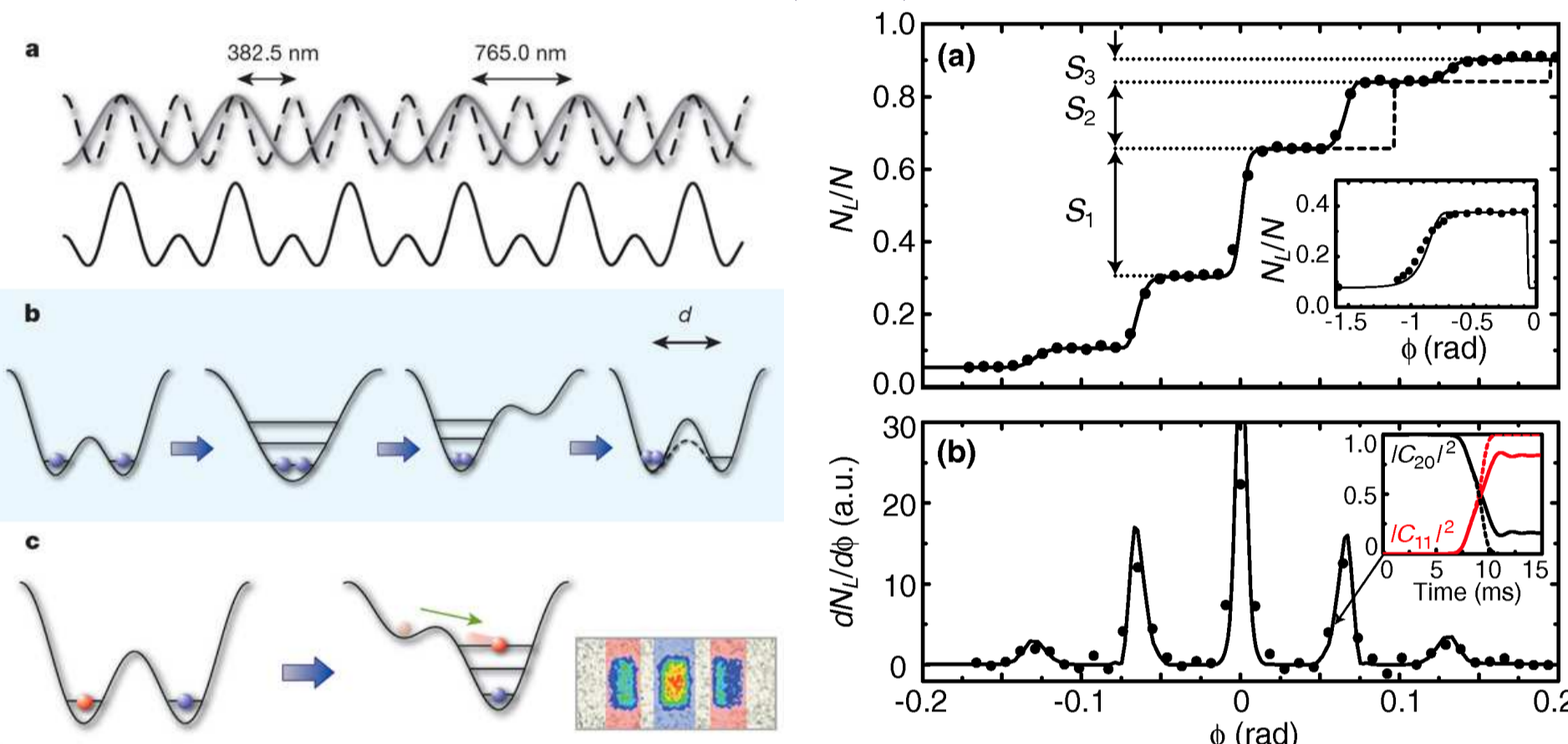
We investigate the transport properties of cold bosonic atoms in a triple-well potential that consists of two large outer wells, which act as microscopic source and drain reservoirs, and a small inner well, which represents a quantum-dot-like scattering region. Bias and gate “voltages” are introduced in order, respectively, to tilt the triple-well configuration and to shift the energetic level of the inner well with respect to the outer ones. By means of exact diagonalization considering a total number of 6 atoms in the triple-well potential, we find diamond-like structures for the occurrence of single-atom transport in the parameter space spanned by the bias and gate voltages, in close analogy with the Coulomb blockade in electronic quantum dots.

## Motivation

Interaction blockade experiments in double-well superlattices created by two optical lattices with the wavelengths  $\lambda_1 = 1530$  nm and  $\lambda_2 = 0.5\lambda_1 = 765$  nm

S. Fölling et al., Nature 448, 1029 (2007)

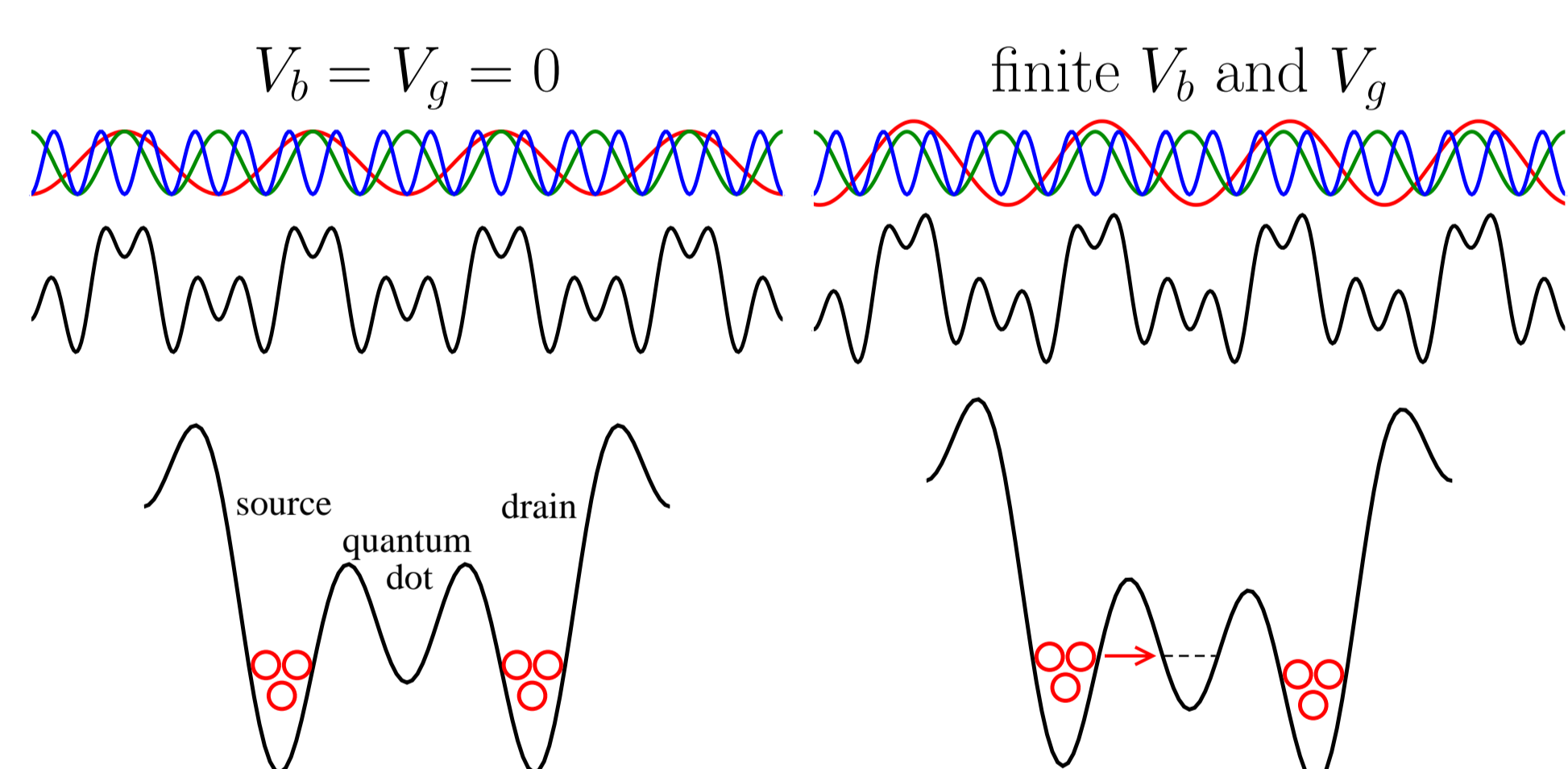
P. Cheinet et al., PRL 101, 090404 (2008)



## Triple-well lattice

→ add a third lattice with wavelength  $\lambda_3 = 0.5\lambda_2$   
Effective potential (for  $k \equiv 4\pi/\lambda_1$ ):

$$V(x) = V_0[-\cos(kx) + \cos(2kx) - \cos(4kx)] - V_g \cos(kx) - V_b \sin(kx)$$



$V_b$  tilts the triple-well potentials: → “bias voltage”  
 $V_g$  pulls down the central well: → “gate voltage”

→ analogy with Coulomb blockade for electrons:

- load the lattice at given gate voltage  $V_g$  and vanishing bias with a well-defined number of particles per triple-well site,
- ramp up the bias voltage until a given final value  $V_b$ ,
- measure the populations in the left, central, and right wells.

Specifically we consider

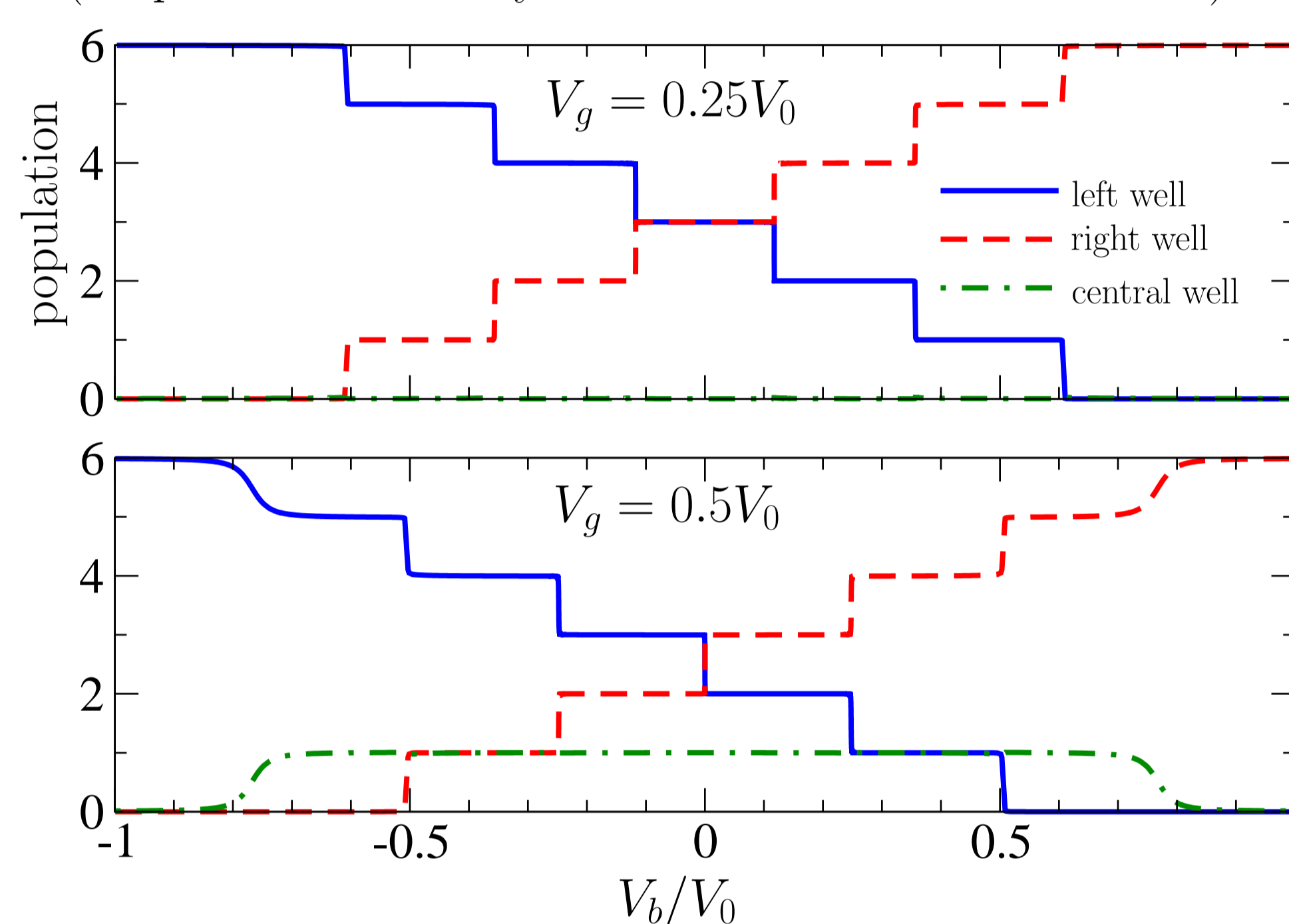
- $^{87}\text{Rb}$  atoms
- main periodicity  $2\pi/k = \lambda_2 = 765$  nm
- main lattice strength  $V_0 = 20\hbar^2 k^2/m$
- effective 1D interaction strength  $g = 4\hbar^2 k/m$

## Ground-state populations

Exact numerical diagonalization (based on the Lanczos algorithm) of the many-body Hamiltonian

$$\hat{H} = \int dx \hat{\psi}^\dagger(x) \left( -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} + V(x) \right) \hat{\psi}(x) + \frac{g}{2} \int dx \hat{\psi}^\dagger(x) \hat{\psi}^\dagger(x) \hat{\psi}(x) \hat{\psi}(x)$$

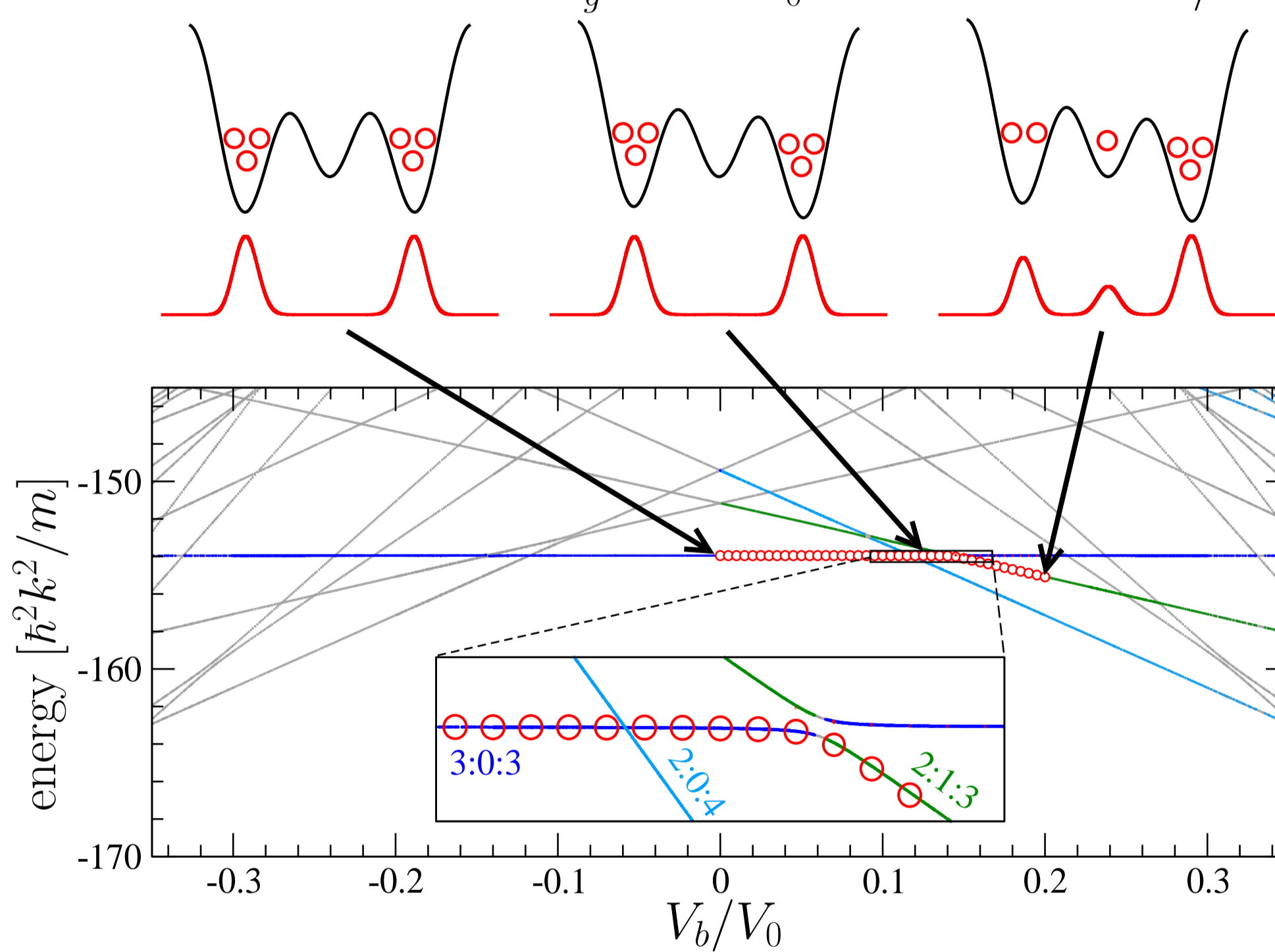
- assuming 6 atoms per triple-well site and
- neglecting hopping between adjacent triple-well sites (→ periodic boundary conditions in  $x$ :  $-\pi \leq kx \leq \pi$ ).



## Single-atom transport

- prepare the lattice with 6 atoms per triple-well site,
- make the time-dependent ramping  $V_b(t) = st$ ,
- decompose the time-dependent many-body wavefunction within the instantaneous eigenbasis.

Numerical calculation for  $V_g = 0.25V_0$  and  $s = 0.002\hbar^3 k^4/m^2$ :



Landau-Zener probability for nonadiabatic transitions at avoided crossings:

$$P = \exp[-2\pi \Delta E^2 / (\hbar s)]$$

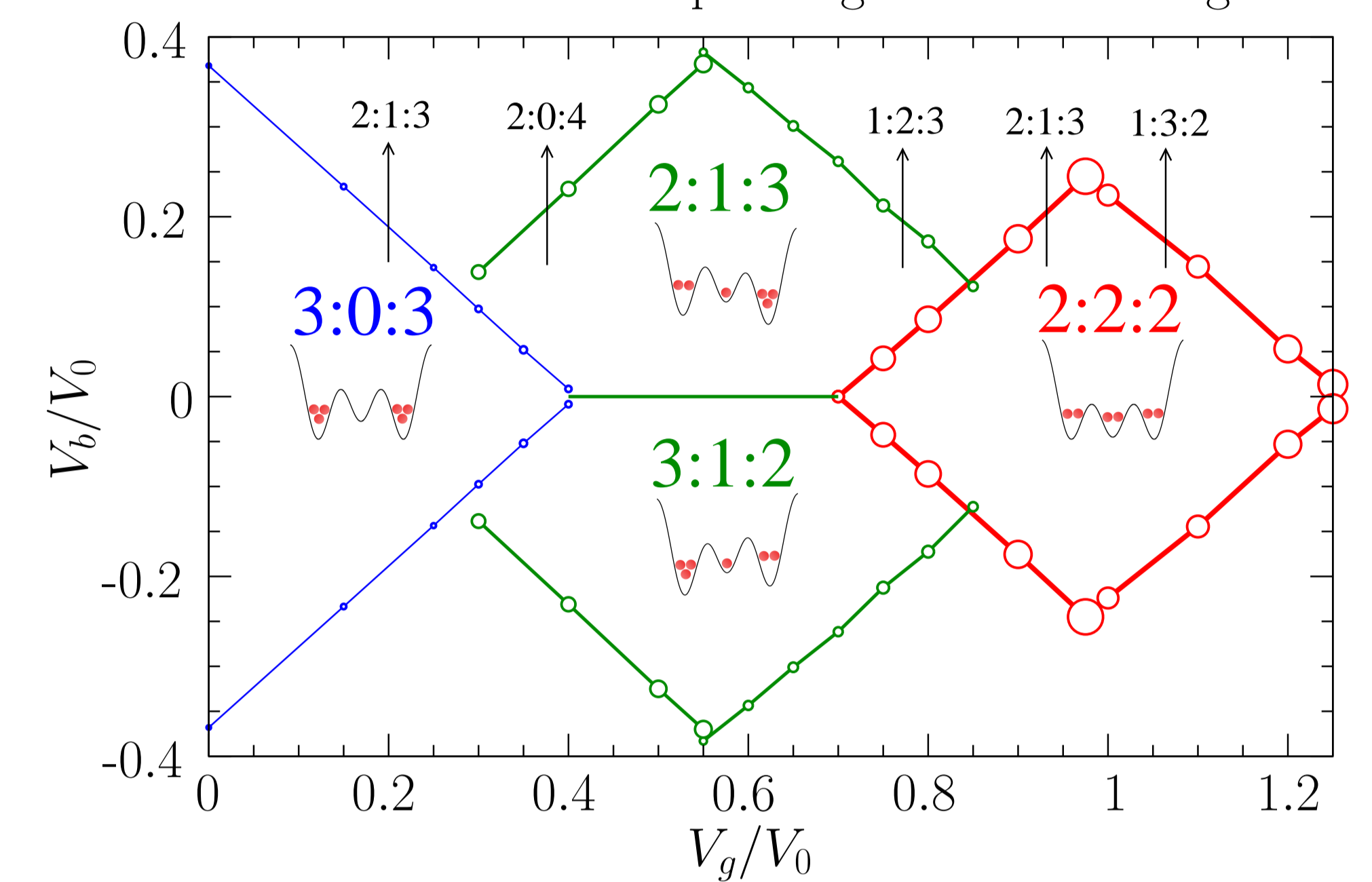
→ choose the ramping speed such that it is

- too fast for the unwanted anticrossings  $N_L:N_C:N_R \leftrightarrow N_L \pm 1:N_C:N_R \mp 1$  with energy scale  $\delta E \sim 0.001\hbar^2 k^2/m$  for  $N_C = 0$ ,
- but slow enough for the “good” anticrossings  $N_L:N_C:N_R \leftrightarrow N_L \pm 1:N_C \mp 1:N_R$  or  $N_L:N_C \pm 1:N_R \mp 1$  with energy scale  $\Delta E \sim 10 \times \delta E$ :

$$\delta E^2 \ll \hbar s < \Delta E^2$$

## Atomic “Coulomb” diamonds

Plotted are the bias voltages  $V_b$  at which a single-atom transfer takes place between adjacent wells. The size of the circles marks the extent of the corresponding avoided crossings.



## Bose-Hubbard model

Consider a simplified Bose-Hubbard model for the system with the on-site energies  $E_{L/R} = E_0 \pm V_b$  and  $E_C = E_1 - V_b$ , with the local interaction energies  $E_U^{(L/R/C)} = E_U \simeq 0.27V_0$ , and with negligible tunnel coupling between adjacent wells.

Local particle-addition energies:

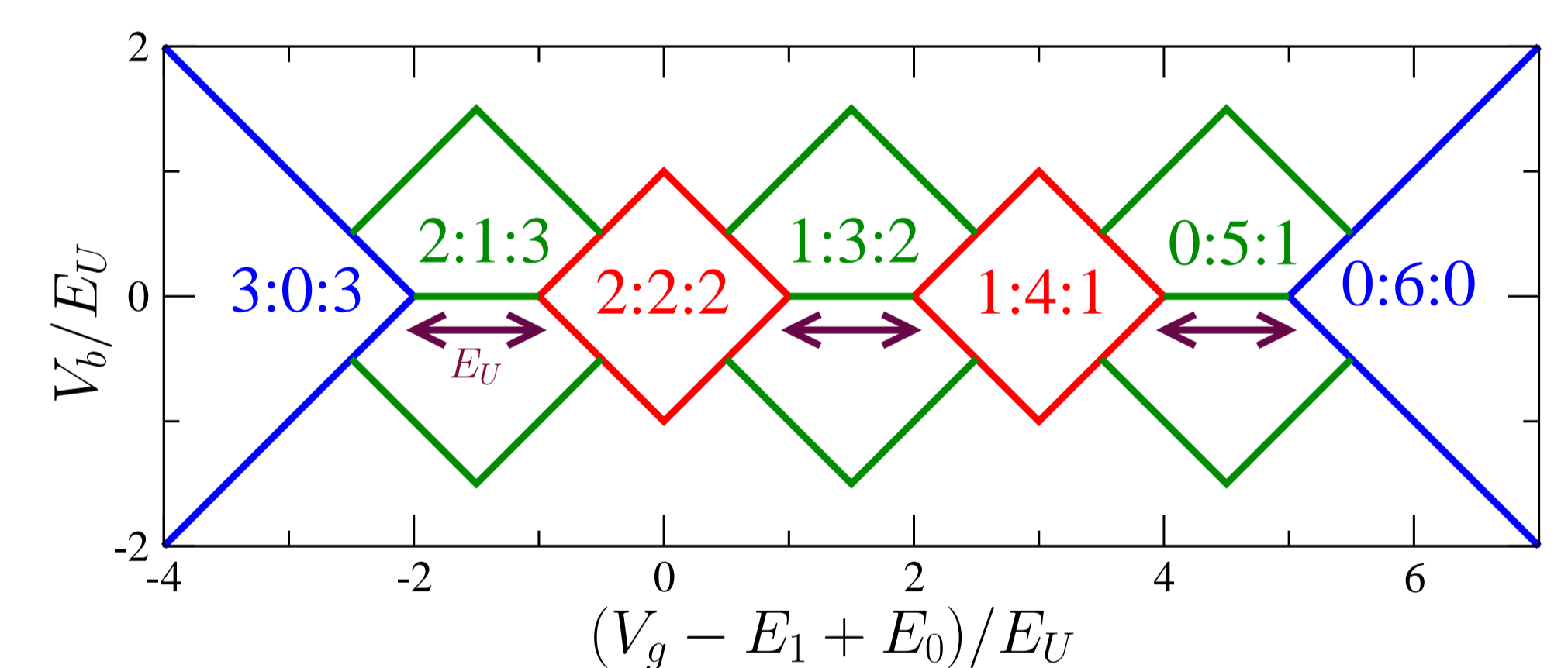
$$\mu_{L/R}^+ = E_0 \pm V_b + N_{L/R} E_U \text{ and } \mu_C^+ = E_1 - V_b + N_C E_U$$

→ avoided crossings of  $N_L:N_C:N_R \leftrightarrow N_L \pm 1:N_C \mp 1:N_R$ :

$$V_b = E_1 - E_0 - V_g + (N_C - N_L \mp 1) E_U$$

→ avoided crossings of  $N_L:N_C:N_R \leftrightarrow N_L:N_C \pm 1:N_R \mp 1$ :

$$-V_b = E_1 - E_0 - V_g + (N_C - N_R \pm 1) E_U$$



Main differences to Coulomb diamonds in quantum dots:

- open ends for empty dot and empty reservoirs
  - asymmetry between balanced ( $N_L = N_R$ ) and unbalanced ( $N_L = N_R \pm 1$ ) populations in the reservoirs
- microscopic nature of the reservoirs

## Perspectives

- extract local interaction energy  $E_U$  from the distance between the diamond structures
- single-atom pumping ( $3:0:3 \rightarrow 2:0:4$ ) following a closed curve in  $V_g - V_b$  space
- atomic transistors

P. Schlagheck, F. Malet, J. C. Cremon, and S. M. Reimann, New J. Phys., in press (arXiv:0912.0484)