# First principles study of heavily doped full Heusler Fe<sub>2</sub>YZ for high thermoelectric power factor

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#### Introduction

► The performance of thermoelectric materials is characterized by the Figure of Merit ZT, related to the Carnot efficiency:

$$\mathsf{ZT} = \frac{\mathsf{S}^2 \sigma}{\kappa_\mathsf{I} + \kappa_\mathsf{e}} \mathsf{T} \qquad \qquad \eta = \eta_\mathsf{Carnot} \frac{\sqrt{\mathsf{ZT} + 1} - 1}{\sqrt{\mathsf{ZT} + 1} + 1}$$

- The Power Factor  $S^2 \sigma$  is the key quantity to optimize for practical applications, such as heat waste recovery.
- $\triangleright$  S requires **low** effective mass carriers,  $\sigma$  requires **high** effective mass carriers.

 $\mathbf{m}_{\alpha\beta}^{*} = \left[\frac{1}{\hbar^{2}}\frac{\partial^{2}\epsilon(\mathbf{i},\mathbf{k})}{\partial\mathbf{k}}\right]$ 

#### **Electronic properties**





- Both characters can be met in a single band from orbitals with highly directional characters  $\rightarrow$  **HIGH** Power Factor !
- ► Where can we find such a band ? In **Fe<sub>2</sub>YZ** semiconductors, bottom of the conduction band ! Extensive work from Ref.  $[1] \rightarrow$  Promising **bulk** TE !



 $\blacktriangleright$  Fe<sub>2</sub>YZ compounds presents Fe – e<sub>g</sub> orbitals, main contribution to the bottom of the conduction band with the aformentionned features.





- Depending the matrix, half-metallic and metallic phases appear, previously associated with disorder [5].
- Electron density of the excess charge (x = 0.0313):

	Fe	e <sub>2</sub> TiSr	n <sub>1-x</sub> Sb	x		Fe <sub>2</sub> VA	Al <sub>1-x</sub> Si	X	F	e <sub>2</sub> Nb(	Ga <sub>1-x</sub> G	Ge <sub>x</sub>
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 $\blacktriangleright$  In the rigid band approx., *n*-type doping from  $0.2 \times 10^{21}$  cm<sup>-3</sup> to  $1.0 \times 10^{21}$  cm<sup>-3</sup> shift the Fermi level to the flat part of the Fe – e<sub>g</sub> band, ensuring maximum  $S^2\sigma$ .

## **Technical details**

- $\blacktriangleright$  Doping simulated by the 2  $\times$  2  $\times$  2 cubic supercell method: 128 atoms, 1 or 2 Y atoms replaced by A  $\longrightarrow \sim 0.6 \times 10^{21}$  cm<sup>-3</sup> and  $\sim 1.2 \times 10^{21}$  cm<sup>-3</sup> *n*-type doping values. The following compounds are studied :
- $\triangleright$  Fe<sub>2</sub>TiSn<sub>1-x</sub>Sb<sub>x</sub>;
- $\triangleright$  Fe<sub>2</sub>TiSi<sub>1-x</sub>P<sub>x</sub>;
- $\triangleright$  Fe<sub>2</sub>VAI<sub>1-x</sub>Si<sub>x</sub>;
- $\triangleright$  Fe<sub>2</sub>TaGa<sub>1-x</sub>Ge<sub>x</sub>;
- $ightarrow Fe_2NbGa_{1-x}Ge_x$ ; each with x = 0.0000; 0.0313; 0.0625.



Results consistent with a Stoner instability studied through a Jellium model (fixed geometry + 1 e<sup>-</sup> + charged background): $\Delta E_{ex} \times g^{NM}(E_F) > 1$ 

$X_2YZ$	$\Delta E_{ex}$ [eV]	$g^{NM}(E_F)$ [St./eV]	$\Delta E_{ex} \times g^{NM}(E_F)$
Fe <sub>2</sub> TiSn	0.200	35.31	7.1
$Fe_2TiSi$	0.154	37.84	5.8
$Fe_2VAI$	0.000	8.07	0.0
$Fe_2TaGa$	0.097	25.14	2.4
$Fe_2NbGa$	0.060	13.76	0.8

#### **Thermoelectric properties**



- Crystal14 package for the DFT calculations [2, 3], with B1 Wu-Cohen hybrid functional for  $E_{xc}$ .
- Thermoelectric properties computed with BoltzTraP [4]
- $\triangleright$  9  $\times$  9  $\times$  9 Monkhorst-Pack k-mesh for structural relaxation of conv. cell. (lattice para. + atomic positions).
- $> 5 \times 5 \times 5$  Monkhorst-Pack k-mesh for structural relaxation of SC (lattice para. + atomic positions).
- $\blacktriangleright$  10  $\times$  10  $\times$  10 Monkhorst-Pack k-mesh for electronic properties.
- > 32  $\times$  32  $\times$  32 Monkhorst-Pack k-mesh for transport and TE properties.
- $\blacktriangleright$  Energy convergence criterium fixed at  $10^{-9}$  Ha.
- ▶ Relaxation time  $\tau = 3.4 \times 10^{-14}$  s, from ref. [1].
- ▶ Basis sets, same as Ref. [1].

### Despite spin-splitting a wide array of good **PF** can be achieved.

## Conclusions

- $\blacktriangleright$  *n*-type doping shifts the Fermi level toward the Fe e<sub>g</sub> band. ► Spin-splitting of the Fe –  $e_g$  band occurs in  $Fe_2TiSn_{1-x}Sb_x$ ,  $Fe_2TiSi_{1-x}P_x$ , and  $Fe_2TaGa_{1-x}Ge_x$ .
- > A wide array of good power factors can be achieved at higher temperatures, ranging from 5 to 20  $\times 10^{-3}$  W/K<sup>2</sup>m.  $\triangleright$  *n*-type doped Fe<sub>2</sub>NbGa is the most promising candidate !

#### References

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