## COSMOGRAIL: the COSmological MOnitoring of **GRAvItational Lenses**\*,\*\*

### XIV. Time delay of the doubly lensed guasar SDSS J1001+5027

S. Rathna Kumar<sup>1</sup>, M. Tewes<sup>2</sup>, C. S. Stalin<sup>1</sup>, F. Courbin<sup>2</sup>, I. Asfandiyarov<sup>3</sup>, G. Meylan<sup>2</sup>, E. Eulaers<sup>4</sup>, T. P. Prabhu<sup>1</sup>, P. Magain<sup>4</sup>, H. Van Winckel<sup>5</sup>, and Sh. Ehgamberdiev<sup>3</sup>

Indian Institute of Astrophysics, II Block, Koramangala, Bangalore 560 034, India, e-mail: rathna@iiap.res.in

2 Laboratoire d'astrophysique, Ecole Polytechnique Fédérale de Lausanne (EPFL), Observatoire de Sauverny, 1290 Versoix, Switzer-

Ulugh Beg Astronomical Institute, Uzbek Academy of Sciences, Astronomicheskaya 33, Tashkent, 100052, Uzbekistan

Institut d'Astrophysique et de Géophysique, Université de Liège, Allée du 6 Août, 17, 4000 Sart Tilman, Liège 1, Belgium

Instituut voor Sterrenkunde, Katholieke Universiteit Leuven, Celestijnenlaan 200B, 3001 Heverlee, Belgium

### ABSTRACT

This paper presents optical R-band light curves and the time delay of the doubly imaged gravitationally lensed quasar SDSS J1001+5027 at a redshift of 1.838. We have observed this target for more than six years, between March 2005 and July 2011, using the 1.2-m Mercator Telescope, the 1.5-m telescope of the Maidanak Observatory and the 2-m Himalayan Chandra Telescope. Our resulting light curves are composed of 443 independent epochs, and show strong intrinsic quasar variability, with an amplitude of the order of 0.2 magnitudes. From this data, we measure the time delay using five different methods, all relying on distinct approaches. One of these techniques is a new development presented in this paper. All our time-delay measurements are perfectly compatible. By combining them, we conclude that image A is leading B by 119.3  $\pm$  3.3 days (1 $\sigma$ , 2.8%), including systematic errors. It has been shown recently that such accurate time-delay measurements offer a highly complementary probe of dark energy and spatial curvature, as they independently constrain the Hubble constant. The next mandatory step towards using SDSS J1001+5027 in this context will be the measurement of the redshift of the lensing galaxy, in combination with deep HST imaging.

Key words. gravitational lensing: strong – cosmological parameters – quasar: individual (SDSS J1001+5027)

<sup>1</sup> Indian Institute of Astrophysics, II Block, Koramangala, Bangal
 <sup>2</sup> Laboratoire d'astrophysique, Ecole Polytechnique Fédérale de La land
 <sup>3</sup> Ulugh Beg Astronomical Institute, Uzbek Academy of Sciences
 <sup>4</sup> Institut d'Astrophysique et de Géophysique, Université de Liège
 <sup>5</sup> Instituut voor Sterrenkunde, Katholieke Universiteit Leuven, Ce
 Received / Accepted **Base 1 Base 1 Base 1 Base 1 Base 1 Base 1 Control 1 Control 1 Base 1 B** 

ter  $H_0$ , on the curvature,  $\Omega_k$ , and on the dark energy equation of state parameter w mostly rely on the combination of the Baryonic Acoustic Oscillations measurements (BAO) with the Cosmic Microwave Background (CMB) observations.

Strong gravitational lensing offers a valuable yet cheap complement to independently constrain some of the cosmological parameters, through the measurement of the so-called "time delays" in quasars strongly lensed by a foreground galaxy (Refsdal 1964). The principle of the method is the following. The travel times of photons along the distinct optical paths forming the multiple images are not identical. These travel time differences, namely the time delays, depend on the geometrical differences between the optical paths (which contain the cosmological information) and on the potential well of the lensing galaxy(ies). In practice, time delays can be measured from photometric light curves of the multiple images of lensed quasar: if the quasar shows photometric variations, these are seen in the individual light curves at epochs separated by the time delay.

A precise and accurate measurement of such a time delay, in combination with a well-constrained model for the lensing galaxy, can therefore be used to extract cosmological information. The excellent performance and strong competitiveness of this time-delay method has recently been quantified by Suyu et al. (2013a) (see also Schneider & Sluse 2013; Suyu et al. 2013b), Linder (2011), and summarized in Treu et al. (2013).

So far, only a few quasar time delays have been measured convincingly, from long and well sampled light curves. The

<sup>\*</sup> Based on observations made with the 2.0-m Himalayan Chandra Telescope (Hanle, India), the 1.5-m AZT-22 telescope (Maidanak Observatory, Uzbekistan), and the 1.2-m Mercator Telescope. Mercator is operated on the island of La Palma by the Flemish Community, at the Spanish Observatorio del Roque de los Muchachos of the Instituto de Astrofísica de Canarias.

Light curves will be available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via http://cdsarc.u-strasbg.fr/vizbin/qcat?J/A+A/???, and on http://www.cosmograil.org.



Fig. 1. Distribution of the average observed FWHM and elongation  $\epsilon$  of field stars in the images used to build the light curves of SDSS J1001+5027.

international COSMOGRAIL<sup>1</sup> (COSmological MOnitoring of GRAvItational Lenses) collaboration is changing this situation by measuring accurate time delays for a large number of gravitationally lensed quasars. The goal of COSMOGRAIL is to reach an accuracy of less than 3%, including systematics, for most of its targets.

In this paper, we present the time-delay measurement for the two-image gravitationally lensed quasar SDSS J1001+5027 ( $\alpha_{2000} = 10:01:28.61, \delta_{2000} = +50:27:56.90$ ), at z = 1.838 (Oguri et al. 2005). The image separation of  $\Delta\theta = 2.86''$  (Oguri et al. 2005) and the high declination of the target makes it a relatively easy prey for medium size northern telescopes and average seeing conditions. The redshift of the lensing galaxy has not been measured spectroscopically but Oguri et al. (2005) measure colors suggestive of an elliptical galaxy at a redshift in the range 0.2 < z < 0.5.

Our paper is structured as follows. Section 2 describes our monitoring, the data reduction, and the resulting light curves. In Section 3 we present a new time-delay point estimator. We add this technique to a pool of four other existing algorithms, to measure the time delay in Section 4. Finally, we summarize our results and conclude in Section 5.

### 2. Observations, data reduction, and light curves

### 2.1. Observations

We monitored SDSS J1001+5027 in the R-band for more than 6 years, from March 2005 to July 2011, with three different telescopes: the 1.2-m Mercator Telescope located at the Roque de los Muchachos Observatory on La Palma (Spain), the 1.5-m telescope of the Maidanak Observatory in Pamir Alai (Uzbekistan), and the 2-m Himalayan Chandra Telescope (HCT) located at the Indian Astronomical Observatory in Hanle (India). Table 1 details our monitoring observations. In total we obtained photometric measurements for 443 independent epochs, with a mean sampling interval below 4 days. Each epoch consists of at least 3, but mostly 4 or more, dithered exposures. Figure 1 summarizes the image quality of our data. The COSMOGRAIL collaboration has now ceased the monitoring of this target, to focus on other systems.

### 2.2. Deconvolution photometry

The image reduction and photometry closely follows the procedure described in Tewes et al. (2013b). We perform the flat-field correction and bias subtraction for each exposure using custom software pipelines, which address the particularities of the different telescopes and instruments.

Figure 2 shows part of the field around SDSS J1001+5027, as obtained by stacking the best monitoring exposures from the Mercator telescope to reach an integrated exposure time of 21 hours. The relative flux measurements of the quasar images and reference stars, for each individual epoch, are obtained though our COSMOGRAIL photometry pipeline, which is based on the simultaneous MCS deconvolution algorithm (Magain et al. 1998). The stars labeled 1, 2, and 3 in Fig. 2 are used to characterize the Point Spread Function (PSF) and relative magnitude zero-point of each exposure.

The 2 quasar images A and B of SDSS J1001+5027 are separated by 2.86", which is significantly larger than the typical separation in strongly lensed quasars. In principle, this makes SDSS J1001+5027 a relatively easy target to monitor, as the quasar images are only slightly blended in most of our images. However, image B lies close to the primary lensing galaxy G1. Minimizing the additive contamination by G1 to the flux measurements of B therefore requires a model for the light distribution of G1. In Fig. 3, we show two different ways of modeling these galaxies. Our standard approach, shown in the bottom panels, consists in representing all extended objects, such as the lens galaxies, by a regularized pixel grid. The values of these pixels get iteratively updated during the deconvolution photometry procedure. Due to obvious degeneracies, this approach may fail when a relatively small extended object (lens galaxy) is strongly blended with a bright point source (quasar), leading to unphysical light distributions. To explore the sensitivity of our results to such a possible bias, we have adopted an alternative approach, by representing G1 and G2 by two simply parametrized elliptical Sersic profiles, as shown in the top row of Fig. 3. For both cases, the residuals from single exposures are convincingly homogeneous. Only when averaging the residuals of many exposures to decrease the noise, it can be seen that the simply parametrized models yield a less good overall fit to the data, since they cannot represent further background sources nor compensate for small systematic errors in the shape of the PSF.

We find that the difference between these approaches in terms of the resulting quasar flux photometry is very marginal, and insignificant regarding the measurement of the time delay. In all the following we will use the quasar photometry obtained using the simply parametrized model (top row of Fig. 3), which is likely to be closer to reality than our pixelized model, in the immediate surroundings of image B.

### 2.3. Light curves

Following Tewes et al. (2013b), we empirically correct for small magnitude and flux shifts between the light curve contributions from different telescopes/cameras, to obtain minimal dispersion in each of the combined light curves. In the present case we choose the photometry from the Mercator telescope as a reference, and we optimize, for the data from the Maidanak and HCT telescopes, a common magnitude shift and individual flux shifts for A and B.

Figure 4 shows the combined 6.5-season long light curves, from which we measure a time delay of  $\Delta t_{AB} = -119.3$  days (see Section 4). In this figure, the light curve B has been shifted by this time delay, to highlight the correspondence and temporal overlap of the data. We observe strong "intrinsic" quasar variability, common to the images A and B. In the period 2006 to 2007, the variability in image A is as large as 0.25 magnitudes

<sup>1</sup> http://www.cosmograil.org/

 Table 1. Summary of COSMOGRAIL observations of SDSS J1001+5027.

Telescope	Camera	FoV	Pixel scale	Monitoring period	Epochs	Exp. time <sup>a</sup>	Sampling <sup>b</sup>
Mercator 1.2 m	MEROPE	$6.5' \times 6.5'$	0".190	Mar. 2005 – Dec. 2008	239	5 × 360 s	3.8 (2.0) d
HCT 2.0 m	HFOSC	$10' \times 10'$	0''296	Oct. 2005 - Jul. 2011	143	$4 \times 300 \text{ s}$	9.5 (6.1) d
Maidanak 1.5 m	SITE	$8.9' \times 3.5'$	0''266	Dec. 2005 – Jul. 2008	41	$7 \times 180 \text{ s}$	5.9 (4.1) d
Maidanak 1.5 m	SI	$18.1' \times 18.1'$	0''266	Nov. 2006 – Oct. 2008	20	$6 \times 600 \text{ s}$	12.6 (9.5) d
Combined				Mar. 2005 – Jul. 2011	443	201.5 h	3.8 (1.9) d

**Notes.** <sup>(a)</sup> The exposure time is given by the number of dithered exposures per epoch and their individual exposure times. <sup>(b)</sup> The sampling is given as the mean (median) number of days between two consecutive epochs, excluding the seasonal gaps.



**Fig. 2.** R-band image centered on SDSS J1001+5027. The image is the combination of the 210 best exposures from the Mercator telescope, for a total exposure time of 21 hours. We use the stars labeled 1, 2, and 3 to model the PSF and to cross-calibrate the photometry of each exposure. The position of the two lensing galaxies G1 and G2 are indicated in zoomed image in the upper left. They are best visible on the deconvolved images presented in Fig. 3.

over a single year. In addition to this large scale correspondence, several small and short scale intrinsic variability features are common to both curves, for instance around December 2005 and January 2010. Our data unambiguously reveals an approximate time delay of  $\Delta t_{AB} \approx -120$  days, with A leading B.

# 2.4. On an apparent mismatch between the light curves of the quasar images

The apparent flux ratio between the quasar images, as inferred from the time-shifted light curves shown in Fig. 4, roughly stays in the range from 0.40 to 0.44 mag over the length of our monitoring. Strong gravitational lens models readily explain different magnifications of the quasar images, yielding stationary flux ratios or magnitude shifts between the light curves. Figure 4 hints however at a moderate correlation between some variable flux ratio and the intrinsic quasar variability. In particular, the amplitude of the quasar variability, in units of magnitudes, appears to be smaller in B than in A. Potential reasons for this mismatch include effects of microlensing by stars of the lens galaxy, or a plain contamination of the photometry of B by some additive external flux. We find that one has to subtract from curve B about 20% of its median flux to obtain an almost stationary magnitude shift, of about 0.66 mag, between the light curves. As such a contamination would be several times larger than the entire flux of galaxy G1, we conclude that plausible errors of our light models for G1 cannot be responsible for the observed discrepancy between the light curves.



**Fig. 3.** Illustration of the two ways of modeling the light-distribution for extended objects, during the deconvolution process. On the left is shown a single 360 second exposure of SDSS J1001+5027 obtained with the Mercator telescope in typical atmospheric conditions. The other panels show the parametric (top row) and pixelized light models (bottom row) for the lens galaxies, as described in the text. The residual image for the single exposure is also shown in each case, as well as the average residuals over the 120 best exposures. The residual maps are normalized by the shot noise amplitude. The dark areas indicate excess flux in the data with respect to the model. Gray scales are linear.



**Fig. 4.** R-band light curves of the quasars images A and B in SDSS J1001+5027, from March 2005 to July 2011. The  $1\sigma$  photometric error bars are also shown. For display purpose, the curve of quasar image B is shown shifted in time by the measured time delay (see text). The light curves are available in tabular form from the CDS and the COSMOGRAIL website.

### 3. A new additional time-delay estimator

Although an unambiguous approximation of the time delay of SDSS J1001+5027 can be made by eye, accurately measuring its value is not trivial, and exacerbated by the "extrinsic" variability between the light curves. Even more obvious features of the data, such as the sampling gaps due to non-visibility periods of the targets, could easily bias the results from a time-delay measurement technique. The impact of these effects on the quality of the time-delay inference clearly differs for each individual quasar lensing system and dataset. To check for potential systematic errors, we feel that a wise approach is to employ several numerical methods based on different fundamental principles.

In the present section we introduce a new time-delay estimation method, based on minimizing residuals of a high-pass filtered difference light curve between the quasar images.

### 3.1. The difference-smoothing technique

This technique is a point estimator, that determines both an optimal time delay and an optimal shift in *flux* between two light curves, while also allowing for smooth extrinsic variability. The correction for a flux shift between the light curves explicitly addresses the mismatch described in Section 2.4, whatever its physical explanation. Such a flux shift may be due to a contamination of light curve B by residual light from the lensing galaxy, from

![](_page_4_Figure_1.jpeg)

**Fig. 5.** The difference light curve  $d_i$  is shown as colored dots for  $\Delta t_{AB} = -118.6$  days, the best time-delay estimate for the new technique introduced in this paper. The difference light curve is smoothed using a kernel of width s = 100 days to compute the differential variation  $f_i$ , shown in black. The black error bars show the uncertainty coefficients  $\sigma_{f_i}$ . The points in the difference light curve  $d_i$  are color coded according to the absolute factors of their uncertainties  $\sigma_{d_i}$  by which they deviate from  $f_i$ . In this plot, the A light curve is used as reference, and a shift in flux of the B light curve is optimized.

the lensed quasar host galaxy, or by microlensing resolving the quasar structure.

Consider two light curves A and B sampled at epochs  $t_i$ , where  $A_i$  and  $B_i$  are the observed magnitudes at epochs  $t_i$ , (i = 1, 2, 3, ..., N). We select A as the reference curve. The light curve B is shifted in time with respect to A by some amount  $\tau$ , and in *flux* by some amount  $\Delta f$ . Formally, this shifted version B' of B is given by

$$\mathbf{B}'_{i}(t'_{i}) = -2.5 \log \left( 10^{-0.4 \, \mathbf{B}_{i}(t_{i}+\tau)} + \Delta f \right). \tag{1}$$

For any estimate of the time delay  $\tau$  and of the flux shift  $\Delta f$ , we form a *difference light curve*, with points  $d_i$  at epochs  $t_i$ ,

$$d_{i} = A_{i} - \frac{\sum_{j=1}^{N} w_{ij} B'_{j}}{\sum_{i=1}^{N} w_{ij}},$$
(2)

where the weights  $w_{ij}$  are given by

$$w_{ij} = \frac{1}{\sigma_{\rm B_j}^2} e^{-(t'_j - t_i)^2 / 2\delta^2}.$$
 (3)

The parameter  $\delta$  is the decorrelation length, as in Pelt et al. (1996), and  $\sigma_{B_j}$  denotes the photometric error of the magnitude  $B_j$ . This decorrelation length should typically be of the order of the sampling period, small enough to not smooth out any intrinsic quasar variability features from the light curve B. The uncertainties on each  $d_i$  are then calculated as

$$\sigma_{d_i} = \sqrt{\sigma_{A_i}^2 + \frac{1}{\sum_{j=1}^N w_{ij}}},$$
(4)

where  $w_{ij}$  are given by Eq. 3. To summarize, at this point we have a discrete difference light curve, sampled at the epochs of curve A, built by subtracting from the light curve A a smoothed and shifted version of B. We now smooth this difference curve  $d_i$ , using again a Gaussian kernel, to obtain a model  $f_i$  for the differential extrinsic variability

$$f_{i} = \frac{\sum_{j=1}^{N} v_{ij} d_{j}}{\sum_{j=1}^{N} v_{ij}},$$
(5)

where the weights  $v_{ij}$  are given by

$$\nu_{ij} = \frac{1}{\sigma_{d_i}^2} e^{-(t_j - t_i)^2 / 2s^2}.$$
(6)

The smoothing time scale *s* is a second free parameter of this method. Its value must be chosen to be significantly larger than  $\delta$ . For each  $f_i$ , we compute an uncertainty coefficient

$$\sigma_{f_i} = \sqrt{\frac{1}{\sum_{j=1}^N \nu_{ij}}}.$$
(7)

The idea of the present method is now to optimize the timedelay estimate  $\tau$  and flux shift  $\Delta f$  to minimize the residuals between the difference curve  $d_i$  and the much smoother  $f_i$ . Any wrong value for  $\tau$  introduces relatively fast structures that originate from the quasar variability into  $d_i$ , and these structures will not be well represented by  $f_i$ . To quantify this match between  $d_i$ and  $f_i$  we define a cost function in the form of a normalized  $\chi^2$ ,

$$\overline{\chi}^{2} = \left[\sum_{i=1}^{N} \frac{(d_{i} - f_{i})^{2}}{\sigma_{d_{i}}^{2} + \sigma_{f_{i}}^{2}}\right] / \left[\sum_{i=1}^{N} \frac{1}{\sigma_{d_{i}}^{2} + \sigma_{f_{i}}^{2}}\right],\tag{8}$$

and minimize this  $\overline{\chi}^2(\tau, \Delta f)$  using a global optimization.

In the above description, the light curves A and B are not interchangeable, thus introducing an asymmetry into the timedelay measurement process. To avoid such an arbitrary choice of the reference curve, we systematically perform all computations for both permutations of A and B, and minimize the sum of the two resulting values of  $\overline{\chi}^2$ .

### 3.2. On the uncertainty estimation procedure

As a point estimator, the technique described above does not provide information on the uncertainty of its result. We stress that simple statistical techniques such as variants of bootstrapping or resampling cannot be used to quantify the uncertainty of such highly non-linear time-delay estimators (Tewes et al. 2013a). These approaches are not able to discredit "lethargic" estimators, which favor a particular solution (or a small set of solutions) while being relatively insensitive to the actual shape

![](_page_5_Figure_1.jpeg)

**Fig. 6.** Error analysis of the 4 time-delay measurement techniques, based on delay estimations on 1000 synthetic curves that mimic our SDSS J1001+5027 data. The horizontal axis corresponds to the value of the true time delay used in these synthetic light curves. The gray vertical lines delimit bins of true time delay. In each of these bins, the colored rods and  $1\sigma$  error bars show the systematic biases and random errors respectively, as committed by the different techniques.

of the light curves. Furthermore, they are not sensitive to plain systematic biases of the techniques.

Consequently, to quantify the random and systematic errors of this estimator, for each dataset to be analyzed and as a function of its free parameters, we follow the Monte Carlo analysis described in Tewes et al. (2013a). It consists in applying the point estimator to a large number of fully synthetic light curves, which closely mimic the properties of the observed data, but have known true time delays. It is particularly important that these synthetic curves cover a range of true time delays around a plausible solution, instead of all having the same true time delay. Only this feature enables the method to adequately penalize estimators with lethargic tendencies.

### 3.3. Application to SDSS J1001+5027

The decorrelation length  $\delta$  and the width of the smoothing kernel s are the two free parameters of the described technique. In this work, we choose  $\delta$  to be equal to the mean sampling of the light curves ( $\delta = 5.2$  days) and s = 100 days, yielding a point estimate of  $\Delta t_{AB} = -118.6$  days for the time delay. The corresponding  $d_i$  and  $f_i$  difference light curves are shown in Fig. 5. Results of the uncertainty analysis will be presented in the next section, together with the performance of other point estimators.

We have explored a range of alternative values for the free parameters (s = 50, 100, 150, 200 and  $\delta = 2.6, 5.2, 10.4$  days), and find that neither the time-delay point estimate from the observed data, nor the error analysis is significantly affected. The time-delay estimates resulting from these experiments stay within 1.2 days around the reference value obtained for  $\delta = 5.2$  and s = 100 days. Regarding the uncertainty analysis, we observe that increasing the smoothing length scale *s* beyond 100 days decreases the random error, but at the cost of an increasing bias, which is not surprising.

![](_page_5_Figure_9.jpeg)

**Fig. 7.** Time-delay measurements of SDSS J1001+5027, following 5 different methods. The total error bar shown here includes systematics and random errors.

**Table 2.** Time-delay measurements for SDSS J1001+5027. The total  $1\sigma$  error bars are given. Whenever possible, we give in parenthesis the breakdown of the error budget: (random, systematic).

Method	$\Delta t_{\rm AB}$ [day]
Dispersion-like technique	-120.5 +/- 6.2 (3.6, 5.0)
Difference-smoothing technique	-118.6 +/- 3.7 (3.4, 1.4)
Regression difference technique	-121.1 +/- 3.8 (3.7, 1.0)
Free-knot spline technique	-119.7 +/- 2.6 (2.4, 0.8)
GP by Hojjati et al. (2013)	-117.8 +/- 3.2
Combined estimate (see text)	-119.3 +/- 3.3

### 4. Time-delay measurement of SDSS J1001+5027

In this work, we use five different methods to measure the time delay of SDSS J1001+5027 from the data shown in Fig. 4. All these methods have been developed to address light curves affected by extrinsic variability, as resulting from microlensing or flux contamination. Three of the techniques, namely the dispersion-like technique, the regression difference technique, and the free-knot spline technique are described in length in Tewes et al. (2013a) and were used to measure the time delays in the 4-image quasar RX J1131–123 (Tewes et al. 2013b).

In the the previous section, we have presented our fourth method, the difference-smoothing technique. These first four methods are point estimators: they provide best estimates, without information on the uncertainty of their results. We proceed by quantifying the accuracy and precision of these estimators by applying them to a set of 1000 fully synthetic light curves, produced and adjusted following Tewes et al. (2013a). These simulations include the intrinsic variations of the quasar source, mimicking the observed variability of SDSS J1001+5027, as well as extrinsic variability on a range of time scales from a few days to several years. They share the same sampling and scatter properties as the real observations.

Figure 6 shows the results of this analysis, depicting the delay measurement error as a function of the true delay used to generate the synthetic light curves. As always, this analysis naturally takes into account the intrinsic variances of the techniques, which are due to the limited ability of the employed global optimizers to find the absolute minima of the cost functions.

As can be seen on Fig. 6, the dispersion-like technique is strongly biased for this particular dataset. This could be a consequence of the simplistic polynomial correction for extrinsic variability linked to this technique. For the other techniques, the bias remains smaller than the random error, and no strong dependence on the true time delay is detected.

The final systematic error bar for each of these four techniques is taken as the worst measured systematic error on the simulated light curves (biggest colored rod in Fig. 6). The final random error is taken as the largest random error across the range of tested time delays. Finally, the total error bar for each technique is obtained by summing the systematic and random components in quadrature.

In the writing process of this paper, Hojjati et al. (2013) proposed a new independent method to measure time delays which is also able to address extrinsic variability. Their method is based on Gaussian process modeling, and does not rely on point estimation. It provides its own standalone estimate of the total uncertainty. We have provided these authors with the COSMOGRAIL data of SDSS J1001+5027, without letting them know about our measured values. They find  $\Delta t_{AB} = -117.8 \pm 3.2$  days.

We include this measurement by Hojjati et al. (2013) as a fifth measurement in our result summary, presented in Table 2 and in a more graphical form in Fig. 7. Not only their time-delay values agree with our four estimates, but also their error bars agree well with ours, in spite of the totally different way of estimating them.

We have five time-delay estimates from five very different methods, and all these estimates are compatible with each other. It remains to combine these results. In doing this, we exclude the delay from the dispersion-like technique which, as we show, is dominated by systematic errors. While the estimates from the four remaining techniques are obtained with very different methods, they are still not independent, as they all make use of the same data. We therefore simply average the four time-delay measurements to obtain our combined estimate, and we use the average of the total uncertainties as the corresponding uncertainty. This leads to  $\Delta t_{AB} = -119.3 \pm 3.3$  days, shown in black on Fig. 7.

### 5. Conclusion

In this paper, we present the full COSMOGRAIL light curves for the two images of the gravitationally lensed quasar SDSS J1001+5027. The final data, all taken in the R-band, totalize 443 observing epochs, with a mean temporal sampling of 3.8 days, from the end of 2004 to mid-2011. The COSMOGRAIL monitoring campaign for SDSS J1001+5027 has now stopped. It involved three different telescopes with diameters from 1.2 m to 2 m, hence illustrating the effectiveness of small telescopes in conducting long-term projects with potentially high impact on cosmology.

We analyse our light curves with five different numerical techniques, including the three methods described in Tewes et al. (2013a). In addition, we introduce and describe a new additional method, based on representing the extrinsic variability by a smoothed version of the difference light curve between the quasar images. Finally, we also present results obtained via the technique of Hojjati et al. (2013), based on modeling of the quasar and microlensing variations using Gaussian processes. The latter technique was *blindly* applied to the data by the authors of Hojjati et al. (2013), without any prior knowledge of the results obtained with the other four methods.

Aside from the dispersion-like technique, dominated by systematic errors, we find that the other four methods yield similar time-delay values and similar random and systematic error bars. Our final estimate of the time delay is taken as the mean of these four best results, together with the mean of their uncertainties:  $\Delta t_{AB} = -119.3 \pm 3.3$  days, with image A leading image B. This is a relative uncertainty of 2.8%, including systematic errors.

The present time-delay measurement can be used in combination with lens models to constrain cosmological parameters, in particular the Hubble parameter,  $H_0$ , and the curvature  $\Omega_k$  (e.g. Suyu et al. 2013a). The accuracy reached on cosmology with SDSS J1001+5027 alone or in combination with other lenses, will rely on the availability of follow-up observations to measure: (1) the lens redshift and velocity dispersion, (2) the mass contribution of intervening objects along the line of sight, (3) the detailed structure of the lensed host galaxy of the quasar. This translates in practice into one single night of an 8m-class telescope, plus about four orbits of the Hubble Space Telescope.

Acknowledgements. We thank the numerous observers who contributed to the data from the Mercator and Maidanak telescopes, and we are grateful for the support provided by the staff at the Indian Astronomical Observatory, Hanle and CREST, Hoskote. We also thank A. Hojjati, A. Kim, and E. Linder for running their curve shifting algorithm on our data. S. Rathna Kumar and C. S. Stalin acknowledge support from the Indo-Swiss Personnel Exchange Programme INT/SWISS/ISJRP/PEP/P-01/2012. COSMOGRAIL is financially supported by the Swiss National Science Foundation (SNSF).

### References

- Hojjati, A., Kim, A. G., & Linder, E. V. 2013, ArXiv1304.0309
- Linder, E. V. 2011, Physical Review D, 84, 123529
- Magain, P., Courbin, F., & Sohy, S. 1998, ApJ, 494, 472
- Oguri, M., Inada, N., Hennawi, J. F., et al. 2005, ApJ, 622, 106
- Pelt, J., Kayser, R., Refsdal, S., & Schramm, T. 1996, A&A, 305, 97
- Planck Collaboration. 2013, ArXiv1303.5076
- Refsdal, S. 1964, MNRAS, 128, 307
- Schneider, P. & Sluse, D. 2013, arXiv:1306.0901
- Suyu, S. H., Auger, M. W., Hilbert, S., et al. 2013a, ApJ, 766, 70
- Suyu, S. H., Treu, T., Hilbert, S., et al. 2013b, arXiv:1306.4732
- Tewes, M., Courbin, F., & Meylan, G. 2013a, A&A, 553, A120
- Tewes, M., Courbin, F., Meylan, G., et al. 2013b, A&A in press, arXiv:1208.6009 Treu, T., Marshall, P. J., Cyr-Racine, F.-Y., et al. 2013, arXiv:1306.1272