

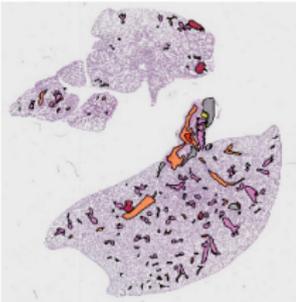
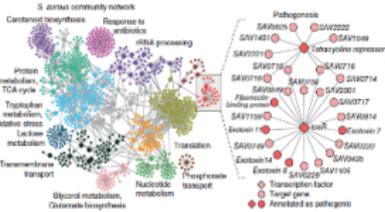
Accelerating Random Forests in Scikit-Learn

Gilles Louppe

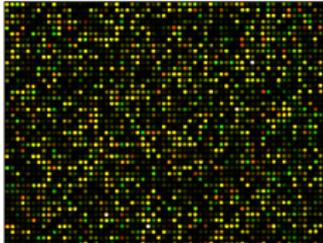
Université de Liège, Belgium

August 29, 2014

Motivation



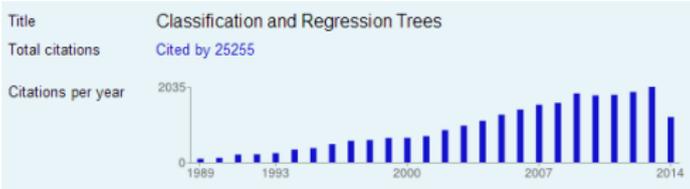
kaggle



Google



... and many more applications!



About

Scikit-Learn

- **Machine learning** library for Python
- Classical and **well-established algorithms**
- Emphasis on **code quality** and **usability**



Myself

- @glouppe
- PhD student (Liège, Belgium)
- Core developer on Scikit-Learn since 2011
Chief tree hugger

Outline

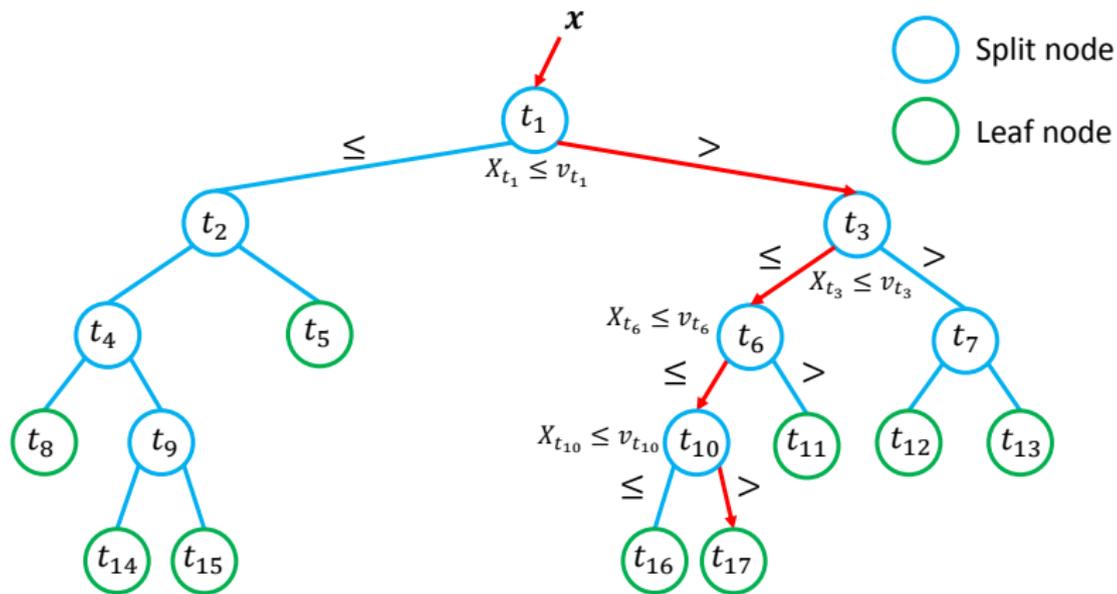
- 1 Basics
- 2 Scikit-Learn implementation
- 3 Python improvements

Machine Learning 101

- Data comes as...
 - A set of **samples** $\mathcal{L} = \{(\mathbf{x}_i, y_i) | i = 0, \dots, N - 1\}$, with
 - **Feature vector** $\mathbf{x} \in \mathbb{R}^p$ (= input), and
 - **Response** $y \in \mathbb{R}$ (regression) or $y \in \{0, 1\}$ (classification) (= output)

- Goal is to...
 - Find a function $\hat{y} = \varphi(\mathbf{x})$
 - Such that error $L(y, \hat{y})$ on new (unseen) \mathbf{x} is minimal

Decision Trees

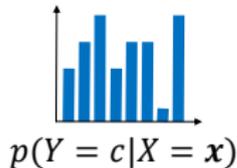


$t \in \varphi$: nodes of the tree φ

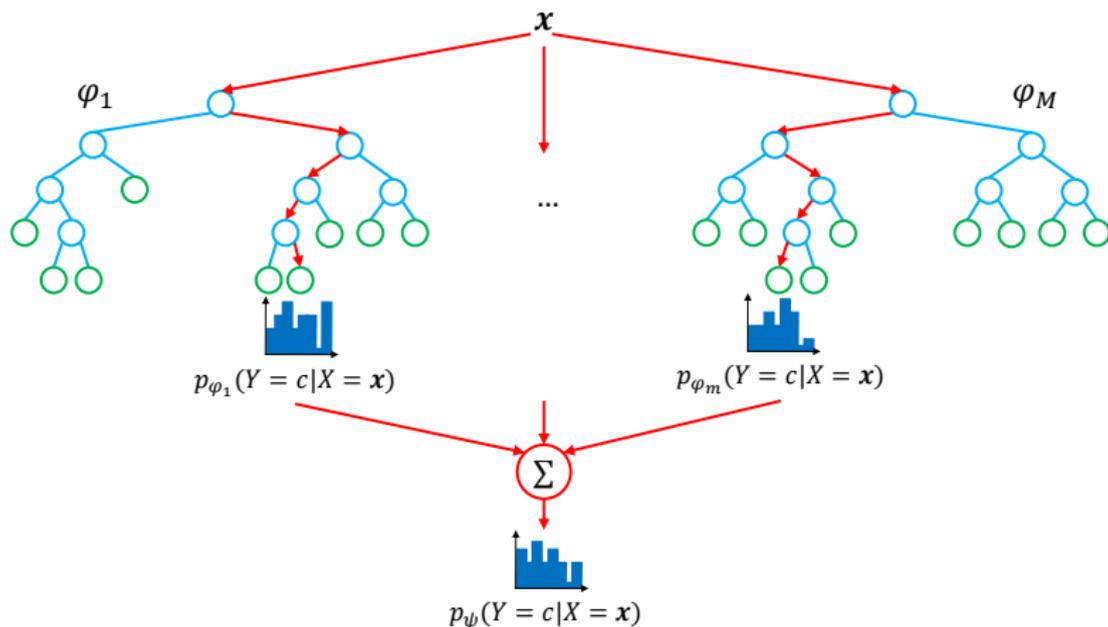
X_t : split variable at t

$v_t \in \mathbb{R}$: split threshold at t

$\varphi(\mathbf{x}) = \arg \max_{c \in \mathcal{Y}} p(Y = c | X = \mathbf{x})$



Random Forests



Ensemble of M randomized decision trees φ_m

$$\psi(\mathbf{x}) = \arg \max_{c \in \mathcal{Y}} \frac{1}{M} \sum_{m=1}^M p_{\varphi_m}(Y = c | X = \mathbf{x})$$

Learning from data

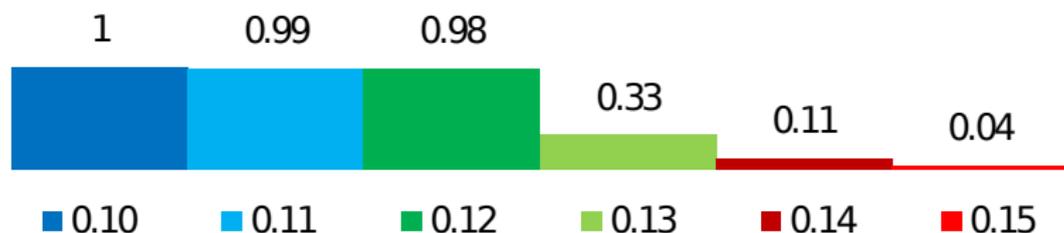
```
function BUILDDECISIONTREE( $\mathcal{L}$ )  
  Create node  $t$   
  if the stopping criterion is met for  $t$  then  
     $\hat{y}_t =$  some constant value  
  else  
    Find the best partition  $\mathcal{L} = \mathcal{L}_L \cup \mathcal{L}_R$   
     $t_L =$  BUILDDECISIONTREE( $\mathcal{L}_L$ )  
     $t_R =$  BUILDDECISIONTREE( $\mathcal{L}_R$ )  
  end if  
  return  $t$   
end function
```

Outline

- ① Basics
- ② Scikit-Learn implementation
- ③ Python improvements

History

Time for building a Random Forest (relative to version 0.10)



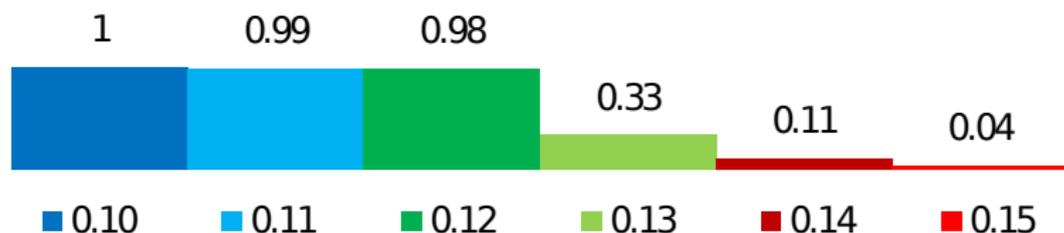
0.10 : January 2012

- First sketch at `sklearn.tree` and `sklearn.ensemble`
- Random Forests and Extremely Randomized Trees modules



History

Time for building a Random Forest (relative to version 0.10)



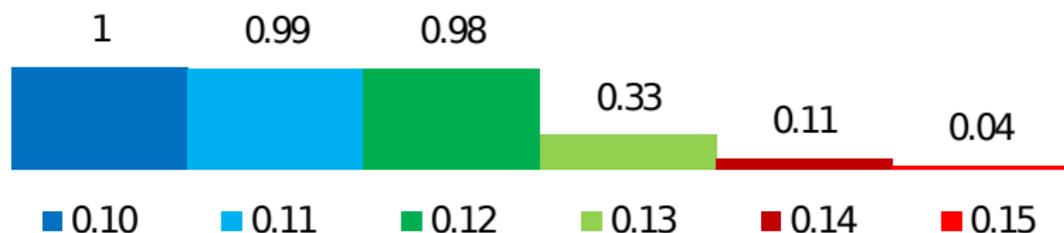
0.11 : May 2012

- Gradient Boosted Regression Trees module
- Out-of-bag estimates in Random Forests



History

Time for building a Random Forest (relative to version 0.10)



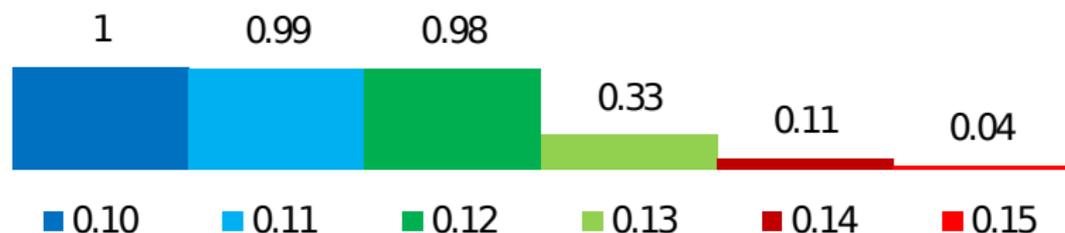
0.12 : October 2012

- Multi-output decision trees



History

Time for building a Random Forest (relative to version 0.10)



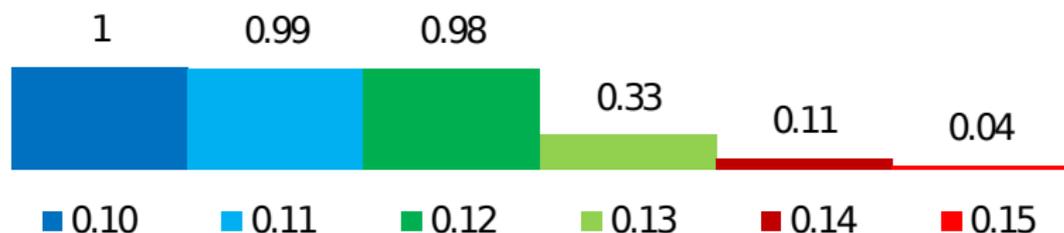
0.13 : February 2013

- Speed improvements
 - Rewriting from Python to Cython
- Support of sample weights
- Totally randomized trees embedding



History

Time for building a Random Forest (relative to version 0.10)



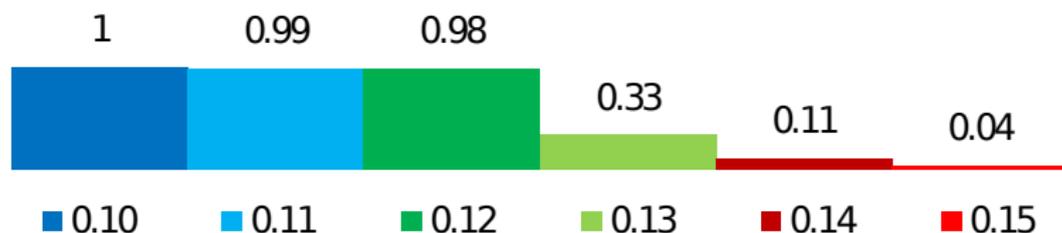
0.14 : August 2013

- Complete rewrite of `sklearn.tree`
 - Refactoring
 - Cython enhancements
- AdaBoost module



History

Time for building a Random Forest (relative to version 0.10)



0.15 : August 2014

- Further speed and memory improvements
 - Better algorithms
 - Cython enhancements
- Better parallelism
- Bagging module



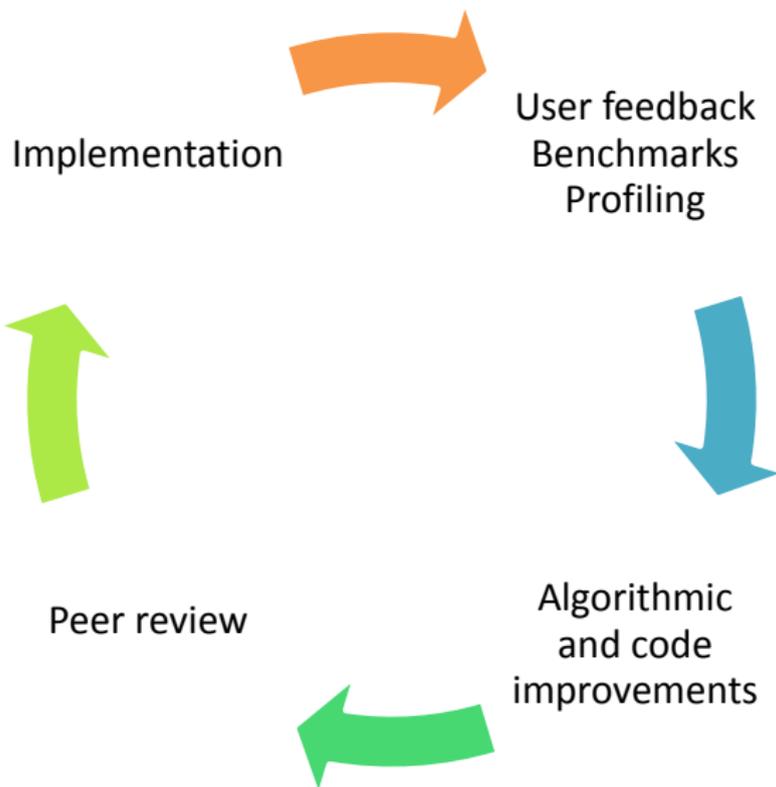
Implementation overview

- Modular implementation, designed with a strict **separation of concerns**
 - Builders : for building and connecting nodes into a tree
 - Splitters : for finding a split
 - Criteria : for evaluating the goodness of a split
 - Tree : dedicated data structure
- Efficient **algorithmic formulation** [See [Louppe, 2014](#)]
Tips. *An efficient algorithm is better than a bad one, even if the implementation of the latter is strongly optimized.*
 - Dedicated sorting procedure
 - Efficient evaluation of consecutive splits
- **Close to the metal**, carefully coded, implementation
2300+ lines of Python, 3000+ lines of Cython, 1700+ lines of tests

But we kept it stupid simple for users!

```
clf = RandomForestClassifier()  
clf.fit(X_train, y_train)  
y_pred = clf.predict(X_test)
```

Development cycle



Continuous benchmarks

- During code review, changes in the tree codebase are monitored with **benchmarks**.
- **Ensure performance** and code quality.
- **Avoid code complexification** if it is not worth it.



ogrisel commented on 3 Feb

@arjoly does you last bugfix has an impact on the outcome of the regression benchmark?

Outline

- ① Basics
- ② Scikit-Learn implementation
- ③ Python improvements

Disclaimer. Early optimization is the root of all evil.

(This took us several *years* to get it right.)

Profiling

Use profiling tools for **identifying bottlenecks**.

```
In [1]: clf = DecisionTreeClassifier()
```

```
# Timer
```

```
In [2]: %timeit clf.fit(X, y)
```

```
1000 loops, best of 3: 394  $\mu$ s per loop
```

```
# memory_profiler
```

```
In [3]: %memit clf.fit(X, y)
```

```
peak memory: 48.98 MiB, increment: 0.00 MiB
```

```
# cProfile
```

```
In [4]: %prun clf.fit(X, y)
```

| ncalls | tottime | percall | cumtime | percall | filename:lineno(function) |
|--------|---------|---------|---------|---------|---------------------------------------|
| 390/32 | 0.003 | 0.000 | 0.004 | 0.000 | _tree.pyx:1257(introsort) |
| 4719 | 0.001 | 0.000 | 0.001 | 0.000 | _tree.pyx:1229(swap) |
| 8 | 0.001 | 0.000 | 0.006 | 0.001 | _tree.pyx:1041(node_split) |
| 405 | 0.000 | 0.000 | 0.000 | 0.000 | _tree.pyx:123(impurity_improvement) |
| 1 | 0.000 | 0.000 | 0.007 | 0.007 | tree.py:93(fit) |
| 2 | 0.000 | 0.000 | 0.000 | 0.000 | {method 'argsort' of 'numpy.ndarray'} |
| 405 | 0.000 | 0.000 | 0.000 | 0.000 | _tree.pyx:294(update) |

```
...
```

Profiling (cont.)

```
# line_profiler
```

```
In [5]: %lprun -f DecisionTreeClassifier.fit clf.fit(X, y)
```

```
Line      % Time      Line Contents
```

```
=====
```

```
...
```

```
256      4.5      self.tree_ = Tree(self.n_features_, self.n_classes_, self.n
```

```
257
```

```
258          # Use BestFirst if max_leaf_nodes given; use DepthFirst othe
```

```
259      0.4      if max_leaf_nodes < 0:
```

```
260      0.5          builder = DepthFirstTreeBuilder(splitter, min_samples_s
```

```
261      0.6          self.min_samples_leaf, m
```

```
262      else:
```

```
263          builder = BestFirstTreeBuilder(splitter, min_samples_sp
```

```
264          self.min_samples_leaf, m
```

```
265          max_leaf_nodes)
```

```
266
```

```
267      22.4      builder.build(self.tree_, X, y, sample_weight)
```

```
...
```


Python is slow :-)

- Python overhead is **too large for high-performance code**.
- Whenever feasible, **use high-level operations** (e.g., SciPy or NumPy operations on arrays) to **limit Python calls** and rely on highly-optimized code.

```
def dot_python(a, b):          # Pure Python (2.09 ms)
    s = 0
    for i in range(a.shape[0]):
        s += a[i] * b[i]
    return s
```

```
np.dot(a, b)                   # NumPy (5.97 us)
```

- Otherwise (and only then!), **write compiled C extensions** (e.g., using Cython) for critical parts.

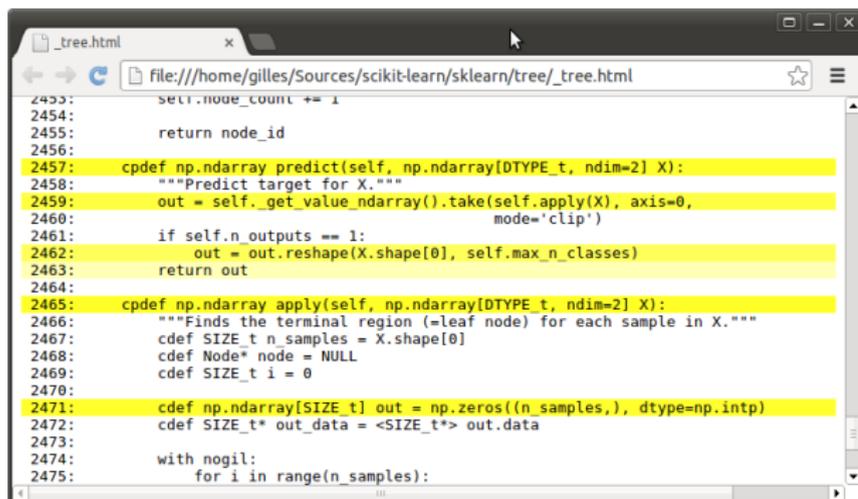
```
cpdef dot_mv(double[:,1] a, double[:,1] b): # Cython (7.06 us)
    cdef double s = 0
    cdef int i
    for i in range(a.shape[0]):
        s += a[i] * b[i]
    return s
```

Stay close to the metal

- Use the right data type for the right operation.
- Avoid repeated access (if at all) to Python objects.
 - Trees are represented by single arrays.

Tips. *In Cython, check for hidden Python overhead. Limit yellow lines as much as possible!*

```
cython -a _tree.pyx
```



```
2453:         self.node_count += 1
2454:
2455:         return node_id
2456:
2457:     cpdef np.ndarray predict(self, np.ndarray[DTYPE_t, ndim=2] X):
2458:         """Predict target for X."""
2459:         out = self.get_value_ndarray().take(self.apply(X), axis=0,
2460:                                             mode='clip')
2461:         if self.n_outputs == 1:
2462:             out = out.reshape(X.shape[0], self.max_n_classes)
2463:         return out
2464:
2465:     cpdef np.ndarray apply(self, np.ndarray[DTYPE_t, ndim=2] X):
2466:         """Finds the terminal region (=leaf node) for each sample in X."""
2467:         cdef SIZE_t n_samples = X.shape[0]
2468:         cdef Node* node = NULL
2469:         cdef SIZE_t i = 0
2470:
2471:         cdef np.ndarray[SIZE_t] out = np.zeros((n_samples,), dtype=np.intp)
2472:         cdef SIZE_t* out_data = <SIZE_t*> out.data
2473:
2474:         with nogil:
2475:             for i in range(n_samples):
```

Stay close to the metal (cont.)

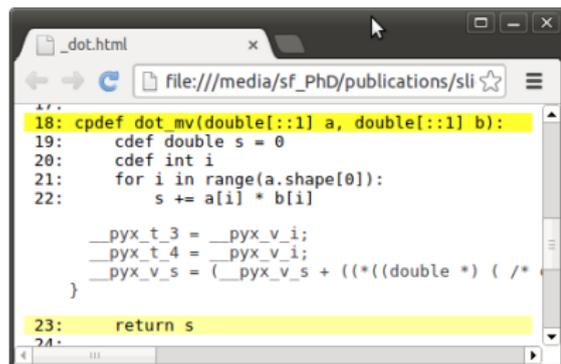
- Take care of **data locality and contiguity**.
 - Make data contiguous to leverage CPU prefetching and cache mechanisms.
 - Access data in the same way it is stored in memory.
Tips. *If accessing values row-wise (resp. column-wise), make sure the array is C-ordered (resp. Fortran-ordered).*

```
cdef int[:, :1] X = np.asfortranarray(X, dtype=np.int)
cdef int i, j = 42
cdef s = 0
for i in range(...):
    s += X[i, j] # Fast
    s += X[j, i] # Slow
```

- If not feasible, use pre-buffering.

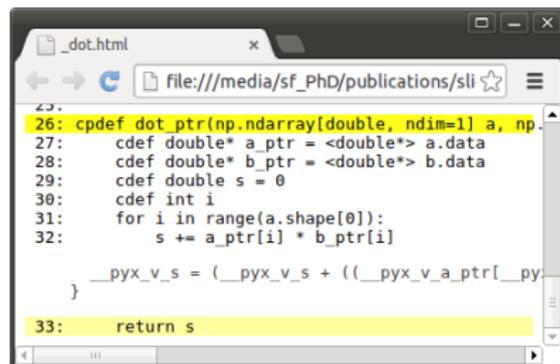
Stay close to the metal (cont.)

- Arrays accessed with **bare pointers** remain the fastest solution we have found (sadly).
 - NumPy arrays or MemoryViews are slightly slower
 - Require some **pointer kung-fu**



```
18: cpdef dot_mv(double[:,1] a, double[:,1] b):
19:     cdef double s = 0
20:     cdef int i
21:     for i in range(a.shape[0]):
22:         s += a[i] * b[i]
23:
24:     return s
```

7.06 us



```
26: cpdef dot_ptr(np.ndarray[double, ndim=1] a, np.
27:     cdef double* a_ptr = <double*> a.data
28:     cdef double* b_ptr = <double*> b.data
29:     cdef double s = 0
30:     cdef int i
31:     for i in range(a.shape[0]):
32:         s += a_ptr[i] * b_ptr[i]
33:
34:     return s
```

6.35 us

Efficient parallelism in Python is possible!



Andreas Mueller
@t3kclt

Just a quick reminder what sklearn random forests look like on EC2. want?
aws.amazon.com/grants/

Reply Retweet Favorited More

```
1 [|||||100.0%]
2 [|||||100.0%]
3 [|||||100.0%]
4 [|||||100.0%]
5 [|||||100.0%]
6 [|||||100.0%]
7 [|||||100.0%]
8 [|||||100.0%]
9 [|||||100.0%]
10 [|||||100.0%]
11 [|||||100.0%]
12 [|||||100.0%]
13 [|||||100.0%]
14 [|||||100.0%]
15 [|||||100.0%]
16 [|||||100.0%]
17 [|||||100.0%]
18 [|||||100.0%]
19 [|||||100.0%]
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21 [|||||100.0%]
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25 [|||||100.0%]
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27 [|||||100.0%]
28 [|||||100.0%]
29 [|||||100.0%]
30 [|||||100.0%]
31 [|||||100.0%]
32 [|||||100.0%]
Mem[||||| 23164/245759M]
Swp[||||| 0/0MB]
```

Joblib

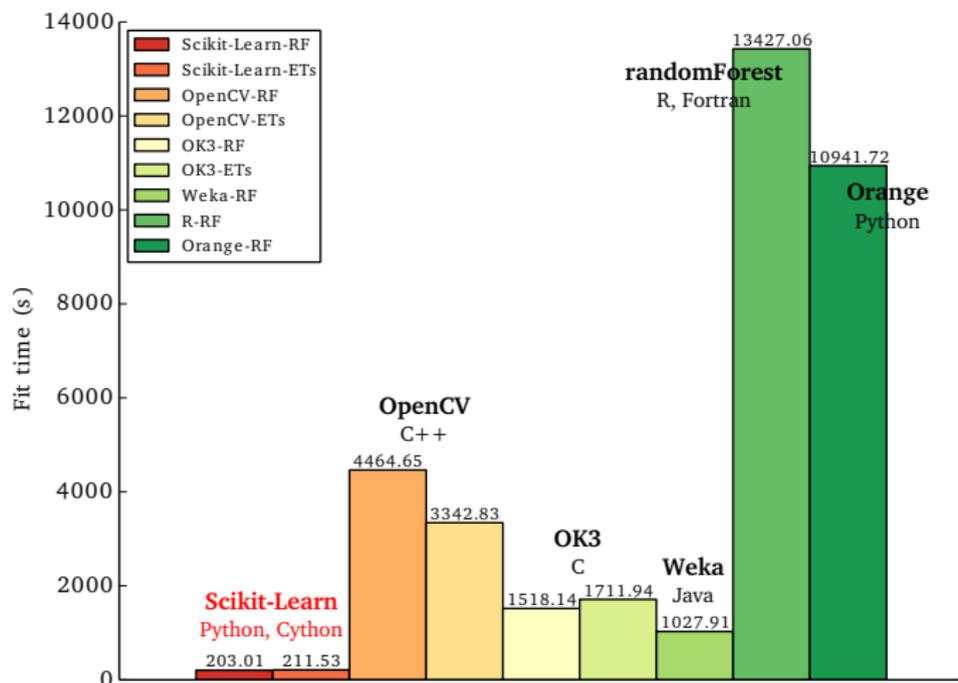
Scikit-Learn implementation of Random Forests relies on joblib for **building trees in parallel**.

- Multi-processing backend
- Multi-threading backend
 - Require C extensions to be GIL-free
 - Tips.** Use *nogil* declarations whenever possible.
 - Avoid memory duplication

```
trees = Parallel(n_jobs=self.n_jobs)(
    delayed(_parallel_build_trees)(
        tree, X, y, ...)
    for i, tree in enumerate(trees))
```

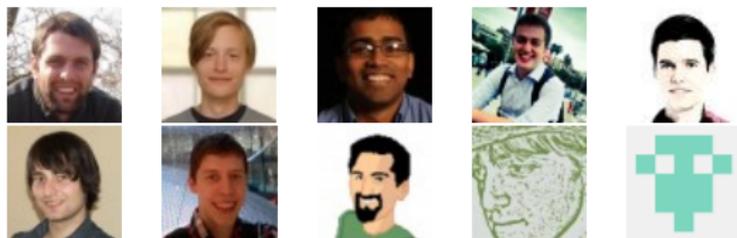
A winning strategy

Scikit-Learn implementation proves to be **one of the fastest** among all libraries and programming languages.



Summary

- The open source development cycle really empowered the Scikit-Learn implementation of Random Forests.



- Combine algorithmic improvements with code optimization.
- Make use of profiling tools to identify bottlenecks.
- Optimize only critical code !