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**Aveiro, Portugal**



**Liège, Belgium**

# **Numerical Simulation of a Conical Shape Made by Single Point Incremental Forming**

## **Adaptive Remeshing technique with solid-shell elements**

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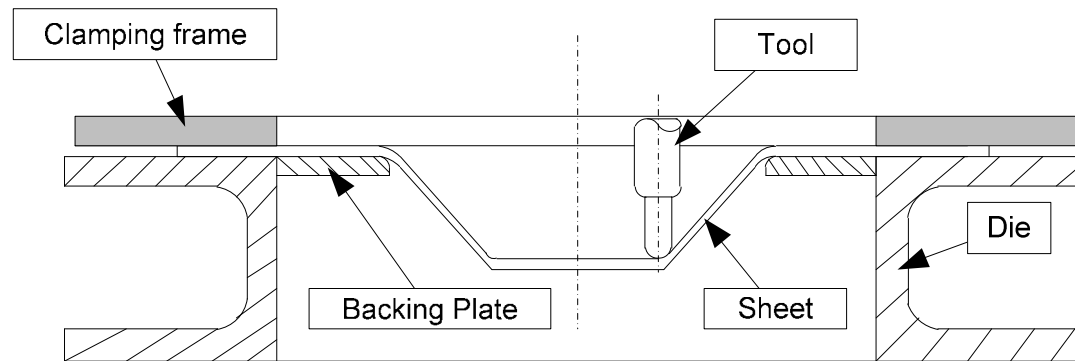
May, 2014



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- Single point incremental forming (SPIF) sheet forming process adapted for rapid prototyping. Neither dies nor punches to form a complex shape.



- Tool guided by numerical control system, forming tool deforms a clamped sheet into its desired shape
- High deformations occur close to the current location of the tool.

## Work Scope

➤ PROBLEM:

- Moving contact between the tool and the sheet
- The nonlinearities



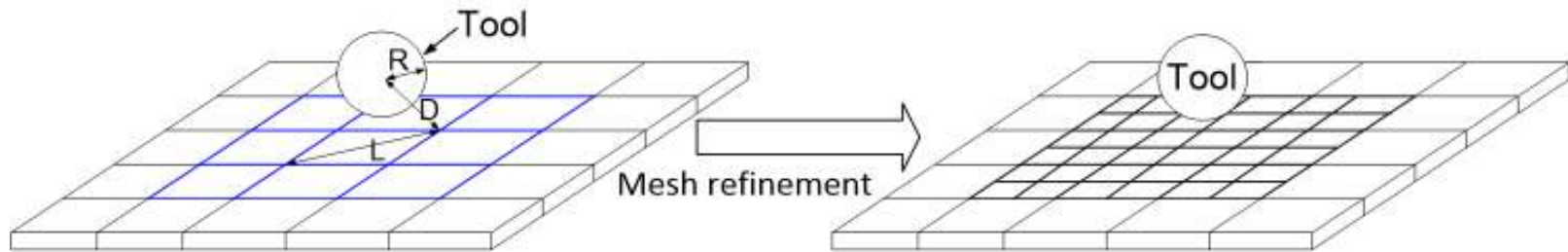
Refined mesh  
near the tool

- First Adaptive SPIF Remeshing : only for Shell finite elements\*.
- Now : extension to 8 nodes 3D finite elements= RESS  
(Reduced Enhanced Solid-Shell).
- RESS + Remeshing ADVANTAGES :
  - Use a 3D constitutive law
  - Prediction of the sheet thickness
  - Decrease the CPU time

\*see Cedric Lequesne *et al.*, Numisheet 2008, Switzerland, September 1 - 5, 2008.

## Refinement / Unrefinement Criterion

- Selection of a neighborhood around the position of the tool center.
- Mesh dynamically refined on the tool vicinity



- Proximity condition :

$$D^2 \leq \alpha (L^2 + R^2)$$

- **D**: minimum distance between the tool center and the four nodes of the contact element
- **L**: length of the longest diagonal of the element
- **R**: radius of the tool
- **$\alpha$** : coefficient adjusting the size of the neighborhood chosen by the user

## Additional Unrefinement Criterion

- To avoid losing geometric accuracy, if the mesh distortion significant keep the refined mesh elements

- Computation of the initial relative position:

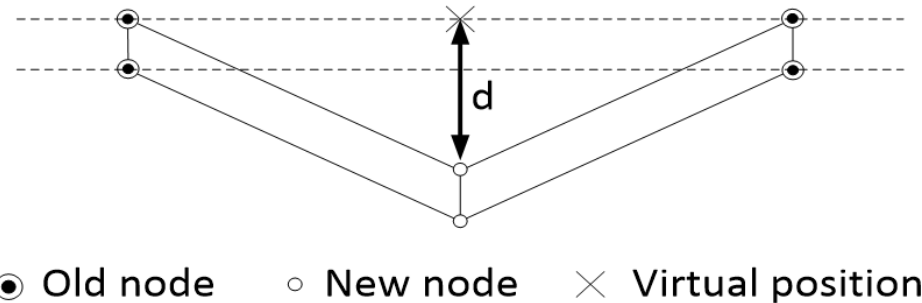
$$\underline{X}_v = \sum_{i=1,4} H_i(\xi, \eta) \underline{X}_i$$

- Computation of the distance

$$d = |\underline{X}_c - \underline{X}_v|$$

- Unrefinement criterion

$$d \leq d_{\max}$$



- $H_i$ : interpolation function

- $X_i$ : nodes positions of the coarse element

- $X_c$ : Current position of the node

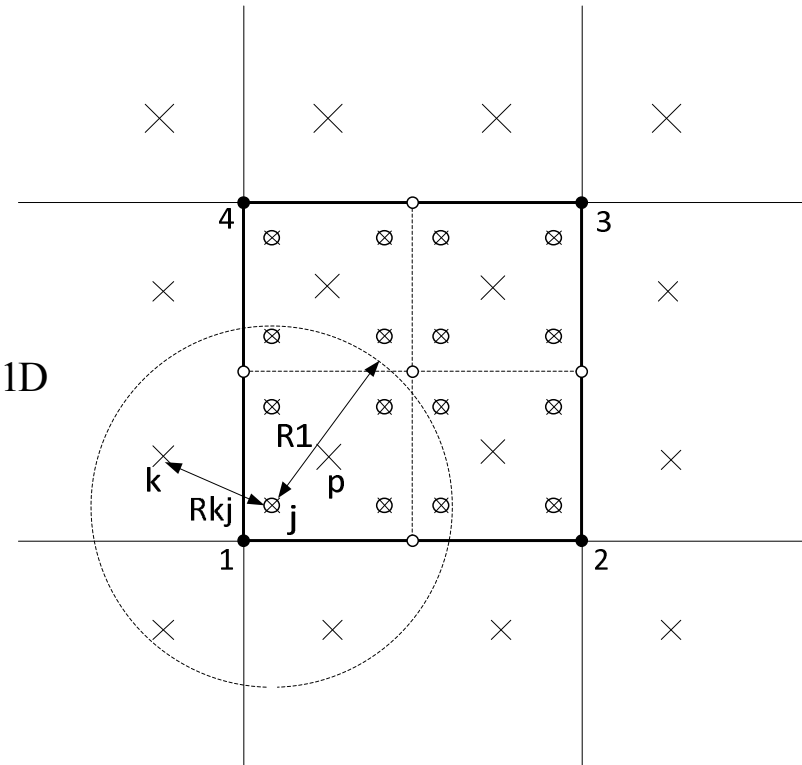
- $d_{\max}$ : maximal admissible distance chosen by the user

## Interpolation of state variables and stress

$$Z_j = \begin{cases} \frac{\sum_k \frac{Z_k}{R_{kJ}^n} + \frac{CZ_p}{R_{pj}^n}}{\sum_k \frac{1}{R_{kJ}^n} + \frac{C}{R_{pj}^n}} & \text{if } R_{pj} > R_{\min} \\ Z_p & \text{if } R_{pj} \leq R_{\min} \end{cases}$$

With :  
 $R_1 = 1.5d$   
 $R_{\min} = 0.0001D$

- **j**: the index of the new integration point
- **k**: the index of the integration point of another element in the sphere
- **p**: is the index of the closest integration point
- **Z<sub>j</sub>**: stress or state variables components at the integration point j
- **R<sub>kj</sub>**: distance between the integration point k and j

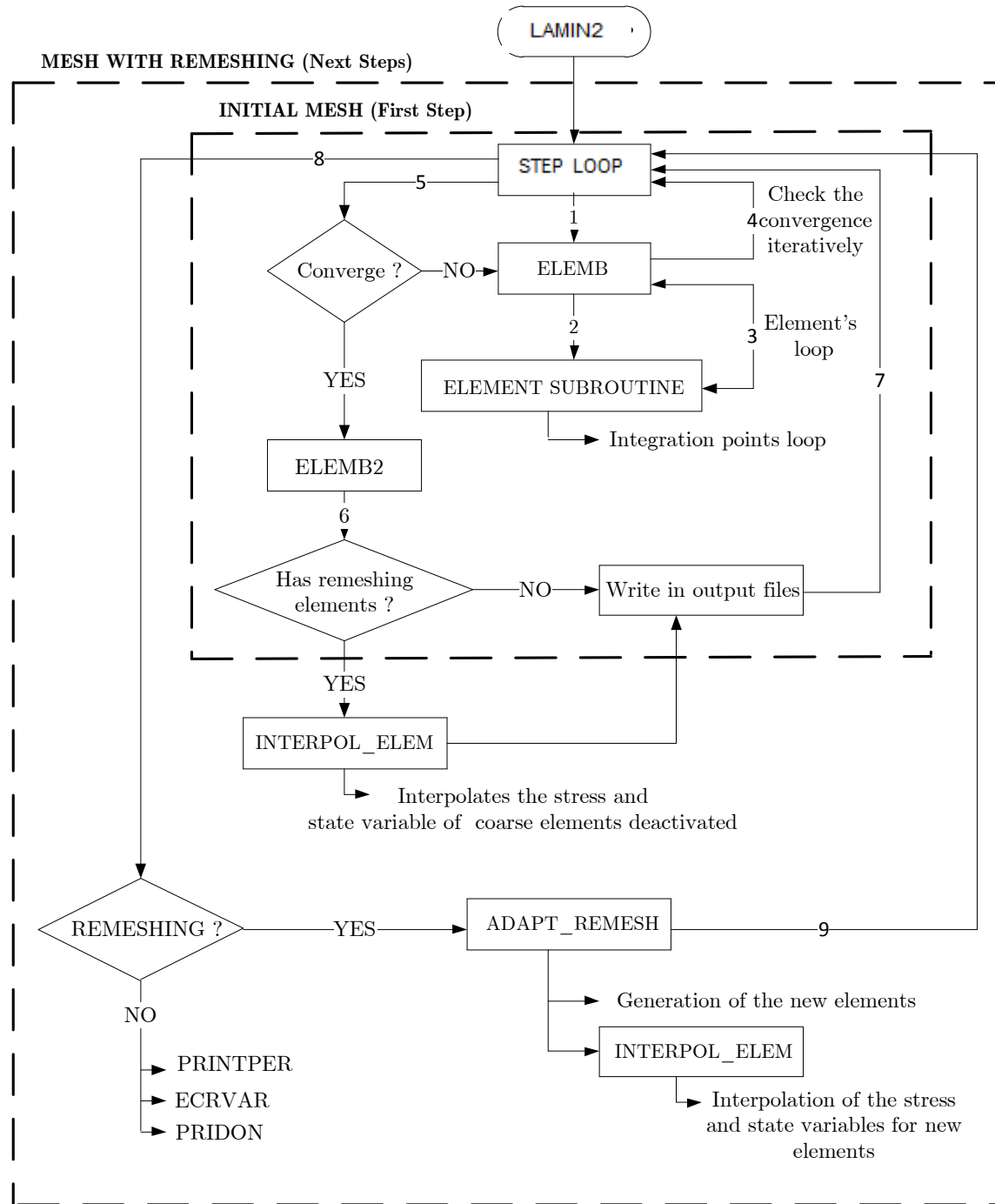


- New node
- ⊗ New integration point
- Old node
- × Old integration point

- **C**: coefficient defined by the user
- **n**: degree of interpolation
- **d**: highest diagonal of the element
- **D**: highest diagonal of the structure

# Adaptive Remeshing

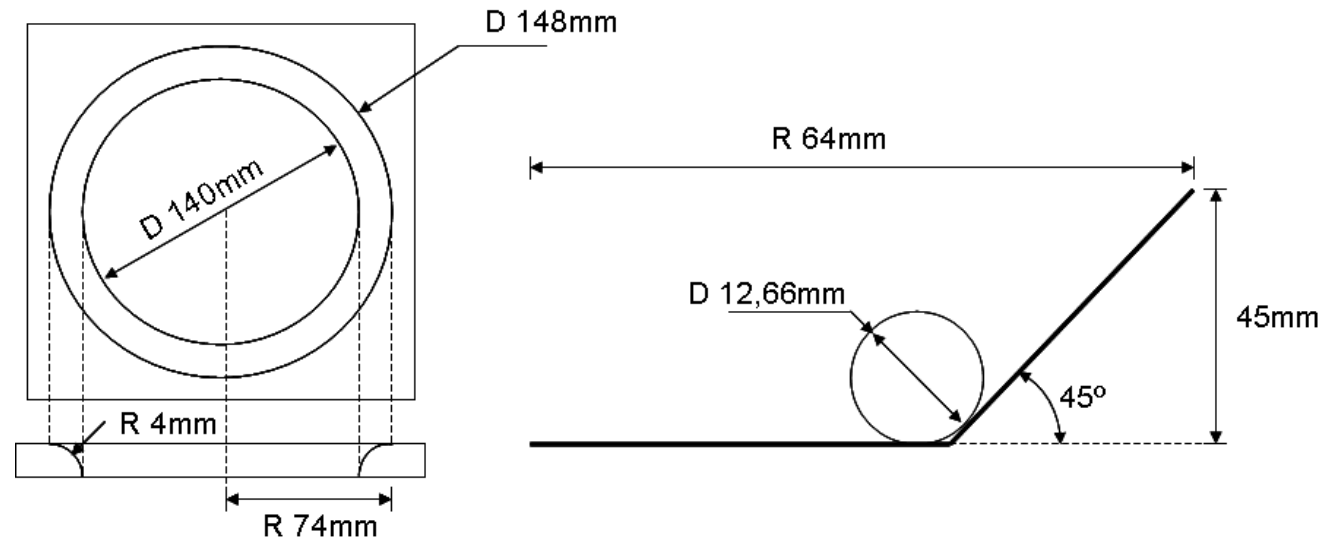
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## Conical shape simulation

- Benchmark proposal from NUMISHEET 2014 conference:



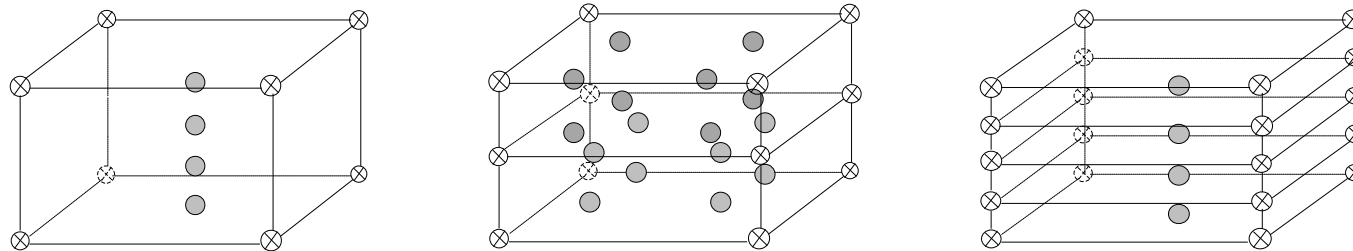
- Setup description:
  - Material : Aluminium alloy AA7075-O
  - thickness: 1.6 mm
  - spherical tool radius: 6.33 mm
  - Vertical step-down of 0.5 mm (90 contours)

## Material

- Material : An aluminium alloy AA7075-O
- The constitutive law: Hill ( **but** Isotropic behaviour law)
- Parameters:
  - Young modulus:  $E_1 = E_2 = E_3 = 72000$  MPa
  - Poisson ratio:  $\nu_1 = \nu_2 = \nu_3 = 0.33$
  - Coulomb modulus:  $G_1 = G_2 = G_3 = 27067.669$  MPa
- Hardening Swift law:  $\sigma_{eq} = K (\epsilon_0 + \epsilon_{pl})^n$  with  $K = 335.1$  MPa,  
 $\epsilon_0 = 0.004$ ,  
 $n = 0.157$

## RESS (Reduced Enhanced Solid Shell)\*

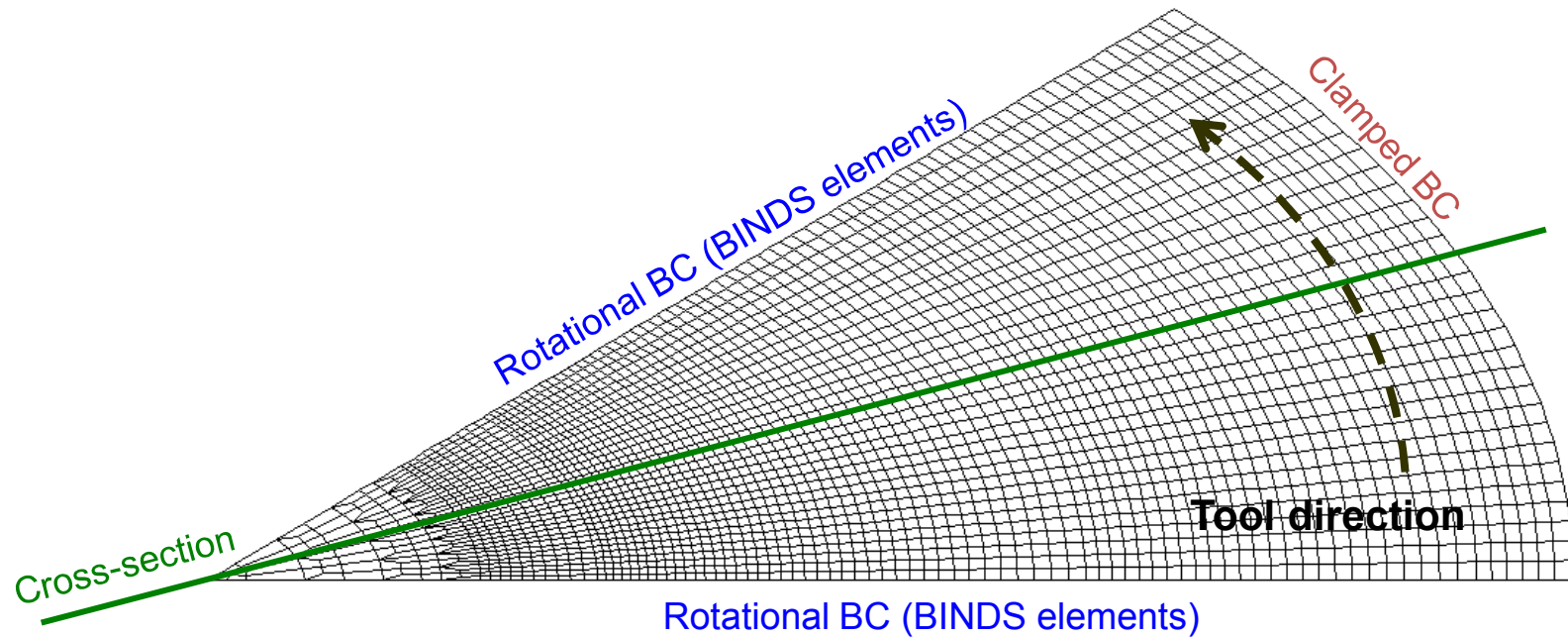
- Solid-Shell Element specially designed for metal forming applications
- Implemented in LAGAMINE code
- Integration scheme (a) advantages:
  - Reduced integration in plane
  - Arbitrary number of integration points in one single layer in thickness direction



- Combination Enhanced Assumed Strain of Simo and Rifai (1990)
- Stabilization technique

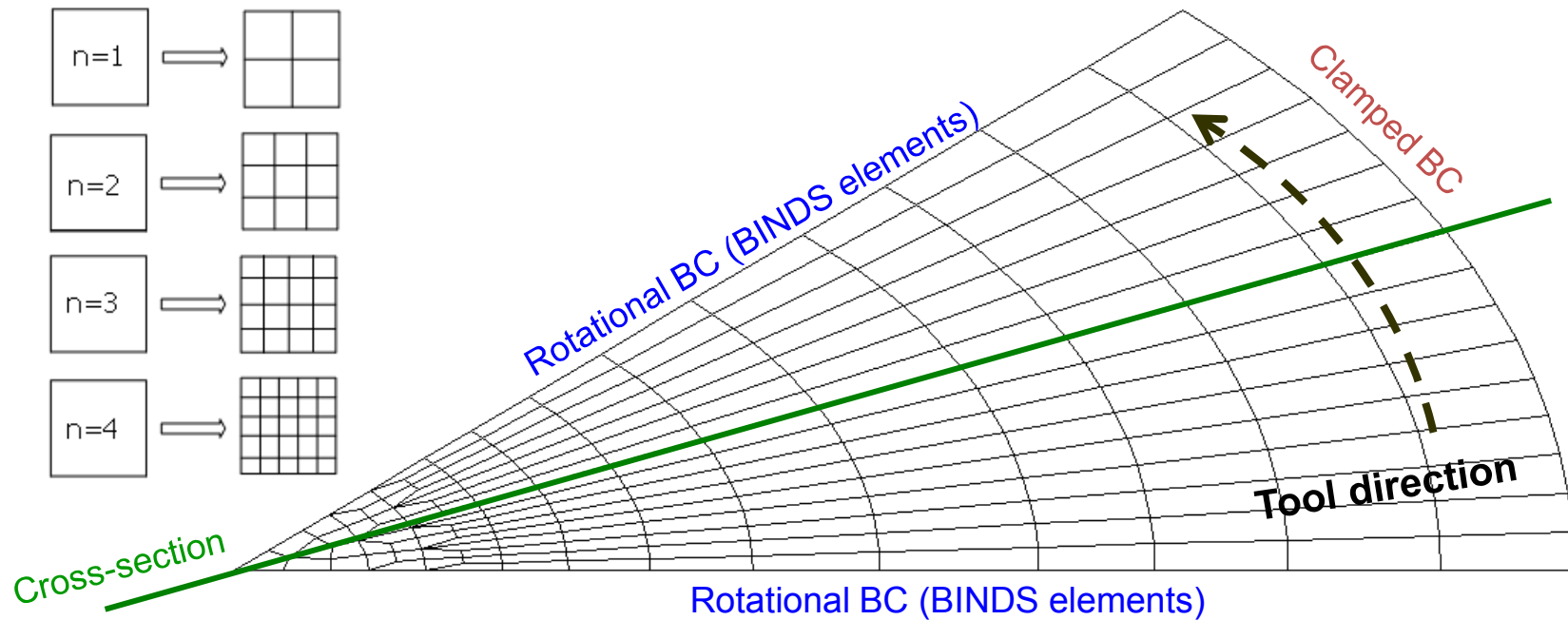
\*See in Alves de Sousa R.J. *et al.* (2007), I. J. P., Vol. 23, pp. 490-515.

## Meshes



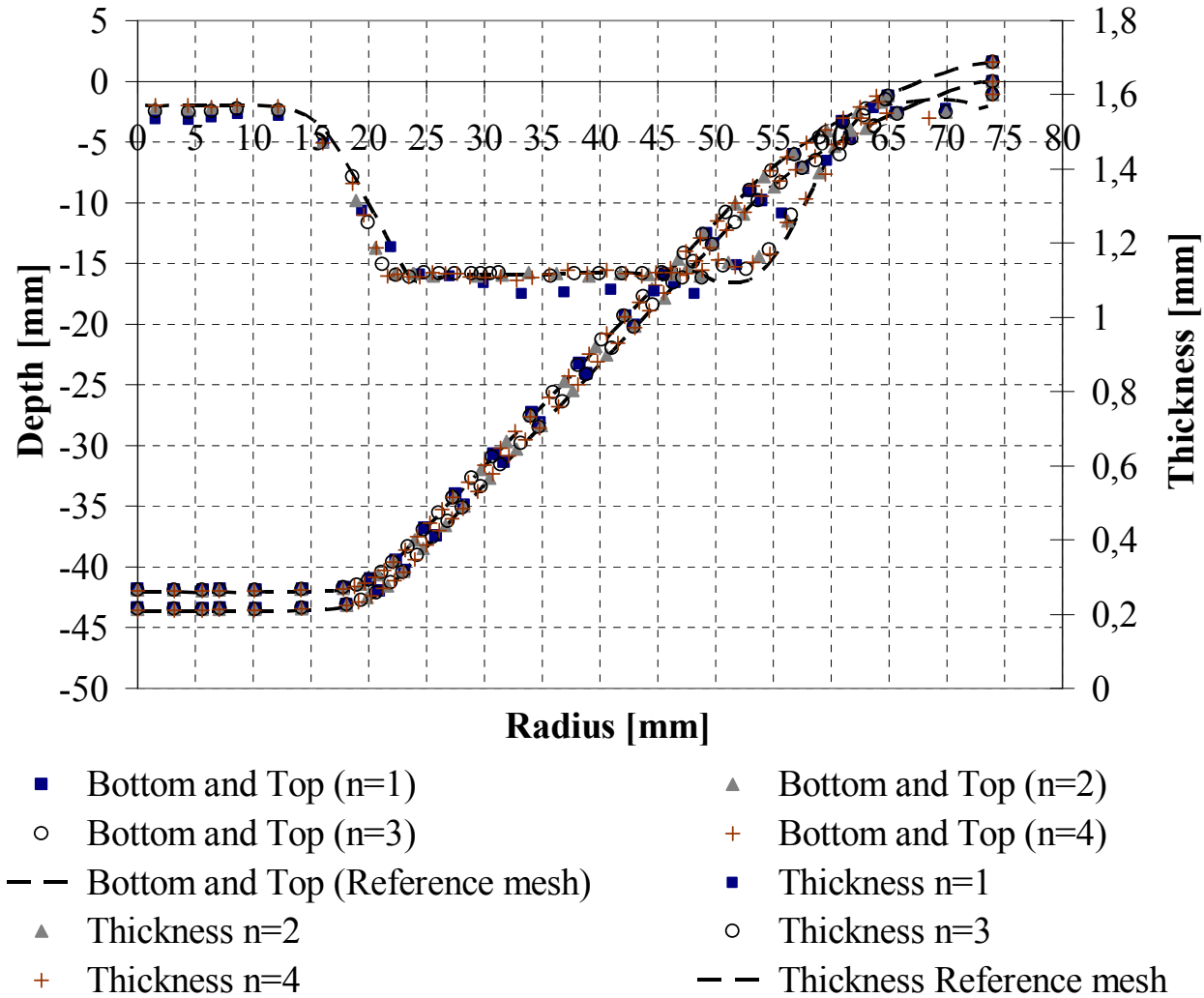
- **Reference mesh** without remeshing 5828 elements (RESS+CFI3D)
- One element in thickness direction
- 3 types of Elements :
  - 8 node solid-shell finite element RESS with 5IP
  - Contact element CFI3D with 4IP
  - Symmetric and rotational boundary conditions (BINDS elements)

## Meshes (continuation)



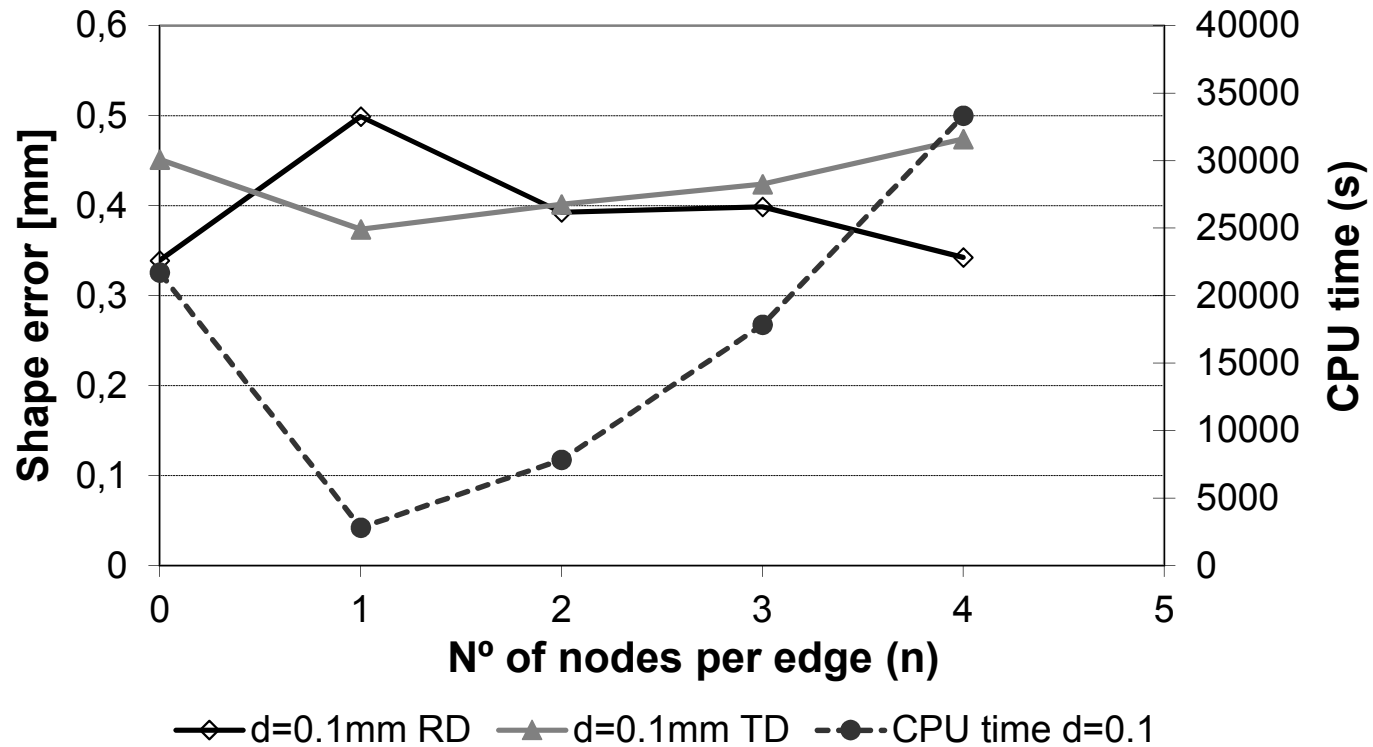
- Coarse mesh with adaptive remeshing, 410 elements (RESS+CFI3D)
- One element in thickness direction
- 3 types of Elements :
  - 8 node solid-shell finite element RESS with 5IP
  - Contact element CFI3D with 4IP
  - Binds elements
- Adaptive remeshing parameters used:  $n=1,2,3,4$ ;  $\alpha=1.0$ ;  $d=0.1\text{mm}$

## Shape and thickness in a cross-section



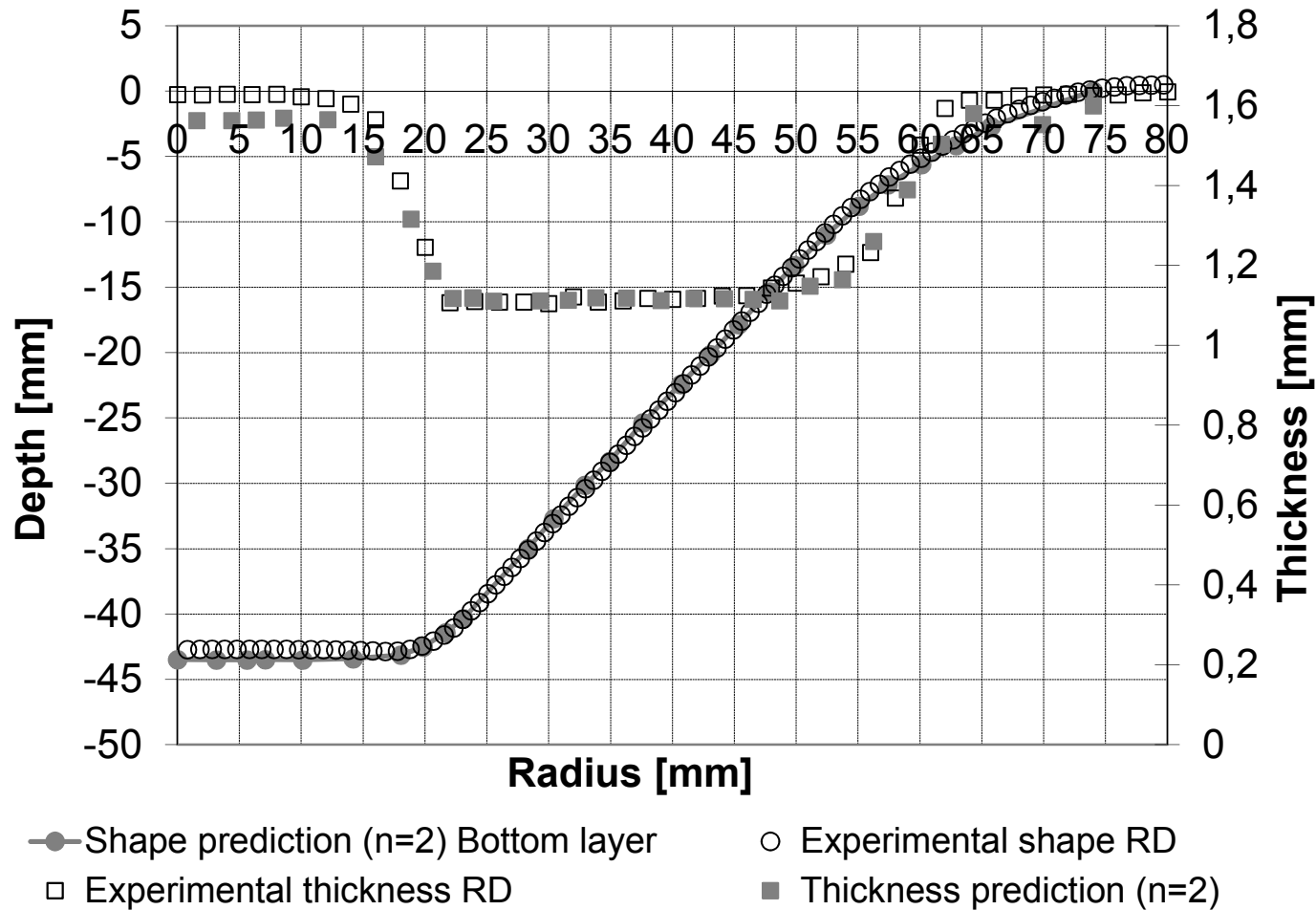
- Numerical shape at the middle section of the pie mesh to avoid boundary condition effect

## Comparisons between time performance



- n=0 indicates the reference mesh (initial refined mesh)
- The shape accuracy for different levels of refinement is analysed in different directions, transverse direction (TD) and rolling direction (RD)
- The refinement level which has a good agreement between the CPU time and accuracy in both directions is n=2

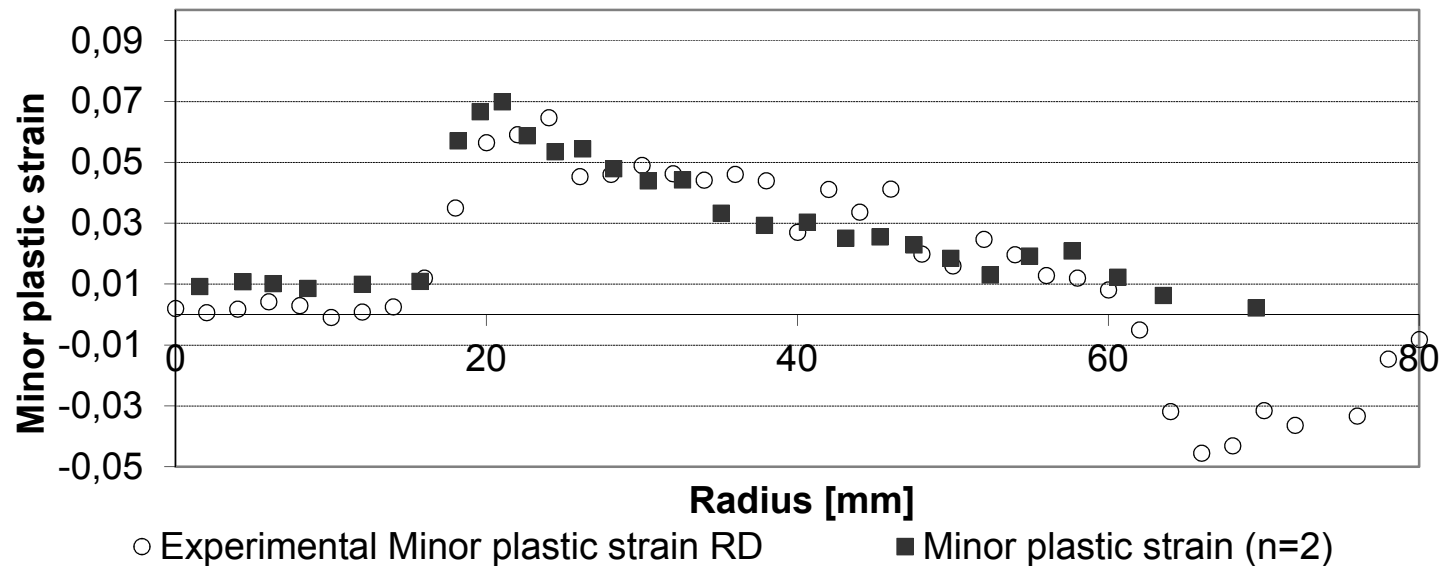
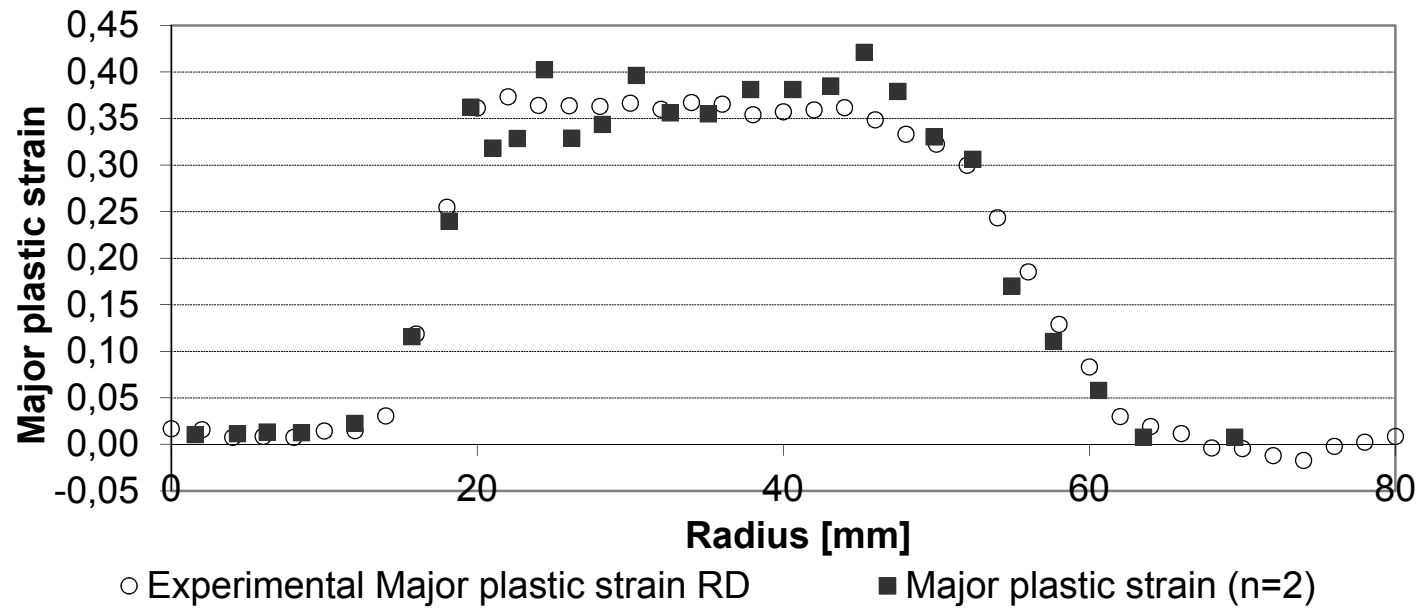
## Numerical vs Experimental



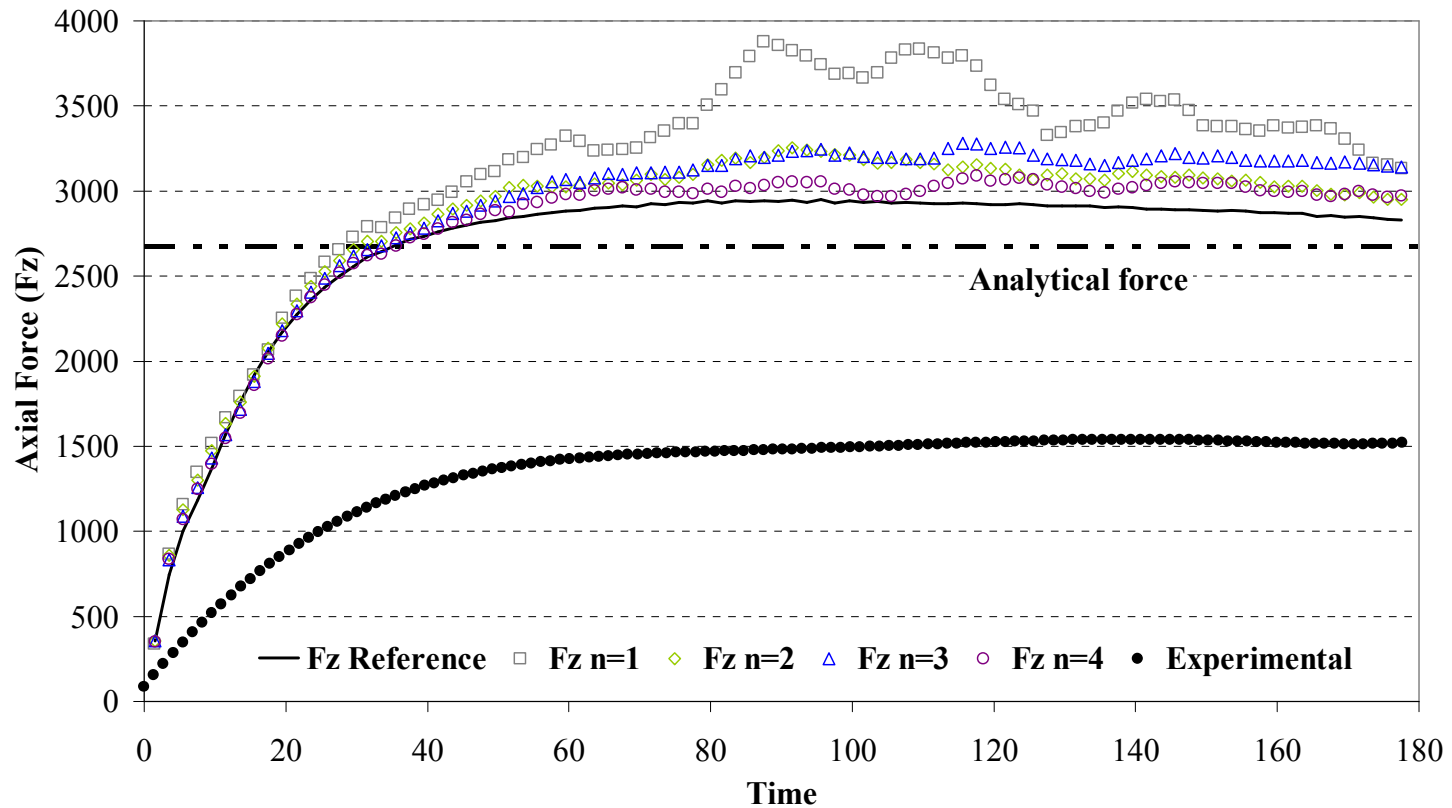
- The accuracy of shape and thickness obtained with adaptive remeshing is acceptable



## Major and minor plastic strain



## Evolution of force prediction



- N = 1 → 4 different levels of refinement
- Analytical force by Aerens\* (team of Duflou KUL)

\*See in Aerens R. *et al.* (2010), I. J. A.M. T., Vol. 46, pp. 969-982.

- 3D analysis of single point incremental forming process.
- This adaptive remeshing method induces CPU time reduction due to the decrease of the number of elements of the mesh
- Interest of 3D finite elements,
  - more accurate thickness computation
  - full 3D constitutive laws
  - all components of the stress field necessary for damage approach.



Thank you for your attention

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