

# MODEL-BASED COMPUTATION OF TOTAL STRESSED BLOOD VOLUME FROM A PRELOAD REDUCTION EXPERIMENT

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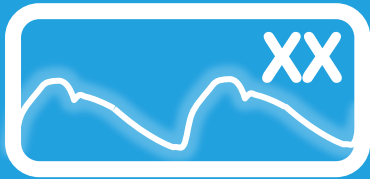
19<sup>TH</sup> IFAC WORLD CONGRESS  
AUGUST 24-29, 2014, CAPE TOWN, SOUTH AFRICA

# 1

# INTRODUCTION

## 1

## LUMPED-PARAMETER CVS MODELS



Limited amount  
of data in the ICU

Difficult  
treatment

Cardiovascular  
diseases

# 1

# INTRODUCTION

## 1

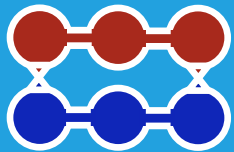
## LUMPED-PARAMETER CVS MODELS



Limited amount  
of data in the ICU

Difficult  
treatment

Cardiovascular  
diseases



Mathematical model

Clear physiological  
picture

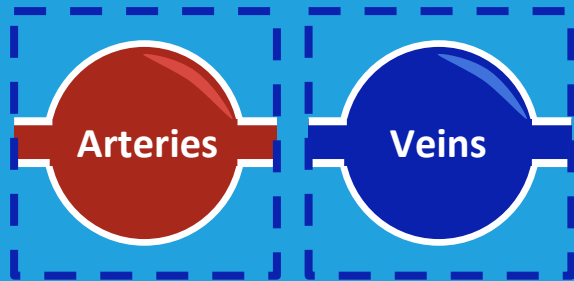
# 1

# INTRODUCTION

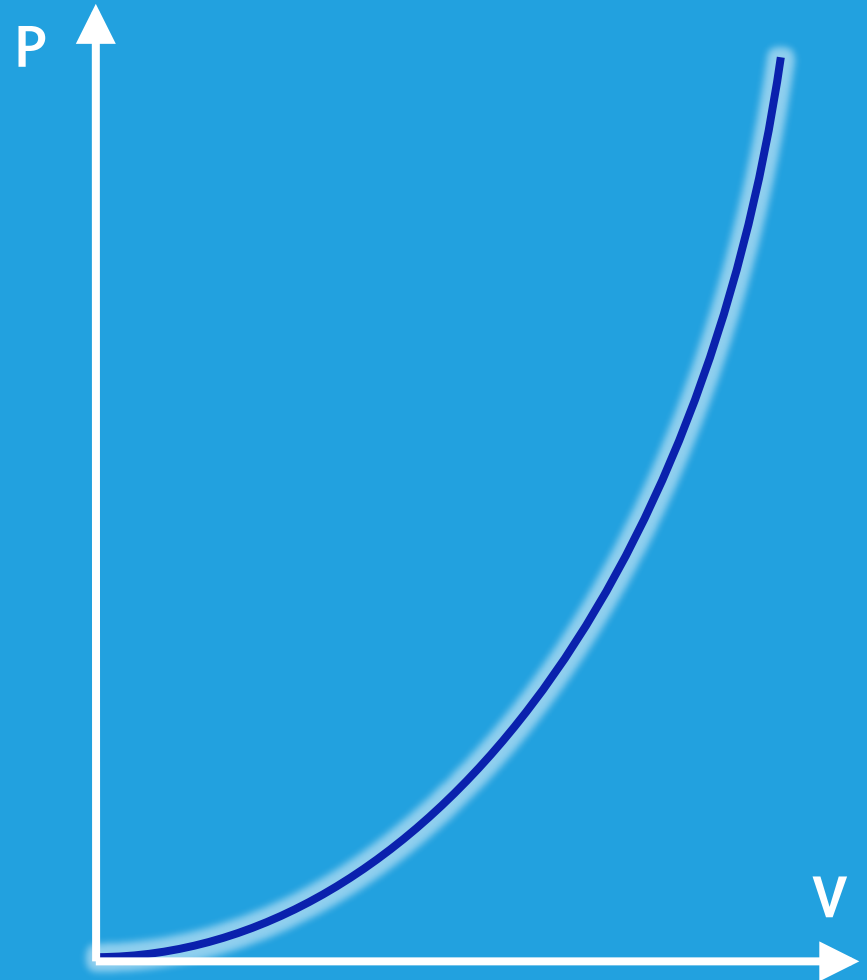
## 1

## LUMPED-PARAMETER CVS MODELS

Passive vessels:



$$P = f(V)$$



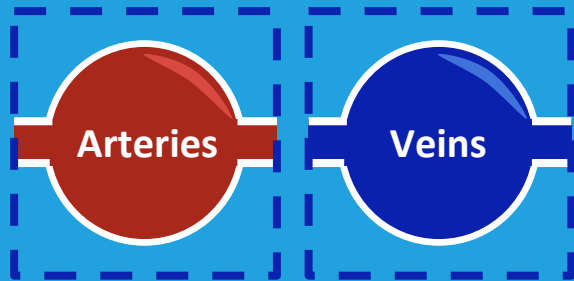
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# INTRODUCTION

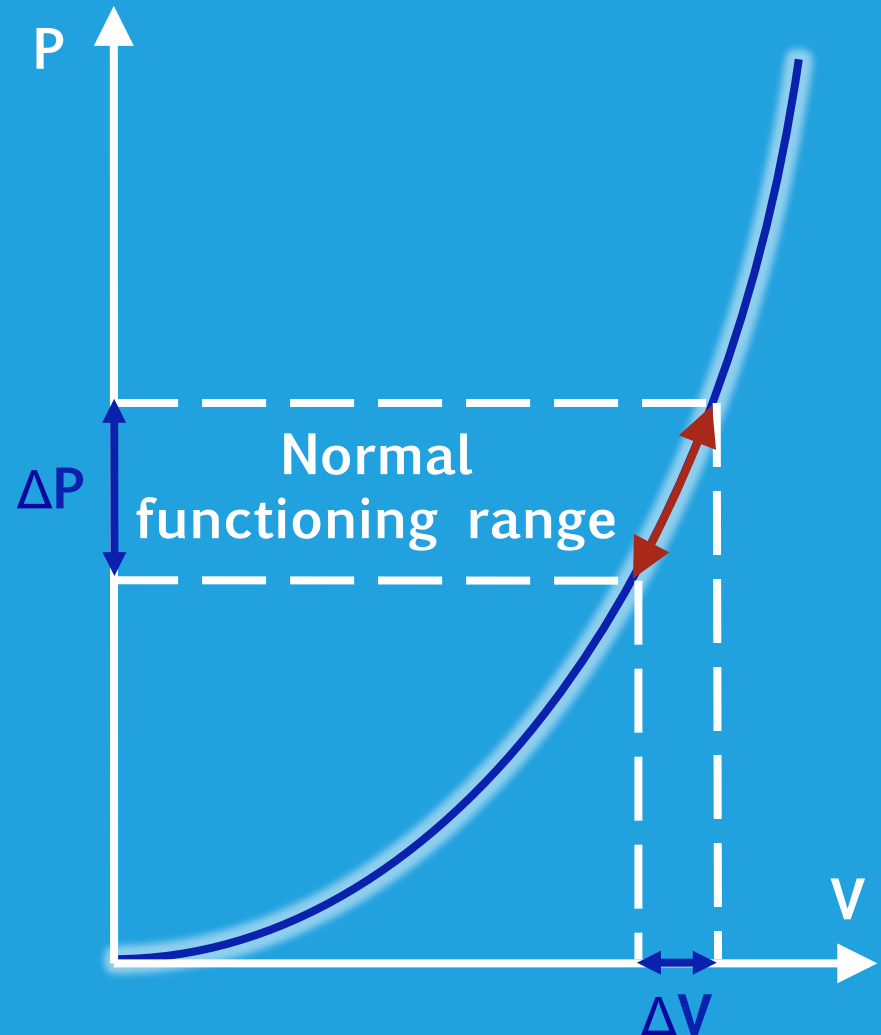
## 1

## LUMPED-PARAMETER CVS MODELS

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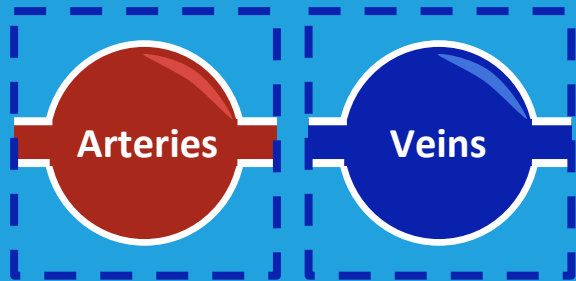
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# INTRODUCTION

## 1

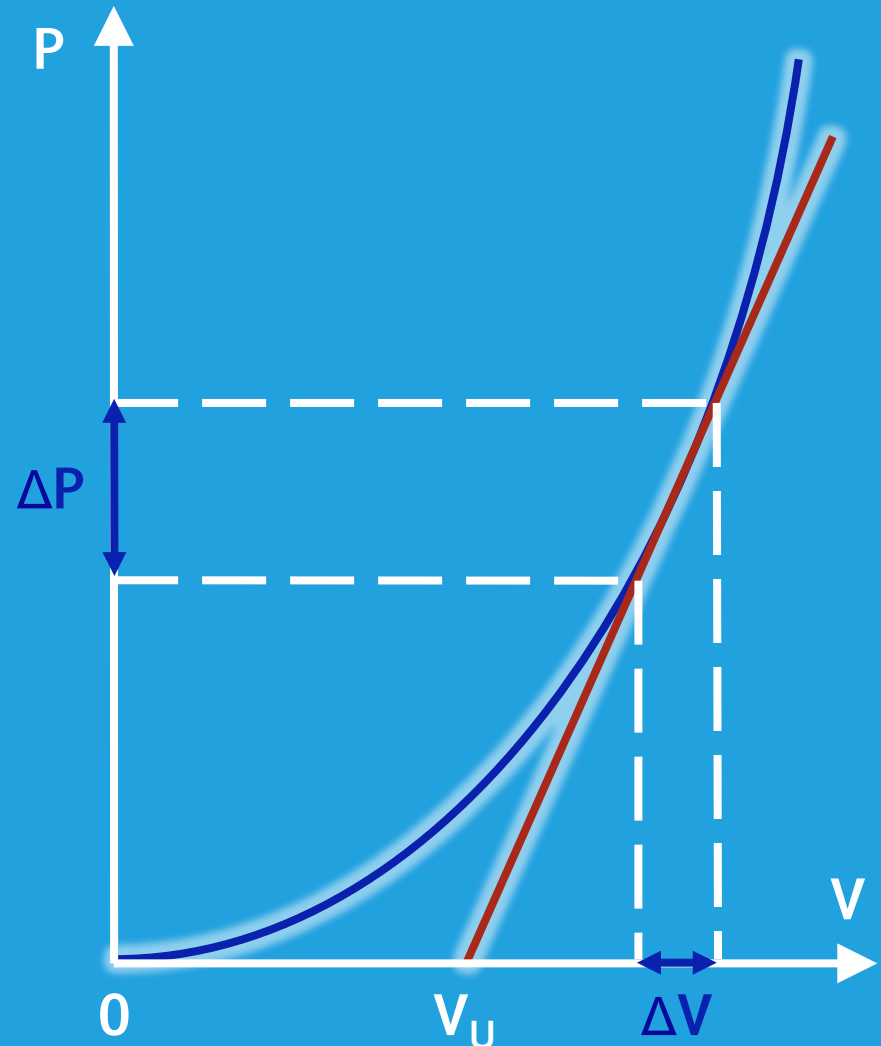
## LUMPED-PARAMETER CVS MODELS

Passive vessels:



$$E = \Delta P / \Delta V$$

$$P = E (V - V_U)$$



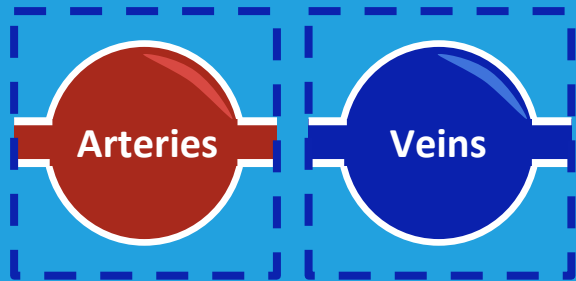
# 1

# INTRODUCTION

## 1

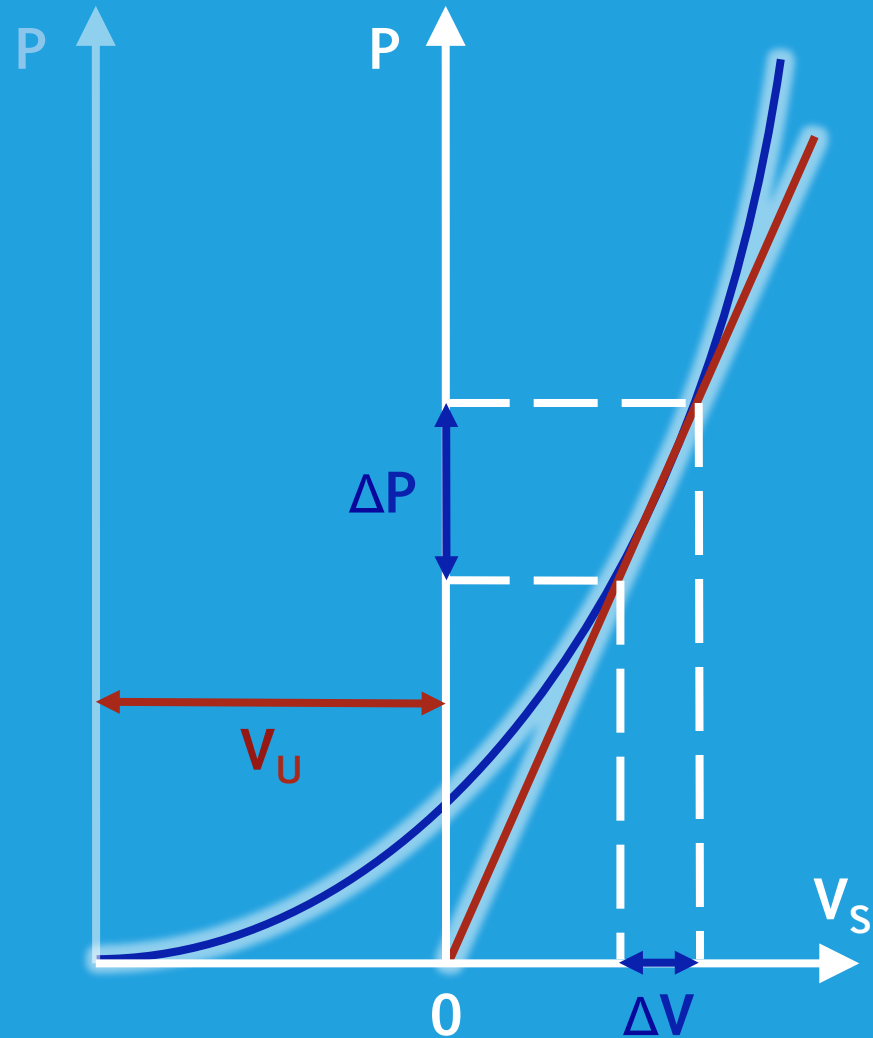
## LUMPED-PARAMETER CVS MODELS

Passive vessels:



$$V_S = V - V_U$$

$$P = E V_S$$



# 1

# INTRODUCTION

## 2

## TOTAL STRESSED BLOOD VOLUME

$$V$$

- Total blood volume:  
 $TBV = \sum_i V_i$

- Unstressed volumes:

$$V_{U,i}$$

$$V_S = V - V_U$$

- Total stressed blood volume:  
 $SBV = \sum_i V_{S,i}$



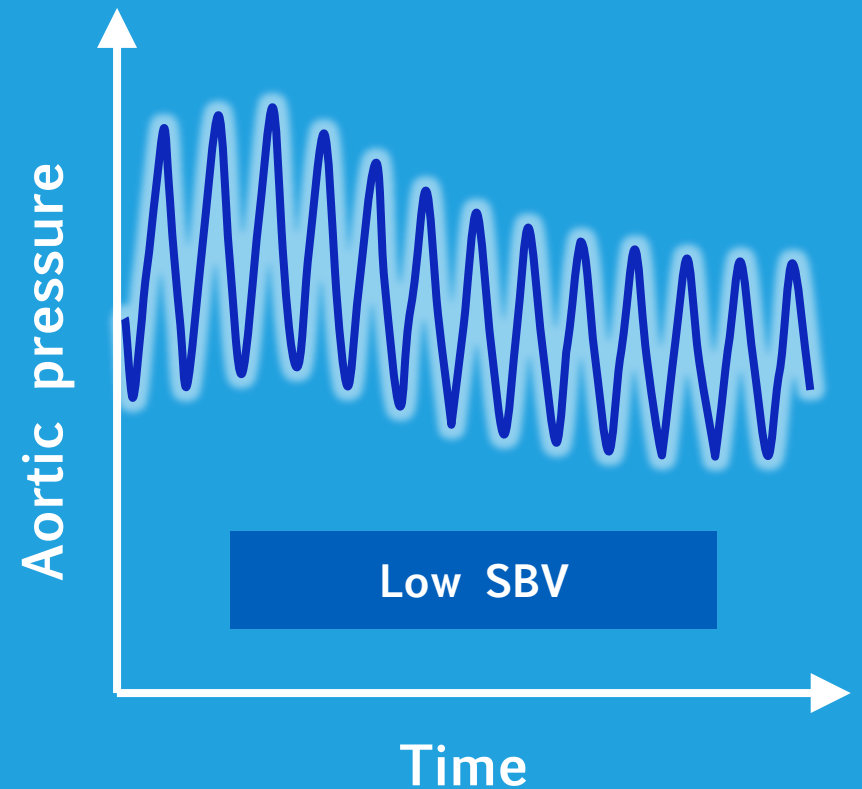
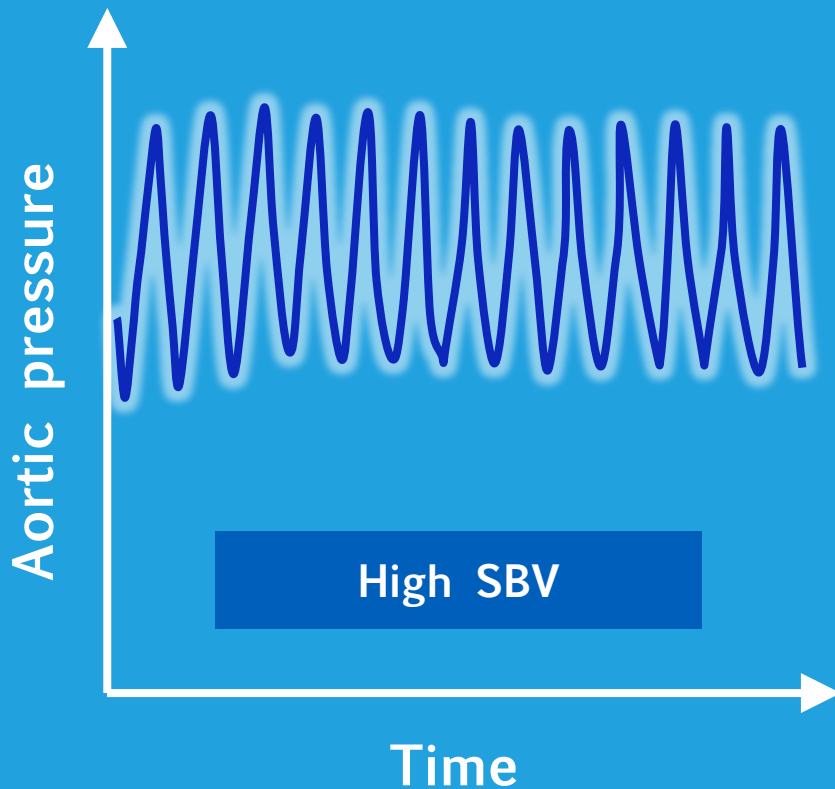
# 1

# INTRODUCTION

## 2

## TOTAL STRESSED BLOOD VOLUME

- In engineering



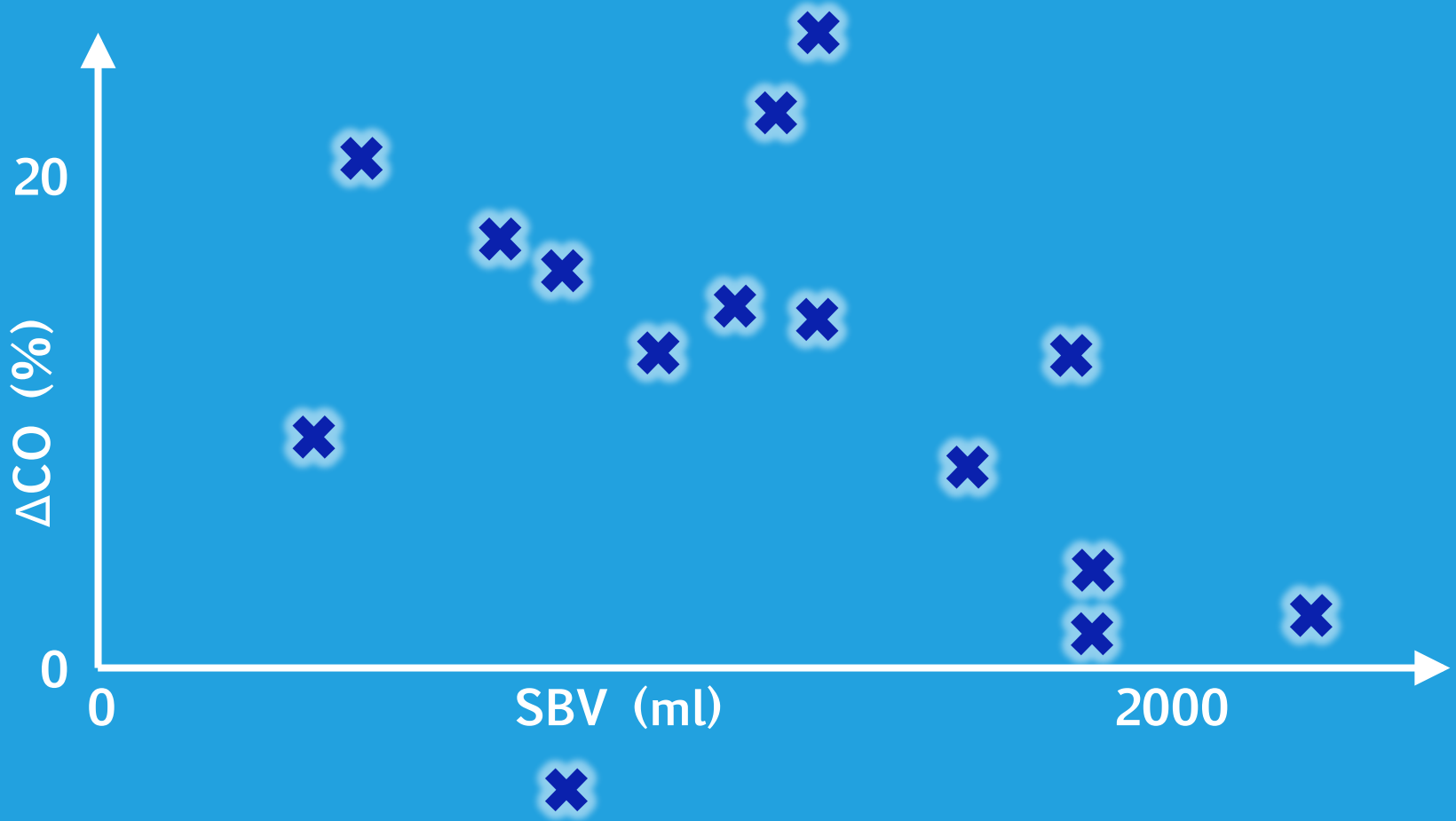
# 1

# INTRODUCTION

## 2

## TOTAL STRESSED BLOOD VOLUME

- In medicine (Maas *et al.*, 2012)

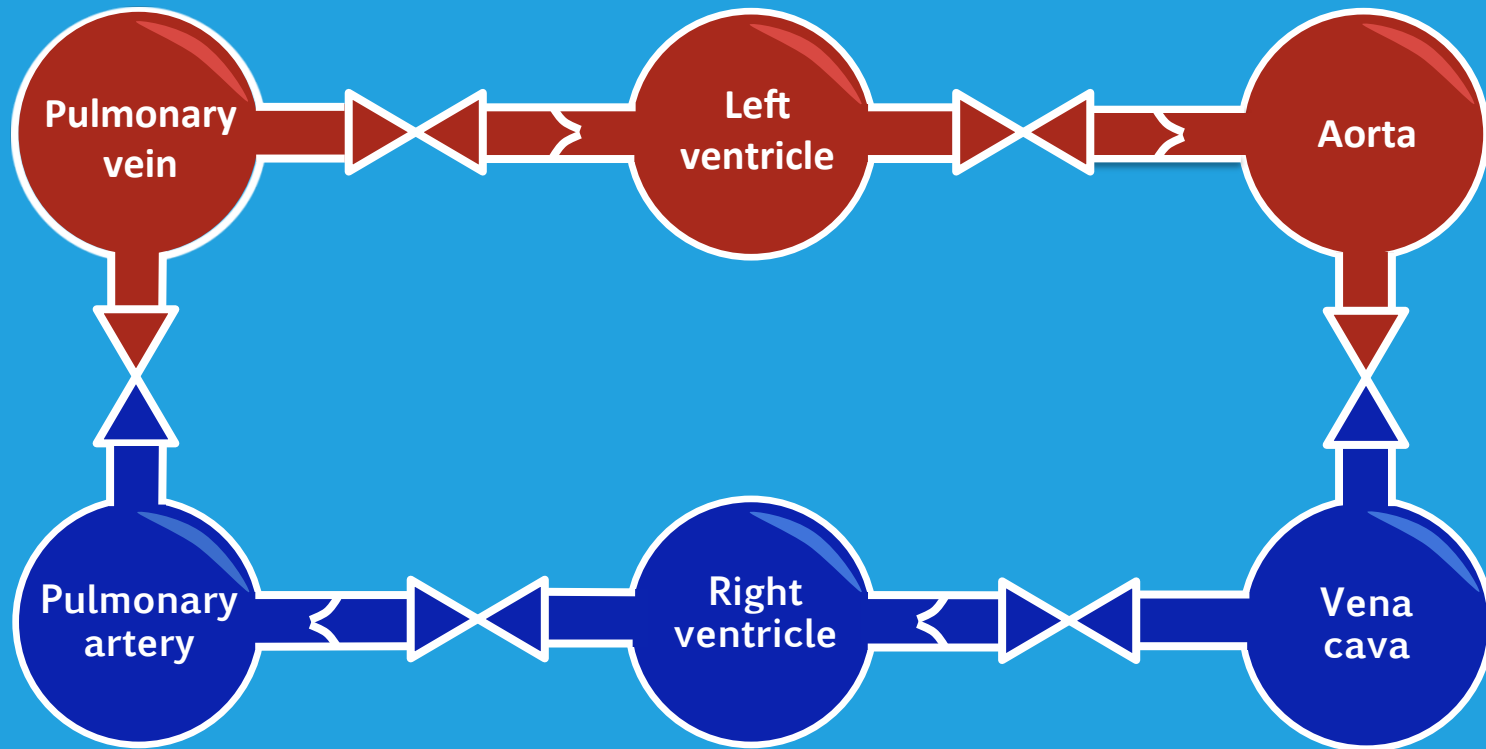


# 2

# METHODS

## 1

## CVS MODEL



Flow resistance



Valve

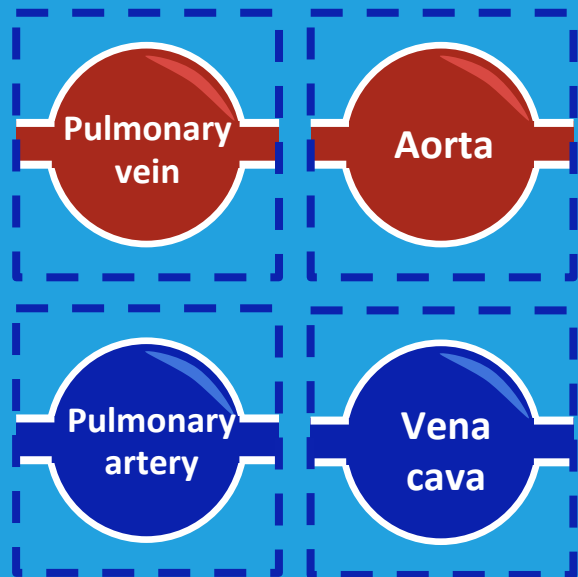
# 2

# METHODS

## 1

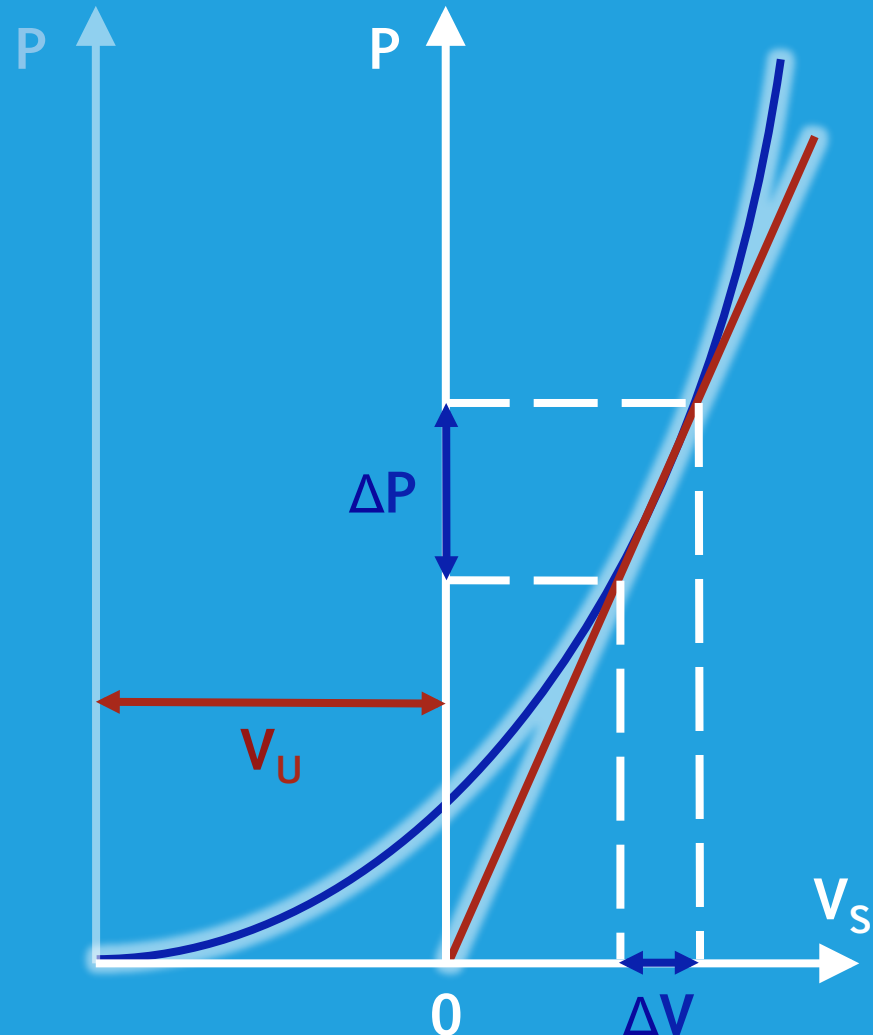
## CVS MODELS

Passive chambers:



$$V_S = V - V_U$$

$$P = E V_S$$



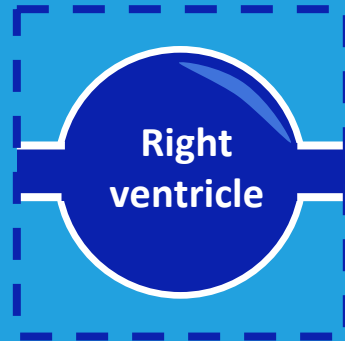
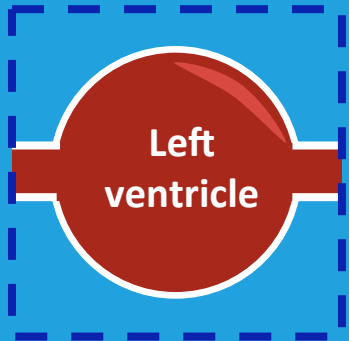
# 2

# METHODS

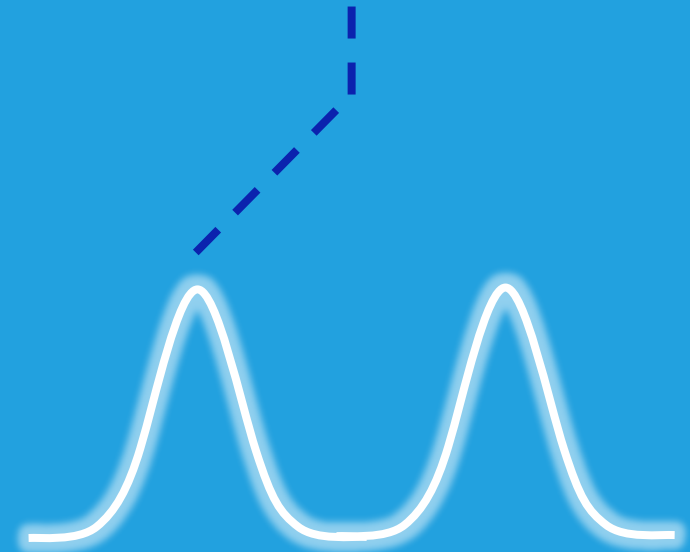
## 1

## CVS MODEL

Cardiac chambers:



$$P = E \ e(t) \ V_S$$



Driver function  
 $e(t)$  in  $[0, 1]$

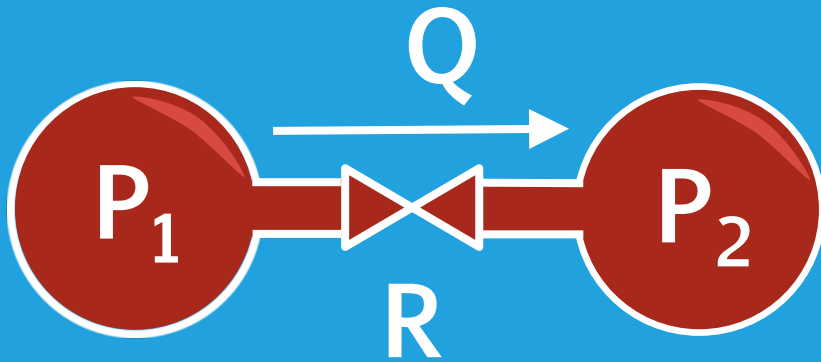
# 2

# METHODS

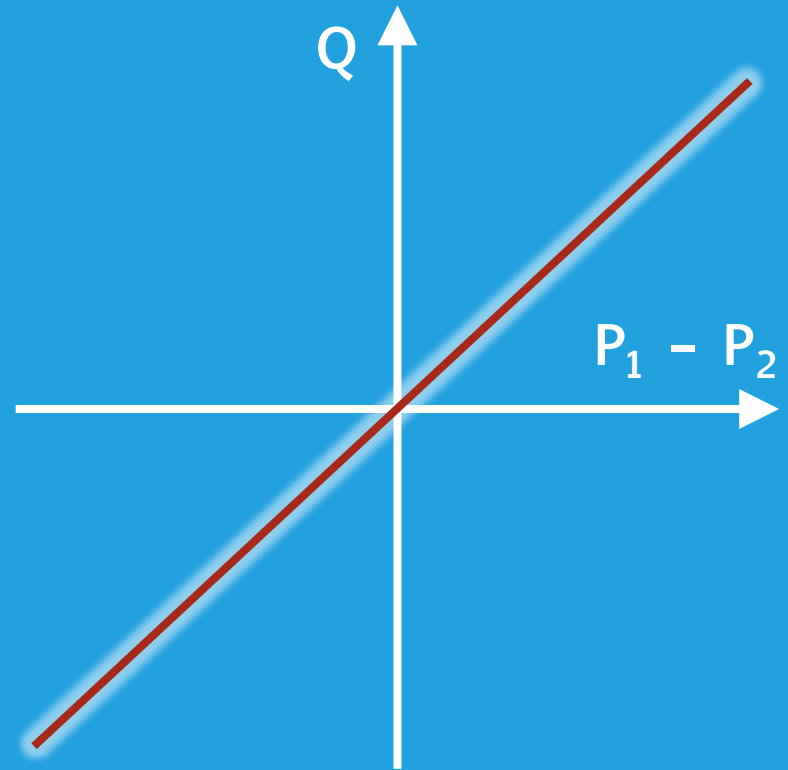
## 1

## CVS MODEL

No valve:



$$Q = \frac{P_1 - P_2}{R}$$



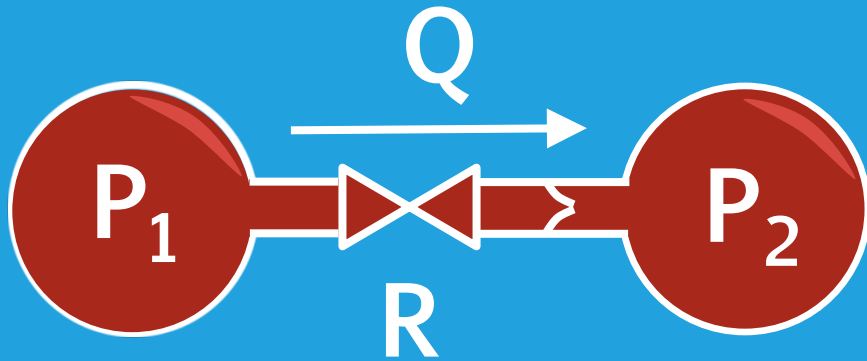
# 2

# METHODS

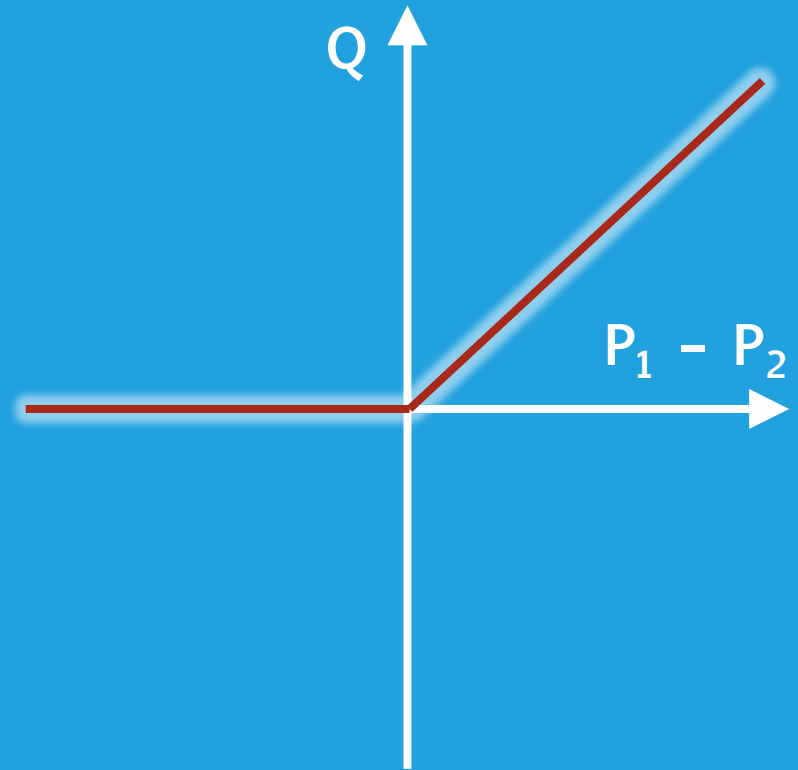
## 1

## CVS MODEL

Valve:



$$Q = \begin{cases} \frac{P_1 - P_2}{R} & \text{if } P_1 > P_2 \\ 0 & \text{otherwise} \end{cases}$$



# 2

# METHODS

## 1

## CVS MODEL

Continuity equation:



$$\dot{V}_S = Q_{in} - Q_{out}$$



# 2

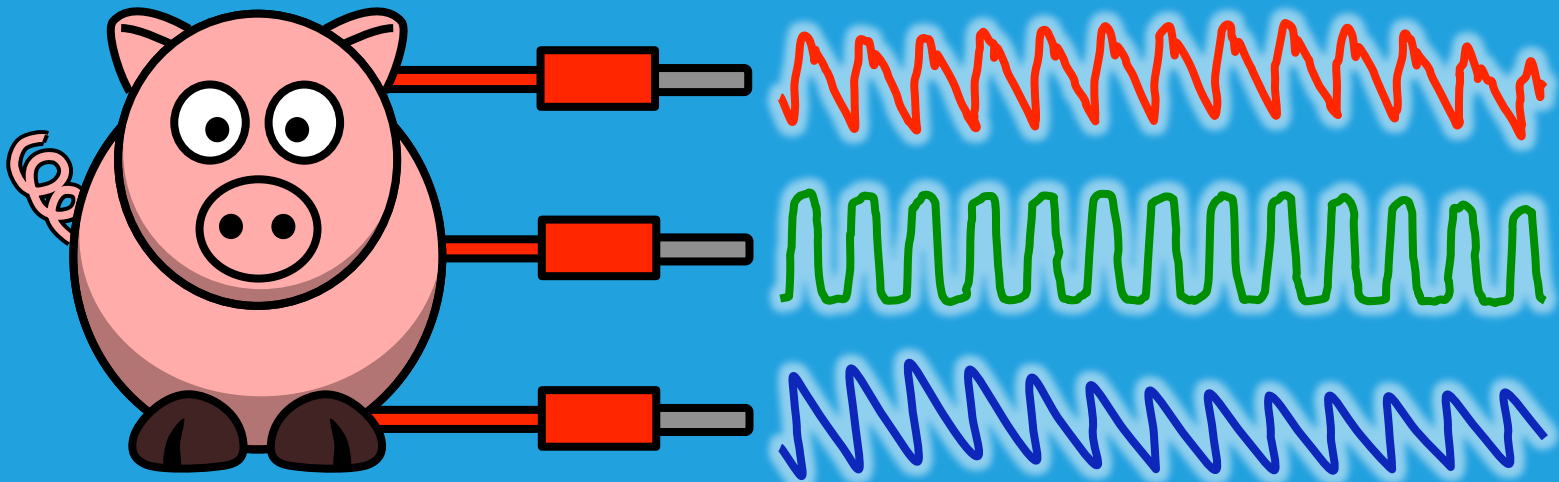
# METHODS

## 2

## EXPERIMENTAL DATA

Pig data:

- Aortic and pulmonary artery pressures
- Ventricular pressures
- Ventricular volumes

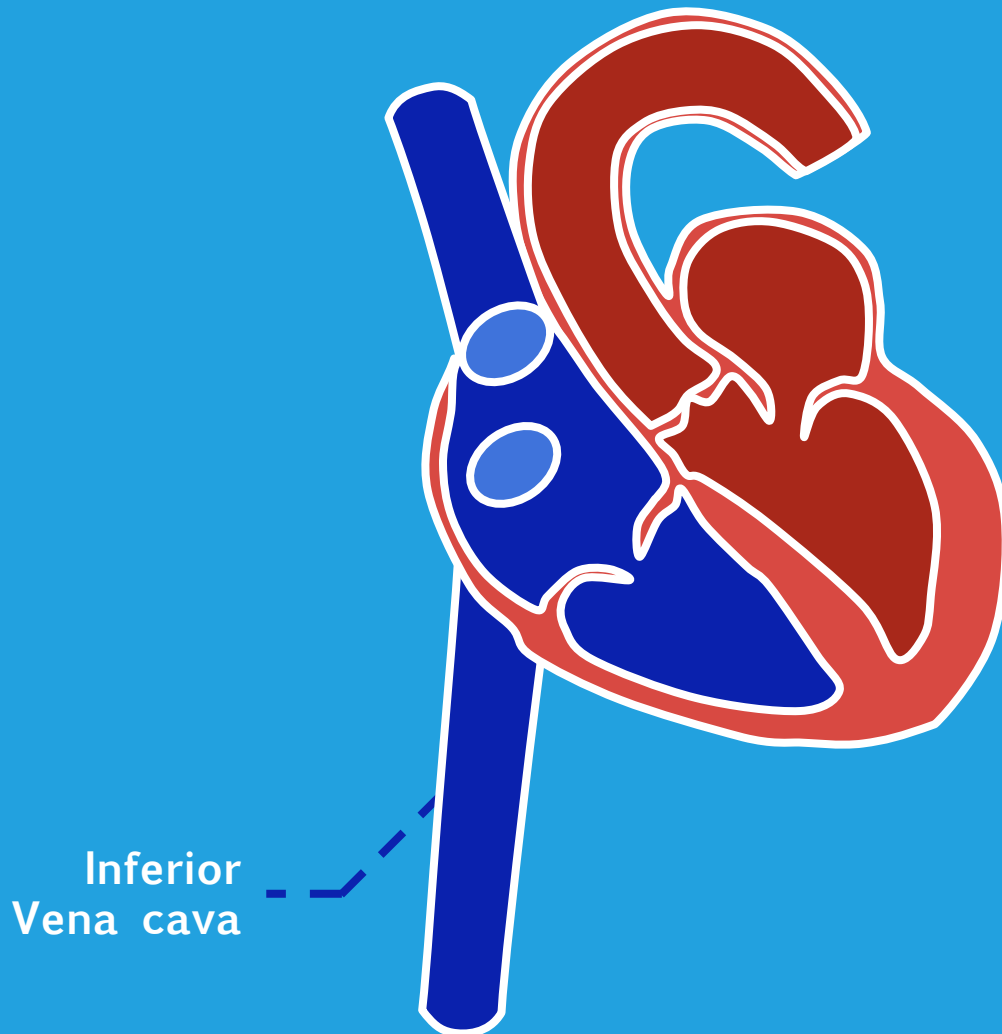


# 2

# METHODS

## 2

## EXPERIMENTAL DATA

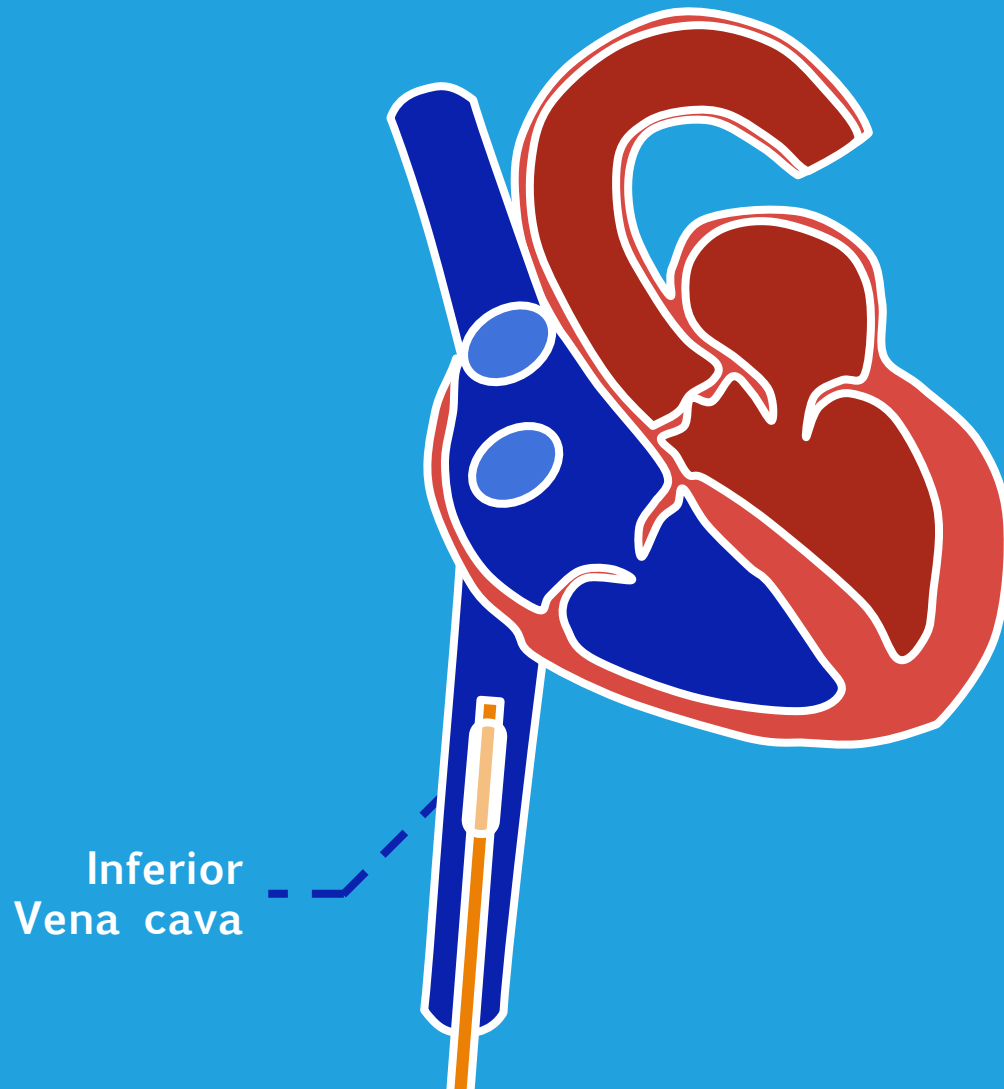


# 2

# METHODS

## 2

## EXPERIMENTAL DATA

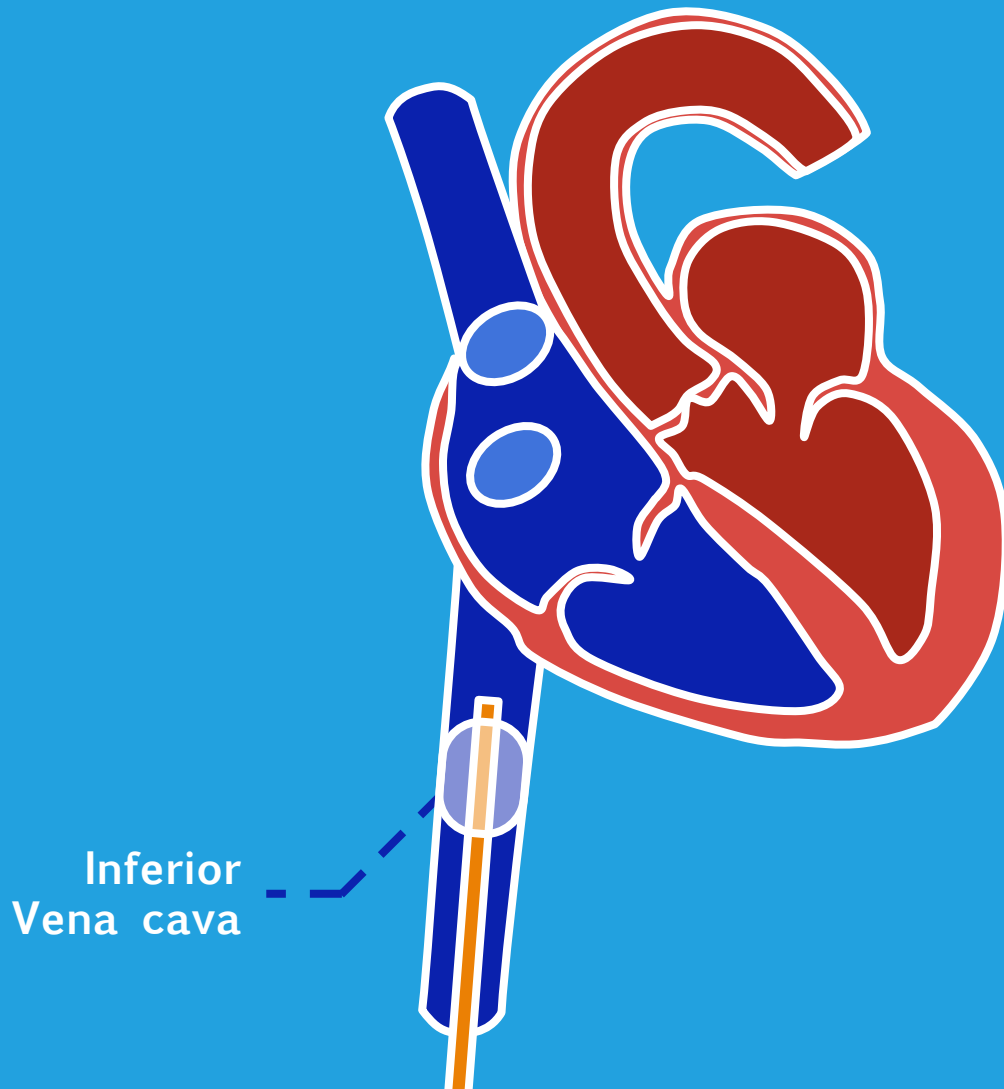


# 2

# METHODS

## 2

## EXPERIMENTAL DATA



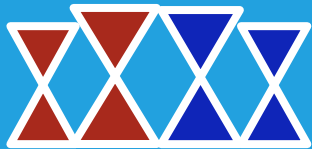
# 2

# METHODS

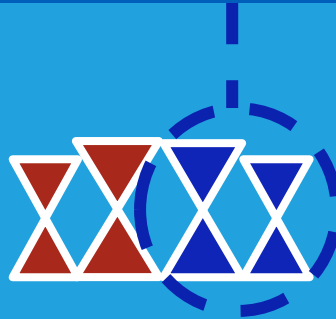
## 3

## PARAMETER IDENTIFICATION

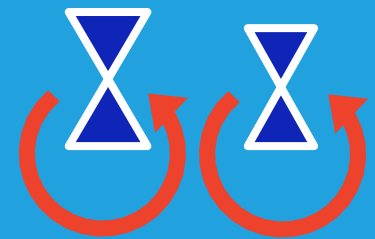
Nominal parameter values



Subset selection algorithm



Identification of selected parameters



# 2

# METHODS

## 3

## PARAMETER IDENTIFICATION: STEP 1

Nominal parameter values

- From the literature
- Directly from data, e.g.:

$$SVR = \frac{MAP}{CO}$$

# 2

# METHODS

## 3

## PARAMETER IDENTIFICATION: STEP 2

Nominal parameter  
values



Subset selection  
algorithm

- $e$  = simulations – measurements
- Jacobian matrix  $J = \partial e / \partial p$
- Hessian matrix  $H \approx J^T J$
- Compute the eigenvalues of  $H$

# 2

# METHODS

## 3

## PARAMETER IDENTIFICATION: STEP 2

Nominal parameter  
values



Subset selection  
algorithm

- Select the  $r$  largest eigenvalues of  $H$
- Find the corresponding parameters through a QR decomposition
- Select these  $r$  parameters for optimization



# 2

# METHODS

## 3

## PARAMETER IDENTIFICATION: STEP 3

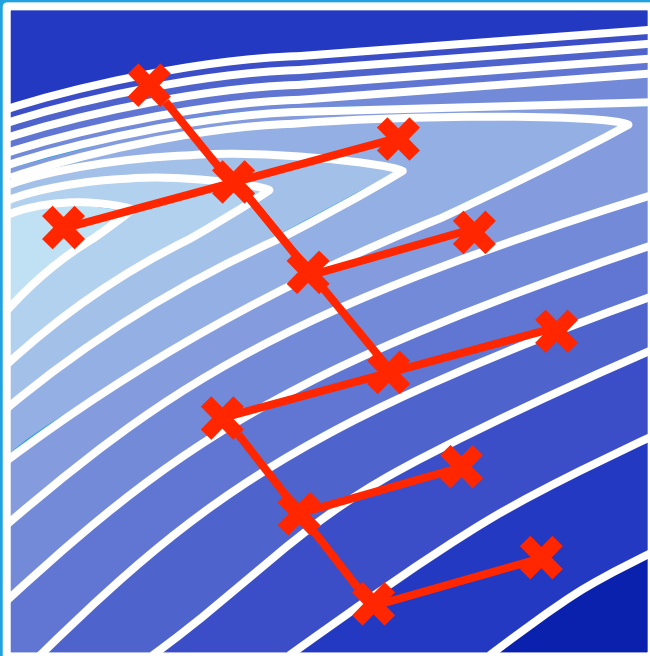
Nominal parameter values



Subset selection algorithm



Identification of selected parameters



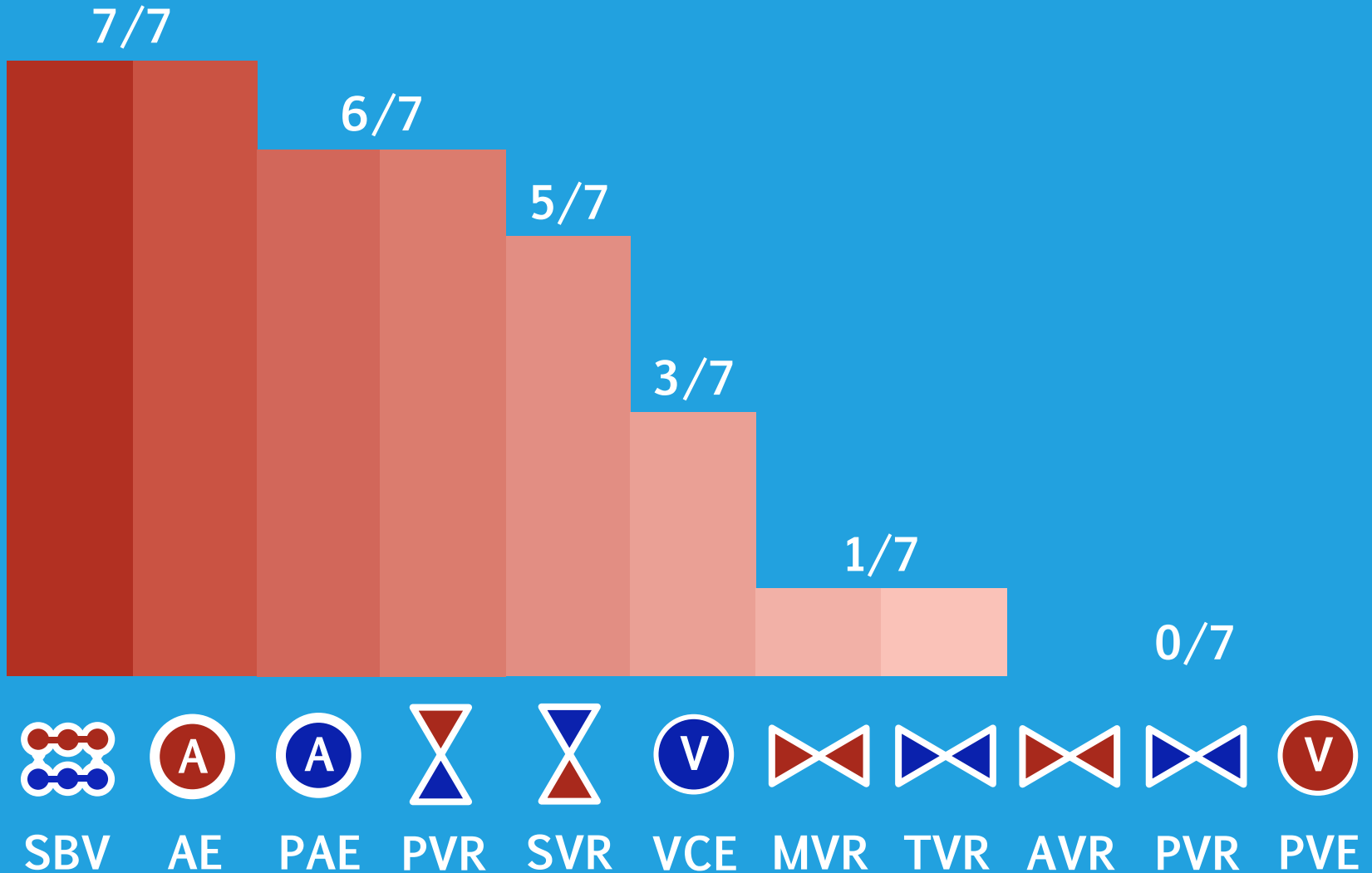
Using the direct search method and the initial values computed at step 1.

# 3

# RESULTS

## 1

## NUMBER OF PARAMETER SELECTIONS

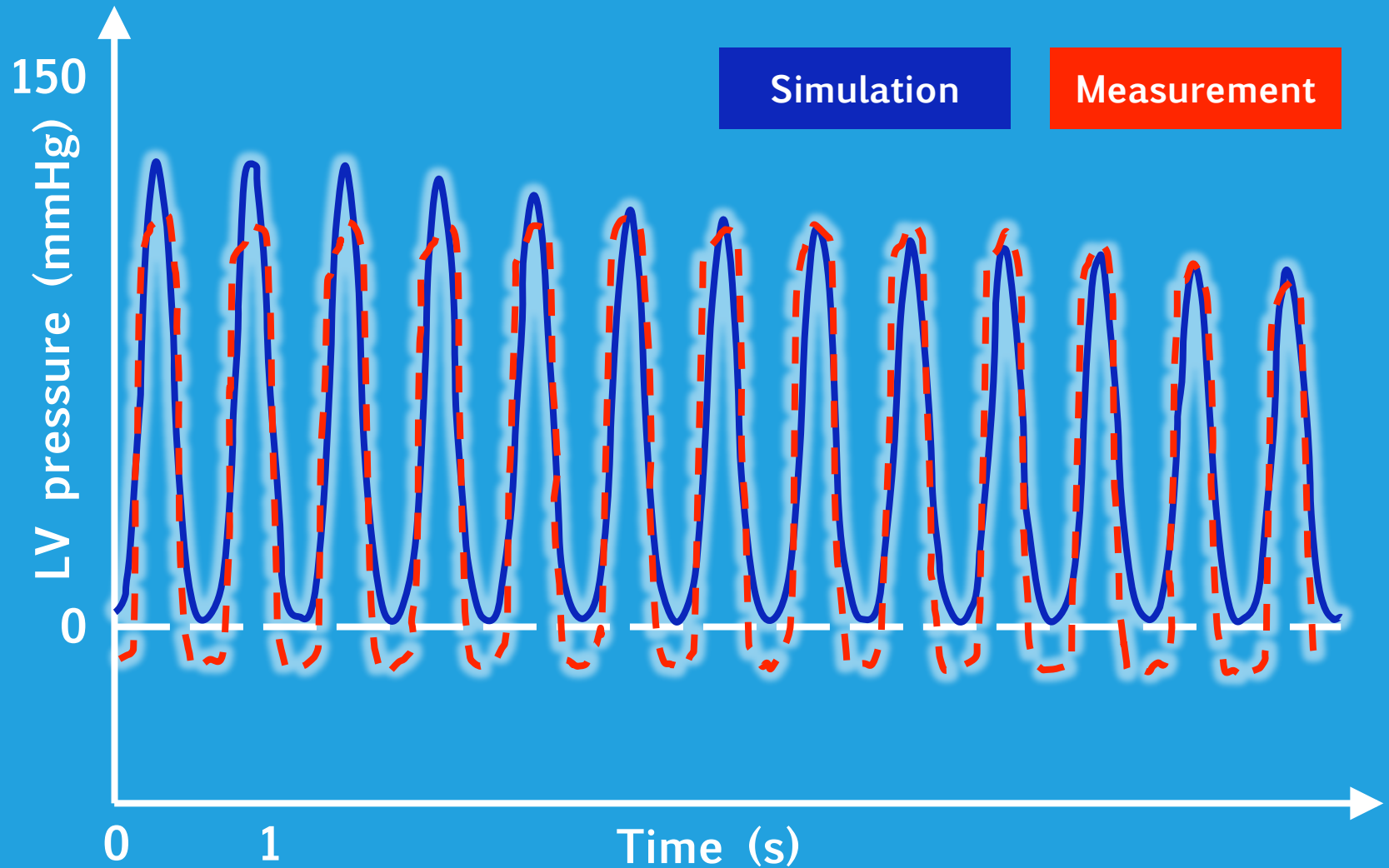


# 3

# RESULTS

## 2

## PARAMETER ADJUSTMENT

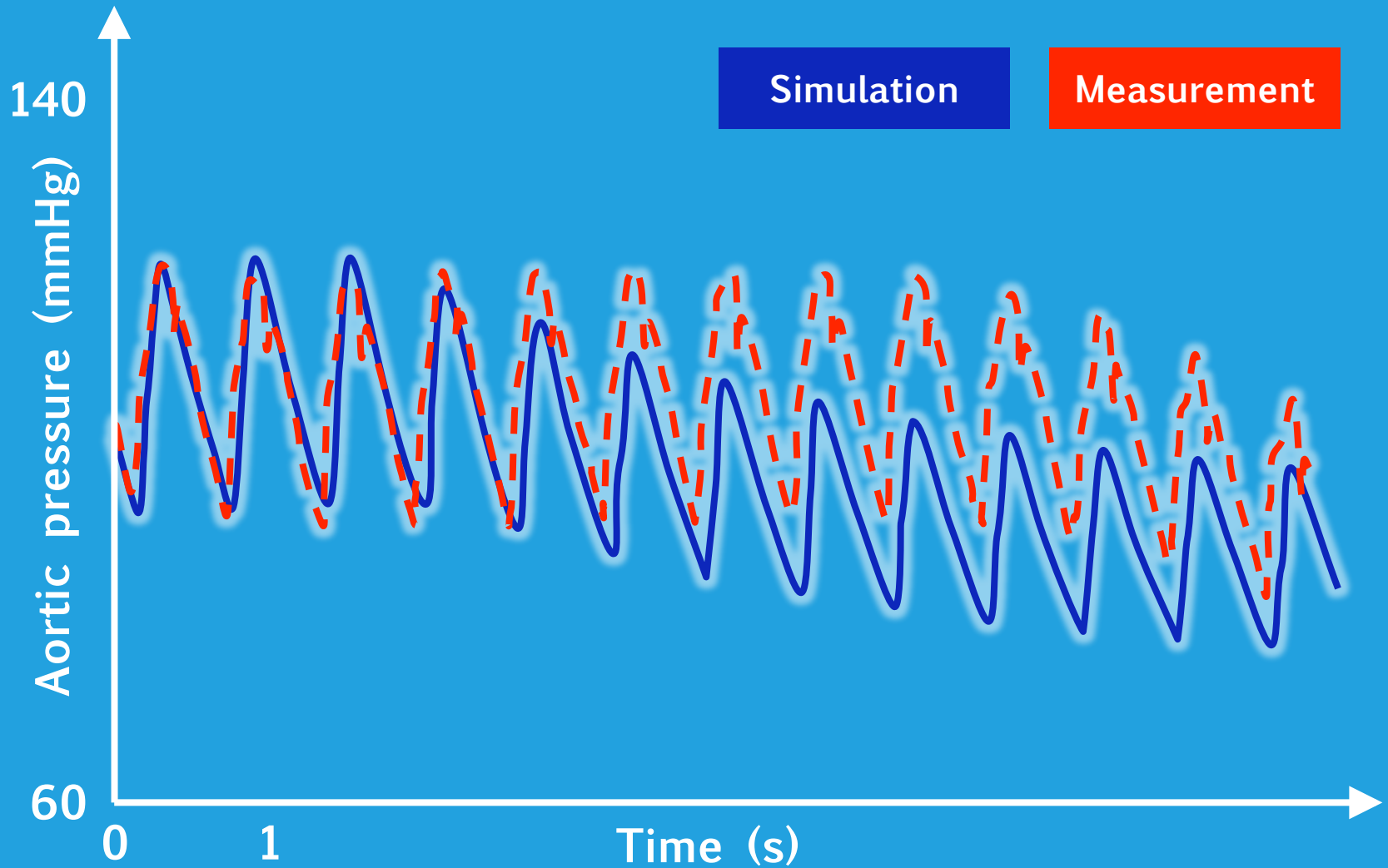


# 3

# RESULTS

## 2

## PARAMETER ADJUSTMENT

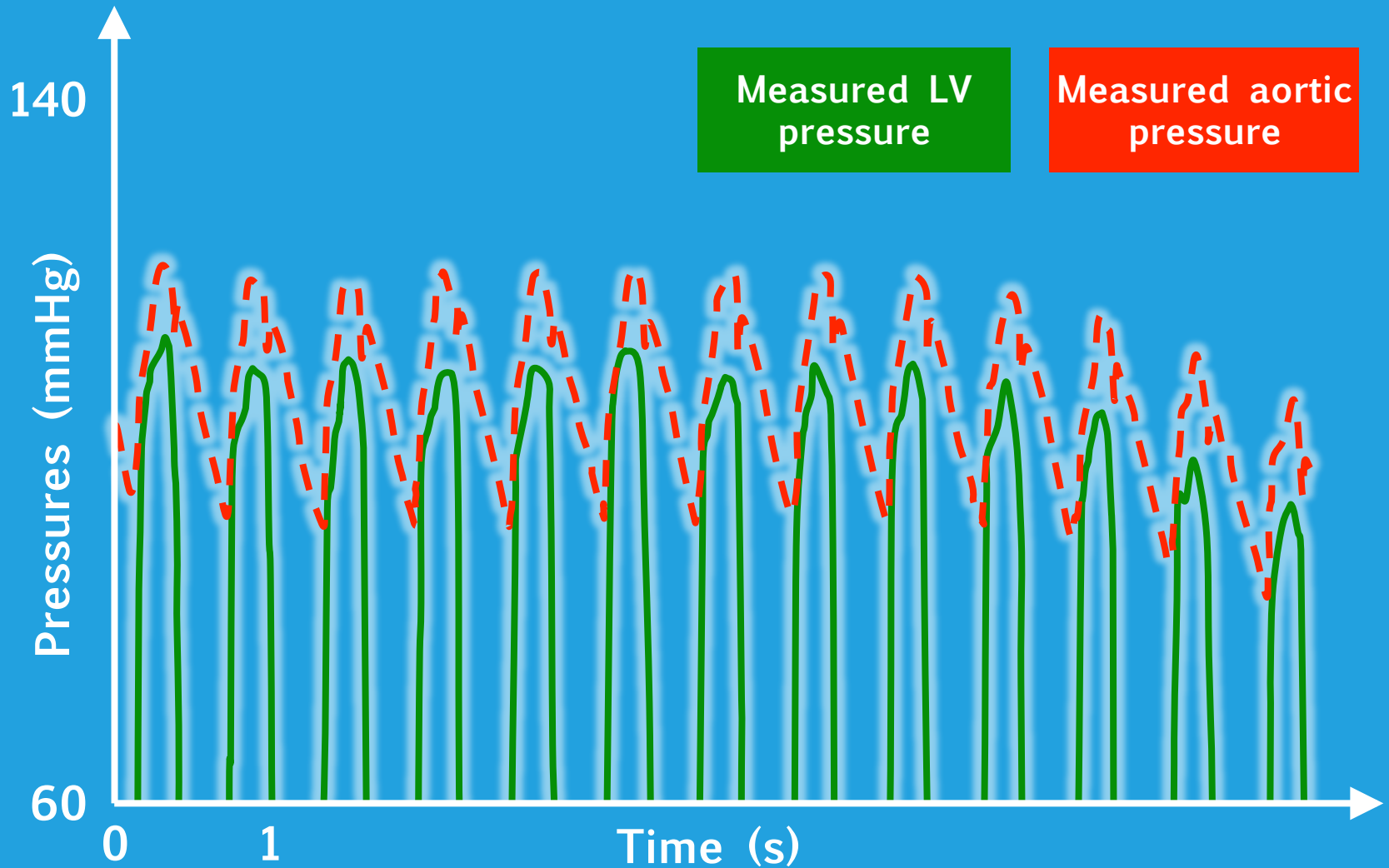


# 3

# RESULTS

## 2

## PARAMETER ADJUSTMENT

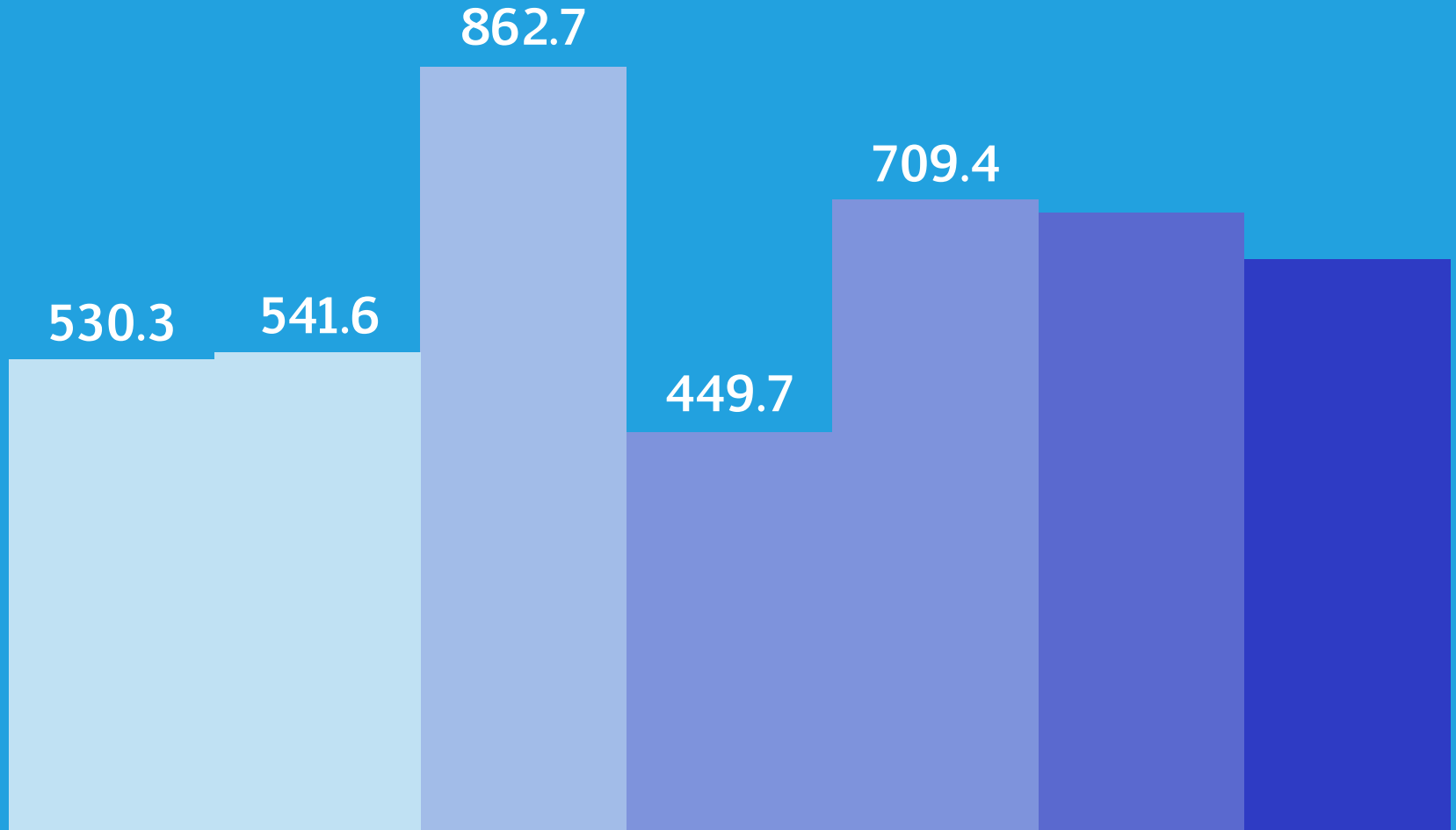


3

# RESULTS

3

VALUE OF SBV (ml)



Datasets

# 4

# LIMITATIONS

The method needs validation.

- With the usual way to compute SBV.
- Track SBV during vascular filling.
- Using simulated data.

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# 5

# EXTENSIONS

The method could be made fully non-invasive:

- SBV is an important parameter.
  - ➔ No need for ventricular pressures.
- Change load by raising the legs.
  - ➔ No need for vena cava occlusion.

# 5

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# EXTENSIONS

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- Model-based method to compute SBV from preload reduction data.
- SBV is an important parameter
  - If validated, the method could provide a non-invasive way to track SBV.

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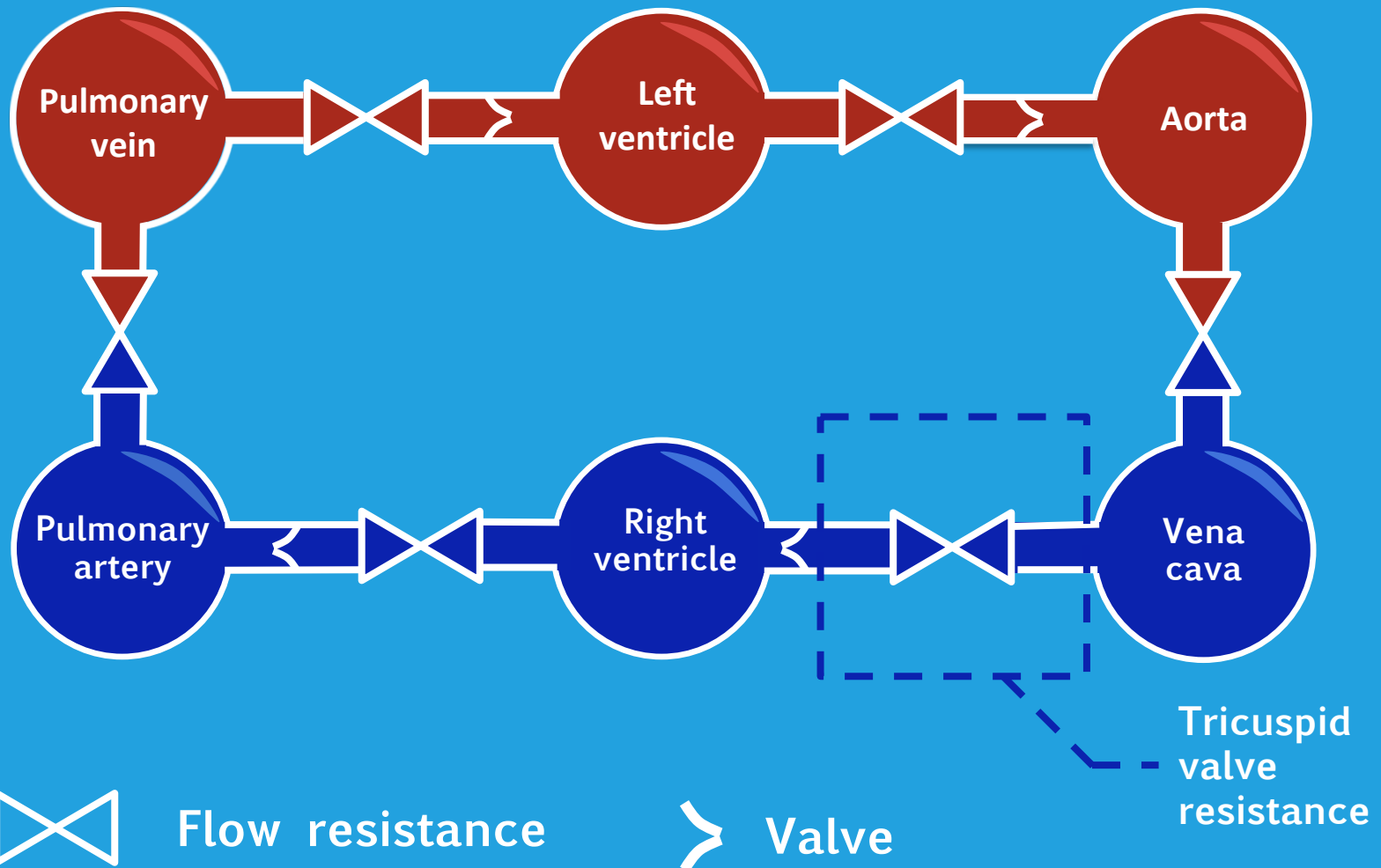
Thanks for your attention!  
Questions?

# 2

# METHODS

## 2

## EXPERIMENTAL DATA

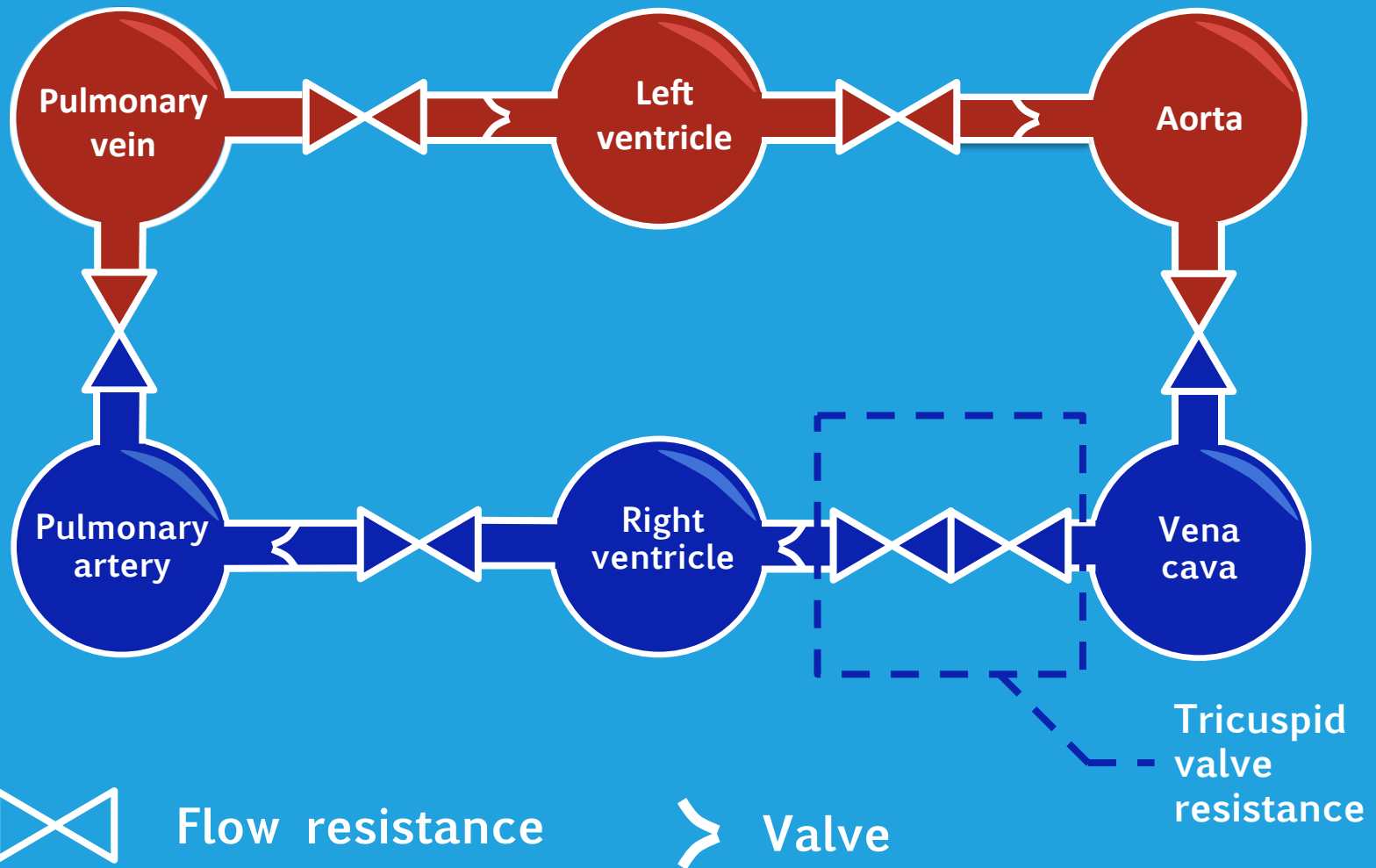


# 2

# METHODS

## 2

## EXPERIMENTAL DATA



# 3

# RESULTS

## 4

## SBV VERSUS WEIGHT

