A relaxation scheme to combine Phasor-Mode and Electromagnetic Transients Simulations

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Abstract—This paper deals with a new scheme for coupling phasor-mode and electromagnetic transients simulations. In each simulation, an iteratively updated linear equivalent is used to represent the effect of the subsystem treated by the other simulation. Time interpolation and phasor extraction methods adapted to this scheme are presented and compared to existing methods. Finally, simulation results obtained with a 74-bus test system are reported.

Index Terms—hybrid simulations, multirate techniques, phasor approximation, electromagnetic transients, boundary conditions.

I. INTRODUCTION

A. Overall objective of the work

Coupled simulations of power systems, combining Phasor-Mode (PM) and ElectroMagnetic Transients (EMT) models, aim at taking advantage of the high speed of PM simulations and the high accuracy of EMT simulations. To this purpose, the EMT model is simulated with a “small” time step size $h$ and the PM model with a “large” time step size $H$. This feature makes the combined PM-EMT simulation a particular case of multirate methods. A typical example of application is the detailed simulation of an unbalanced fault using the EMT model in a subsystem surrounding the fault location, and the PM model for the rest of the power system.

The first related work can be traced back to 1981 [1]. Since then, a significant number of advances have taken place, as testified by the state-of-the-art report in [2]. However, there is still room for improvement in coupled PM-EMT simulations, to reach the targeted speed-accuracy compromise. Some authors even challenge the theoretical basis supporting this type of hybrid simulation [3].

This paper revisits and improves the techniques to represent one subsystem into the simulation of the other, and extract the relevant signals from one simulation, for use in the other.

B. Simplified representation of EMT and PM subsystems

Figure 1 illustrates two issues addressed in this paper. First, the coupling of PM and EMT simulations implies modelling the PM subsystem’s response when performing the EMT simulation, and conversely. This requires choosing a simplified representation of the EMT subsystem, to be used in PM simulation, and a simplified representation of the PM subsystem, for use in the EMT simulation. Second, this work considers the possibility to iterate between both models, at each discrete time of the simulation, until satisfactory convergence is reached and simulation proceeds with the next discrete time. The choice of the simplified representations of, respectively, the EMT and the PM subsystem impacts the speed of convergence of this relaxation process.

For the sake of simplicity, this paper focuses on the case where the PM and EMT subsystems are connected to each other through a single boundary bus. Three simple models come to mind for the representation of either of the two systems, when simulating the other: (i) an ideal voltage source attached to the boundary bus; (ii) an ideal current source injecting into the boundary bus, or (iii) a linear relation between the boundary voltage and current, in the form of a Thévenin (or Norton) equivalent.

Figure 2 summarizes the combinations of representations documented in the literature.

In Ref. [4], it was chosen to use an ideal current source to represent the EMT subsystem in the PM model, and an ideal voltage source to represent the PM subsystem in the EMT model, as shown in Fig. 2.a. While this configuration offers the advantage of simplicity, it requires to have, at the boundary, three-phase voltages and currents with negligible imbalance.
and distortion since this is the usual assumption taken in phasor-mode simulation. In turn, this requires to place the boundary far enough from the location of the disturbance, i.e. to have a large enough EMT subsystem. With the increasing computational power available nowadays, it should generally not be a problem to increase the size of the EMT subsystem until fundamental-frequency positive-sequence currents are observed at the boundary with the PM subsystem. The approach used in [5] is shown in Fig. 2.b. While still relying on a current source to represent the EMT subsystem, it uses a Frequency Dependent Network Equivalent (FDNE) admittance in parallel with an ideal current source to represent the PM subsystem. This more accurate representation, valid over a wide frequency range, allows putting the boundary closer to the disturbance location without degrading accuracy.

The representation considered in this paper resorts to the use of both a Norton and a Thévenin equivalent, as shown in Fig. 2.c. Note that choosing between a Norton or a Thévenin representation is free; the shown combination is convenient for incorporation in the usual PM and EMT models. Apparently, this approach can be traced back to Ref. [6] but, to the authors’ knowledge, it has not been used in any recent, published work. The reason may be that researchers oriented their efforts towards improving the representation of the PM subsystem in the EMT simulation in order for the boundary to be located closer to the disturbance without losing accuracy.

It must be emphasized that the impedance, admittance, voltage and current parameters involved in the equivalents are updated during the dynamic simulation, while iterating between the PM and EMT simulations. Thus, the method differs from merely using a fixed Thévenin or Norton equivalent to represent the other subsystem. More details about this relaxation procedure are given in Section II.

C. Information exchanged by PM and EMT simulations

The EMT and PM simulations must receive information compatible with their modelling assumptions. This requires performing time interpolation and phasor extraction, respectively, as shown in Fig. 3.

Time interpolation is needed to convert the “slowly” varying voltage and current phasors, provided by the PM simulation, into voltage and current sources evolving sinusoidally with time, at the nominal fundamental frequency, but with “slowly varying” magnitudes and phase angles. While a simple linear time interpolation can be used for that purpose, there are some problematic situations, such as the application of a fault close to the boundary between the EMT and PM subsystems. This and other issues are addressed in Section III.

Phasor extraction, used for passing information from EMT to PM simulation, consists in extracting the positive-sequence phasors from three-phase, possibly distorted and unbalanced, bus voltage and branch current signals sampled at period $h$. In the context of hybrid simulations, a phasor extraction method was early proposed in [1], using RMS approximations to obtain power and a Fast Fourier Transform (FFT) to determine the fundamental voltage magnitude. The drawback of FFT and similar approaches is that they introduce a time delay. An improved method has been proposed in [7], relying on instantaneous values of real and reactive power. This method resorts to energy balance to extract the current phasor.

In contrast, the method detailed in Section IV, which extends the one proposed in [4], resorts to projections on rotating axes to extract voltage or current phasors. To the best of the authors’ knowledge, this procedure has not been considered elsewhere, which might explain why the representation shown in Fig. 2.c has not been used either.

II. RELAXATION PROCESS BETWEEN EMT AND PM SIMULATIONS

The relaxation scheme sketched in Fig. 1 is shown in greater detail in Fig. 4. The two simulations exchange phasors. This assumes that the boundary is far enough from the disturbance, so that phase imbalances, aperiodic components and harmonics can be neglected, as discussed in the Introduction.

The focus is on iterations performed when passing from time $t$ to time $t + H$, i.e. over one step of the PM simulation. At the $k$-th iteration, given the estimates $(V_k^k, I_k^k)$ of the boundary voltage and current phasors at $t + H$, the PM simulation performs time interpolation and phasor extraction.
simulation determines the evolution of the PM subsystem over a single step $H$, with the EMT subsystem replaced by a Norton equivalent. The latter involves an admittance $y_{\text{emt}}$ and the Norton current:

$$I_{\text{na}} = \bar{I}^k + y_{\text{emt}} \bar{V}^k$$  \hspace{1cm} (1)

updated with the latest available boundary voltage and current. The PM simulation yields the new estimates $\bar{V}^{k+\frac{1}{2}}$, $\bar{I}^{k+1}$ of the boundary voltage and current, where the superscript $k+\frac{1}{2}$ indicates that half of the iteration has been performed.

In a case a fault is simulated (taking place in the EMT subsystem), $y_{\text{emt}}$ can be computed beforehand for the pre-fault, during-fault and post-fault situations. Alternatively, it could be estimated numerically, from the previous values of the boundary voltage and current.

Given the updated values $(\bar{V}^{k+\frac{1}{2}}, \bar{I}^{k+1})$ of the boundary voltage and current phasors at time $t+H$, the EMT simulation provides the evolution of the EMT subsystem from $t$ to $t+H$, using small time steps $h$ with the PM subsystem replaced by a Thévenin equivalent. The latter involves an impedance $\tilde{z}_{\text{pm}}$ (also determined beforehand or estimated during the iterations), and the Thévenin voltage:

$$E_{\text{th}} = \bar{V}^{k+\frac{1}{2}} - \tilde{z}_{\text{pm}} \bar{I}^{k+\frac{1}{2}}$$  \hspace{1cm} (2)

updated with the latest available boundary voltage and current. In the EMT simulation, this Thévenin equivalent is replaced by differential equations as the rest of the EMT model. This simulation yields the new estimates $(\bar{V}^{k+1}, \bar{I}^{k+1})$.

Convergence is checked by comparing $||\bar{V}^{k+1} - \bar{V}^k||$ and $||\bar{I}^{k+1} - \bar{I}^k||$ to some tolerances. If the latter are satisfied, the simulation proceeds with the next time interval $[t+H, t+2H]$. Otherwise, an additional relaxation iteration is performed.

Let $\bar{V}_{\text{pm}}$ and $\bar{I}_{\text{pm}}$ (resp. $\bar{V}_{\text{emt}}$ and $\bar{I}_{\text{emt}}$) be the values of the boundary voltage and current, provided by PM (resp. EMT) simulation, once convergence has taken place. At convergence, the circuits in Fig. 4 operate as shown in Fig. 5, where intermediate values have been replaced by final ones.

The following equations are easily derived from Fig. 5:

$$I_{\text{pm}} = I_{\text{emt}} + y_{\text{emt}} \bar{V}_{\text{emt}} - y_{\text{emt}} \bar{V}_{\text{pm}}$$  \hspace{1cm} (3)

$$\bar{V}_{\text{emt}} = \bar{V}_{\text{pm}} - \tilde{z}_{\text{pm}} I_{\text{pm}} + \tilde{z}_{\text{pm}} I_{\text{emt}}$$  \hspace{1cm} (4)

Introducing (4) into (3) and rearranging the terms yields:

$$(1+\tilde{z}_{\text{pm}} y_{\text{emt}}) I_{\text{pm}} = (1+\tilde{z}_{\text{pm}} y_{\text{emt}}) I_{\text{emt}} \Leftrightarrow I_{\text{pm}} = I_{\text{emt}}$$  \hspace{1cm} (5)

where it has been assumed that the parenthesis is nonzero. Hence, Eq. (3) becomes:

$$\bar{V}_{\text{pm}} = \bar{V}_{\text{emt}}$$  \hspace{1cm} (6)

From Eqs. (5) and (6) it is concluded that, whatever the values of $y_{\text{emt}}$ and $\tilde{z}_{\text{pm}}$, the converged solution reached by the PM and EMT simulations is such that the boundary bus has the same voltage in both of them, and the current injected by one is the current received by the other. Thus, there is a perfect match between the PM and EMT simulations. On the other hand, the values of $y_{\text{emt}}$ and $\tilde{z}_{\text{pm}}$ influence the convergence of the relaxation process. For instance, if $y_{\text{emt}}$ was set to zero, at the $k$-th iteration the PM simulation would be performed with the boundary current set to $I^k$; hence, the current change induced by the change of voltage $\bar{V}^k$ would be accounted for at the $(k+1)$-th iteration only. The Norton equivalent (with $y_{\text{emt}} \neq 0$) yields a linear approximation of that variation of the current with the voltage. Similar considerations apply to the Thévenin equivalent and $\tilde{z}_{\text{pm}}$.

One can reasonably assume that, the more accurate the linear approximation, the faster the convergence of the relaxation process. This assertion is supported by numerical results in [8], where the rate of convergence of the relaxation scheme is assessed under the assumption that the EMT and PM subsystem behave linearly.

The PM and EMT simulations match for any choice of $y_{\text{emt}}$ and $\tilde{z}_{\text{pm}}$, provided the PM and EMT models are iterated until convergence. The same does not hold true if a single iteration is performed, i.e. a single PM simulation followed by a single EMT simulation when passing from $t$ to $t+H$. This case is of interest when hybrid simulation is used to test “hardware in the loop” [9]. In that application, $y_{\text{emt}}$ and $\tilde{z}_{\text{pm}}$ should be as accurate as possible to preserve the solution accuracy.

Figure 4. Relaxation process with iteratively updated equivalents to account for one subsystem when simulating the other subsystem.

Figure 5. Situation reached when the relaxation process has converged.
III. FROM PM TO EMT: TIME INTERPOLATION

Consider an EMT simulation over the time interval $[t \, t + H]$. Thus, the values of all states at time $t$ have been computed and accepted; the ones at time $t + H$ are being computed. The last PM simulation provides the estimates $V^{k+\frac{1}{2}}(t + H)$ and $I^{k+\frac{1}{2}}(t + H)$ of the boundary voltage and current (see Fig. 4).

The corresponding estimated Thévenin voltage is given by:

$$E_{th}(t + H) = V^{k+\frac{1}{2}}(t + H) - \hat{z}_{pm} I^{k+\frac{1}{2}}(t + H)$$  \hspace{1cm} (7)

A linear interpolation of respectively the magnitude and the phase angle of $E_{th}$ is considered, as shown in Fig. 6. For simplicity of presentation, $H$ is assumed to be a multiple of $h$, i.e. $H = \rho h$ where $\rho$ is an integer. Thus, at the discrete time $t + nh$ ($n = 0, \ldots, \rho$), the interpolated Thévenin voltage magnitude is given by:

$$E(t + nh) = ||E_{th}(t)|| + \frac{n}{\rho} \left( ||E_{th}(t + H)|| - ||E_{th}(t)|| \right)$$  \hspace{1cm} (8)

where $|| \|$ denotes the magnitude. The interpolated phase angle is given by:

$$\phi(t + nh) = \angle E_{th}(t) + \frac{n}{\rho} \left( \angle E_{th}(t + H) - \angle E_{th}(t) \right)$$  \hspace{1cm} (9)

Considering phase $a$, for instance, the discretized Thévenin voltage is obtained as ($n = 0, \ldots, \rho$):

$$e_a(t + nh) = \sqrt{2} E(t + nh) \sin (\omega(t + nh) + \phi(t + nh))$$  \hspace{1cm} (10)

where $\omega$ is the nominal angular speed of the system.

The simulation of large disturbances, typically faults, in the EMT subsystem calls for some comments. In such a case, the phasor of the voltage at the boundary is expected to undergo a fast and significant change (although this is attenuated by setting the boundary with the PM subsystem far enough the fault location). An example is provided in Fig. 7 showing the evolution of a boundary bus voltage in response to a three-cycle fault applied at $t = 20$ ms and cleared at $t = 80$ ms.

There are two issues: accuracy and convergence of the relaxation process.

For what concerns accuracy, the use of a Thévenin equivalent reproduces the sharp voltage drop in the EMT simulation. As regards convergence, the advantage of approximating the response of the PM subsystem by a Thévenin equivalent is worth being repeated. By so doing, the abrupt change in voltage is already rendered by the first EMT simulation, through the voltage drop in the Thévenin impedance $\hat{z}_{pm}$. This feature would not be obtained with a pure voltage source as shown in Fig. 2.a (upper right diagram). The problem was reported in [10], where it is suggested to use the voltage $V^{k+\frac{1}{2}}(t + H)$ over the whole time interval $H$ instead of interpolation. On the contrary, the use of a Thévenin equivalent preserves the convergence of the relaxation process. For instance, in the case of Fig. 7, it was possible to use steps of 20 ms in the PM simulation, as shown by the curve labelled “PM” in the figure.

IV. FROM EMT TO PM: PHASOR EXTRACTION

As shown in Fig. 4, the EMT simulation provides updated estimates $(V^{k+1}, I^{k+1})$ of the boundary voltage and current. The positive-sequence phasor of either the current or the voltage is extracted. Assuming arbitrarily that it is the current, the boundary voltage phasor is easily obtained from Fig. 4 as:

$$V^{k+1} = V^{k+\frac{1}{2}} + \hat{z}_{pm}(I^{k+1} - I^{k+\frac{1}{2}})$$  \hspace{1cm} (11)

The phasor extraction consists of two steps: (i) projection on a rotating reference frame, using the method initially proposed in [4], and (ii) post-processing using a low-pass filter, which improves that method.

A. Projection on a rotating reference frame

The amplitude and the phase angle of the positive-sequence component of the currents are computed from the three time-varying current waveforms by projecting the latter on $(x, y)$ reference axes, using a Park-type transform. This technique, inspired of the principle of Phase Locked Loop (PLL) systems [11], is free from any delay associated with processing of the current waveforms.

More precisely, $(x, y)$ are the orthogonal axes used in the PM simulation to project the rotating vectors associated with quasi-sinusoidal variables, and obtain their corresponding rectangular components. As shown in Fig. 8, these axes rotate at the nominal angular speed $\omega$ and, at time $t$, the $x$ axis is at an angular position:

$$\theta = \omega t + \theta_0 = \omega t$$  \hspace{1cm} (12)
with respect to a fixed reference, where the position of the x-axis at $t = 0$ has been arbitrarily set to zero.

The current waveforms to process can be written as:

$$i_{abc} = \begin{bmatrix} i_a \\ i_b \\ i_c \end{bmatrix} = \begin{bmatrix} \sqrt{2}I_a \cos(\omega t + \psi_a) + \epsilon_a \\ \sqrt{2}I_a \cos(\omega t + \psi_a - \frac{2\pi}{3}) + \epsilon_b \\ \sqrt{2}I_a \cos(\omega t + \psi_a - \frac{4\pi}{3}) + \epsilon_c \end{bmatrix}$$

(13)

where $\epsilon_a$, $\epsilon_b$ and $\epsilon_c$ are noise terms accounting for deviations with respect to three-phase, balanced, positive-sequence components. The current in $i_{abc}$ are projected on the above mentioned axes by applying the linear transform [12]:

$$i_{0xy} = Ti_{abc}$$

(14)

with:

$$T = \frac{\sqrt{2}}{3} \begin{bmatrix} 1/\sqrt{2} & 1/\sqrt{2} & 1/\sqrt{2} \\ \cos(\theta) & \cos(\theta - \frac{2\pi}{3}) & \cos(\theta - \frac{4\pi}{3}) \\ -\sin(\theta) & -\sin(\theta - \frac{2\pi}{3}) & -\sin(\theta - \frac{4\pi}{3}) \end{bmatrix}$$

(15)

In the ideal case where the three currents make up a balanced, positive sequence, i.e. $\epsilon_a = \epsilon_b = \epsilon_c = 0$, the projected currents are easily obtained as:

$$i_{0xy} = \begin{bmatrix} i_0 \\ i_x \\ i_y \end{bmatrix} = \begin{bmatrix} 0 \\ I_a \cos \psi_a \\ I_a \sin \psi_a \end{bmatrix}$$

(16)

The last two components are the projections on x and y of a vector rotating at angular speed $\omega$, representing the current in phase a, having an amplitude $I_a$ and a phase angle $\psi_a$ with respect to the x axis (see Fig. 8). In the PM simulation, $i_x$ and $i_y$ are the rectangular components of the current source shown in the upper block of Fig. 4. Its magnitude and phase angle are easily obtained as:

$$I_a = \sqrt{i_x^2 + i_y^2} \quad \psi_a = \arctan \left( \frac{i_y}{i_x} \right)$$

(17)

At this point of the procedure, Eq. (14) is applied only to the currents $i_{abc}$ obtained at time $t+H$ of the EMT simulation.

### B. Low-pass filtering

Because the effects of a fault located in the EMT subsystem are expected to be still felt at the boundary between PM and EMT subsystems, the boundary current waveforms contain noise terms. The latter stem from aperiodic, negative- and zero-sequence components, and harmonics, whose effect must be filtered out.

While three-phase, balanced, positive-sequence currents are converted into constant $i_x$ and $i_y$, aperiodic (resp. negative-sequence) components present in the phase currents will be transformed into sinusoidal components at nominal (resp. double nominal) frequency. Thus, the filter must:

- preserve the amplitude of components with frequencies between 0 and 5 Hz. This covers the frequency spectrum of concern in PM simulation;
- filter out the fundamental-frequency, double-fundamental-frequency and higher frequency components;
- not affect the phase of the initial signal in the $[0 \, 5]$ Hz frequency range, to avoid introducing any delay between the EMT and PM simulations.

This low-pass numerical filter processes sampled $i_x$ and $i_y$ values obtained by applying (14) at equidistant discrete times in $[t \, t + H]$. The sampling period can be $h$, the time step size used in EMT simulation. Re-sampling may be necessary in case the discrete times of the EMT simulation are not equidistant, for instance because it was necessary to reduce the time step size during the simulation. The width $H$ of the time interval processed by the filter is usually no smaller than one half cycle at the nominal frequency, and most often closer to one cycle. It may be occasionally reduced, for instance at fault application and clearing. The time interval processed by the filter should not become too narrow, for accuracy reasons.

Satisfactory results have been obtained with a Butterworth low-pass filter. For a continuous-time filter, the magnitude-squared transfer function takes on the form:

$$\|H_c(j\omega)\|^2 = \frac{1}{1 + (j\omega/j\omega_c)^{2N}}$$

(18)

where $\omega_c$ is the cutoff frequency. This filter is characterized by a magnitude response maximally flat in the passband. This means that the first $2N-1$ derivatives of the function (18) are zero at $\omega = 0$ [13].

The filter is applied twice, once with increasing and once with decreasing times. Doing so should almost cancel the phase shift introduced by the filter in the pass-band. The order of the filter has been taken to two. However, applying the filter twice yields globally a fourth-order filter, which is expected to give sufficient cut-off band attenuation for most systems.

### V. SIMULATION RESULTS

#### A. Test system and computing tools

Tests have been performed on the 74-bus, 102-branch, 20-machine Nordic test system documented in [14] and shown in Fig. 9. The RAMSES software developed at the University of Liège [15] has been used for PM simulation, while the EMT subsystem solver was implemented in MATLAB, communicating with RAMSES. The results of the PM-EMT simulation have been compared to those given by EMTP-RV applied to
the whole system. The trapezoidal rule was used with a step size $h$ of 50 $\mu$s, and a step size $H$ of 20 ms.

This paper reports on preliminary tests in which only a small EMT subsystem has been considered. It is identified in Fig. 9. It includes six buses, two loads and one synchronous machine represented in detail. It is connected to the rest of the system through a single interface bus (4043).

**B. Case 1: tripping the three-phase load L47**

The 100 MW/44 MVar load connected to bus 47 is tripped at $t = 1$ s. Figure 10 shows the evolution of the voltage magnitude at the boundary bus, given by the proposed method and EMTP-RV, respectively. There is a reasonably good match between both responses.

Figure 11 shows that the same hold true for the rotor speed of machine g15, located in the EMT subsystem. The response shows the effect of speed governors, installed on generators in the NORTH and EQUIV areas, i.e. in the PM subsystem.

Further tests involve comparing the response of components located in the PM subsystem. An example is provided by Fig. 12, showing the rotor speed of g14, located very near the boundary bus. Incidentally, this figure illustrates the advantage of hybrid simulation with respect to replacing the PM subsystem by a simple equivalent. The former, by preserving the topology of the system, not only offers more accuracy but also gives access to individual components for which the phasor approximation is valid.

**C. Case 2: tripping one phase of load L47**

This case involves an unbalanced disturbance in the EMT subsystem, namely the opening of one phase of the load L47. Figure 13 shows the evolution of the rotor speed of g14. As expected, the EMTP-RV simulation reveals the presence of negative-sequence 100-Hz oscillations. The latter are not rendered by the PM-EMT simulation since g14 is located in the PM subsystem, where only the positive sequence is
The method has been illustrated through a sample of results obtained with a 74-bus system including a 6-bus EMT subsystem. A reasonably good match has been found between the proposed method and a full EMTP-RV simulation. More accurate results are expected by slightly enlarging the EMT subsystem, so that the boundary currents better satisfy the positive-sequence assumption underlying the PM simulation.

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VI. CONCLUSION

In this paper, a hybrid simulation combining PM and EMT models has been proposed. The heart of the method is a relaxation process between one “large” time step of the PM simulation and multiple “small” time steps of the EMT simulation.

A key point of this process is the inclusion of iteratively updated Thévenin/Norton equivalents to account for one subsystem when simulating the other subsystem. It has been shown that, whatever the values of the Thévenin impedance or Norton admittance, at convergence, there is a perfect match between both simulations. On the other hand, these parameters impact the convergence of the relaxation process.

The Thévenin voltage passed by the PM to the EMT simulation is linearly interpolated over the small time steps of the EMT simulation. Conversely, boundary voltage and current phasors are extracted from the waveforms of the EMT simulation, and passed to the PM simulation. The phasor extraction involves a projection on a rotating reference frame followed by a low-pass filtering.

Figures 13 and 14 show the speed of machines g14 and g15, respectively, considered. On the other hand, Fig. 14 shows that these oscillations are present in both simulations for g15, located in EMT subsystem.

In this case the responses provided by the EMTP-RV and PM-EMT simulations are in less good agreement. This is due to the boundary (bus 4043) being too close to the disturbance location (bus 47), which causes the boundary phase currents to include other than positive-sequence components. For more accurate results, the EMT subsystem should be somewhat enlarged.