

OVERHEAD TRANSMISSION LINES DESIGN

SOME MECHANICAL ASPECTS

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point out the effects of some basic choices on galloping phenomena. Important parameters of transmission lines are: type of conductor, span length, subconductor diameter, bundle geometry, type and number of spacers, sag-span ratio, yoke plate dimension, bundle orientation, etc.

This paper describes some analyses including the theoretical modeling and specific approach on the transmission line system with its important parameters. Various simulations on real cases are given as a help for overhead transmission lines design.

BASIC MECHANISM

Galloping is nearly always caused by moderately strong, steady cross-winds acting upon an asymmetrical iced conductor surface. This asymmetry generally appears when the meteorological conditions are favorable to formation of ice coating around the conductors which grows preferentially on the side facing the wind or the precipitation. The origin of galloping is caused by two aerodynamic forces due to the wind action on an asymmetrical conductor profile. Because of boundary conditions, cable can rotate only around its shear center. So that the aerodynamic drag and lift (acting in the aerodynamic center) are replaced by three loads acting in the shear center of the cable: the same drag f_D and lift f_L , and an additional pitching moment M_W . The drag and lift forces are respectively oriented parallel and perpendicular to the relative wind speed which refers to conductor in movement. The reference directions are defined in Figure 1.

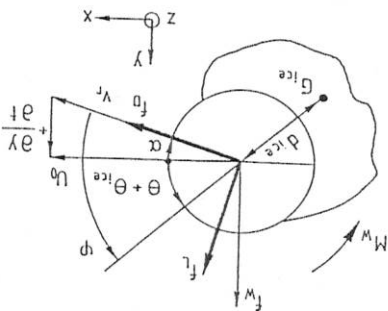


Figure 1: Definition for angles and forces

According to aerodynamics, the drag force f_D , lift force f_L and moment M_W are given by

$$f_D = K_D V_r^2 C_D(\phi), \quad f_L = K_L V_r^2 C_L(\phi), \quad M_W = K_M V_r^2 C_M(\phi)$$

$$\text{with } K_D = \frac{1}{2} \rho_{air} \phi \quad \text{and} \quad K_M = \frac{1}{2} \rho_{air} \phi^2$$

where ρ_{air} is mass density of air, V_r is relative wind speed, ϕ is diameter of conductor, C_D , C_L and C_M represent aerodynamic coefficients of drag, lift and moment. The eccentricity of ice shape is defined by $\epsilon = 2 \left(\frac{d_{ice}}{0.5d} - 1 \right)$, where d_{ice} is the distance between the shear center of conductor and the center of the ice gravity. For a 3/2 eccentricity ice shape, the general shapes of aerodynamic coefficients are shown in Figure 2.

With long distance power transmission lines of HVAC and HVDC, there are not only electrical aspects to be considered. If a general collapse occurs due to mechanical aspects, there will be no way to

refit all the power system.

This paper deals with galloping. Galloping is a large amplitude, low frequency and wind-induced oscillation on both single and bundle overhead transmission lines. Even though galloping is sometimes weak and fugitive, in some other cases it may cause lots of troubles. The effects of galloping on a line are dependent on the severity and the duration of the event and on the type of line construction. The typical problems that galloping causes are:

The electrical damage: Because galloping amplitudes may approach or even exceed the sag of the span, the conductors may get too close so that it may cause phase-to-phase flashovers, which make circuit breakers operation and the arcing damage to conductors. After a few time, the galloping lines must be tripped out with many problems for network operation.

The mechanical damage: When galloping occurs, the strings and towers are subjected to great dynamic stress leading to damage to strings and towers, such as loosening and ejection of tower bolts, wearing on landing bolts, ovaling of hole and distortion of tower swivels as well as associated hardware. Galloping also causes the fatigue of conductor at semi-tension strings, jumpers and tower steelwork during sustained events. In addition, damages to spacers and stock-bridge dampers, to subconductor strands at suspension clamps and spacer clamps from fault current can also occur.

Of course, the cost of repair and the lost of revenue are also two important factors to define the risk. In several instances the losses of revenue due to gallop-induced outages have exceeded \$500,000 for a utility in one year [14].

Although this problem has been recognized for about 60 years [1,2,3,4], because of the complexity of galloping mechanism, there is no definite way to avoid it.

Before any special investigation on anti-galloping device, it is always necessary to perform an appropriate structural analysis to

Model decomposition of the function $y(z, t)$ (vertical), $x(z, t)$ (horizontal) and $\theta(z, t)$ (torsion) are given by

(horizontal) and $\theta(z, t)$ (torsion) are given by

$$y(z, t) = \sum_{k=1}^{\infty} \tilde{y}_k(t) \sin k\delta \quad (4)$$

$$x(z, t) = \sum_{k=1}^{\infty} \tilde{x}_k(t) \sin k\delta \quad (5)$$

$$\theta(z, t) = \sum_{k=1}^{\infty} \tilde{\theta}_k(t) \sin k\delta \quad (6)$$

where t represents time, L and z are span length and the distance from the beginning of the span to the point where to be studied.

k is model number. The 3-DOF conductor system with each mode k are described by

$$m\ddot{y}_k + C_y \dot{y}_k + T \left(\frac{T}{k\pi} \right)^2 y_k = -mg + F_v \sin k\delta \quad (7)$$

$$m\ddot{x}_k + C_x \dot{x}_k + T \left(\frac{T}{k\pi} \right)^2 x_k = \frac{\pi}{2} \int_{\pi}^{\pi} [F_h] \sin k\delta \quad (8)$$

$$I\ddot{\theta}_k + C_{\theta} \dot{\theta}_k + GJ \left(\frac{T}{k\pi} \right)^2 \theta_k = \frac{\pi}{2} \int_{\pi}^{\pi} [M_m] \sin k\delta \quad (9)$$

where T , the tension on the cable is given by the constitutive law which needs to consider appropriate evaluation of deformed length of the cable from tension tower (including all suspensions and spans in one section). GJ represents the torsional stiffness, and spans in one section). GJ represents the torsional stiffness, which is linear for the single conductor but highly non-linear for bundle. Bundle stiffness depends on many parameters such as tension, spacer, number of subspan and yoke plate, etc.

The angle of attack

In this line system, one of the most active factor is the angle of attack. It is defined as φ in Figure 1.

The source of the external excitations is wind. The wind velocity relative to the conductor is described by

$$v_x = V_0 \sin(\theta_0 + \theta) - \dot{x}$$

$$v_y = V_0 \cos(\theta_0 + \theta) - \dot{y}$$

Therefore the relative wind velocity is given by

$$V_r = \sqrt{[V_0 \sin(\theta_0 + \theta) - \dot{x}]^2 + [V_0 \cos(\theta_0 + \theta) - \dot{y}]^2} \quad (10)$$

where θ_0 is the angle in the original equilibrium position, generally it is the ice accretion angle θ_{ice} . V_0 and V_{0y} are the components of wind velocity. R is the radius of subconductor.

The angle of attack is described by

$$\alpha = \theta_0 + \theta - \arctan \frac{V_0 \sin(\theta_0 + \theta) - \dot{x}}{V_0 \cos(\theta_0 + \theta) - \dot{y}} \quad (11)$$

Under the basic approximation and after some analytical steps, the linearized aerodynamic excitations on the line system are described by

$$m\ddot{y} + C_y \dot{y} + K_y y = -mg + F_v$$

$$m\ddot{x} + C_x \dot{x} + K_x x = F_h$$

$$I\ddot{\theta} + C_{\theta} \dot{\theta} + K_{\theta} \theta = M_m$$

where y and x are the displacements in vertical and horizontal, respectively, θ is the torsional angle. The definition for angles and forces in this 3-DOF system is shown in Figure 1. The coefficient C_y , C_x and C_{θ} represent the damping, and K_y , K_x and K_{θ} represent the stiffness in these 3 degrees of freedom, The F_v , F_h and M_m are corresponding the external excitations on the conductor system. They are combined by the aerodynamic drag, lift and moment due to the asymmetric profile, which are written in part 2. Furthermore, m and I are the mass and the moment of inertia of the conductor's cross-section per unit length.

The basic second-order partial derivatives equations for vertical, horizontal and torsional motion can be found in the literature for cable structures [11] as the following form

$$m\ddot{y} + C_y \dot{y} + K_y y = -mg + F_v$$

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The early theory of galloping was formalized by Den Hartog [1], without taking into account the dynamic effect of torsion. Early in the eighties, Rawlins [12] already presented the linearized stability equations in 3-DOF for galloping on single conductor. Today very few developments on both stability and time response analysis have been performed on bundle conductors. Yu *et al* [7] recently published some interesting developments in the field, limited to single conductor, but including some new insights in stability analysis and time analysis.

We developed a full 3-DOF analysis on both single and bundle conductors including stability analysis, parameter analysis and time response. This development includes the appropriate modalization of bundle torsional stiffness and tension oscillation including multi-span sections. All mixing between 1, 2 and 3 loops galloping are included in our theory, together with all so called "second order" coupling terms which sometimes were neglected [3,6]. This part describes a generalization on some former developments [8,9] based on 2-DOF model after our comparison between 2-DOF and 3-DOF models [10].

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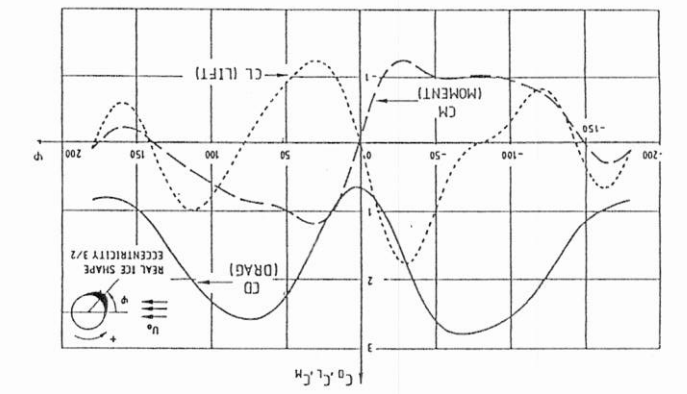
A NEW 3-DOF TRANSMISSION LINE SYSTEM

This oscillation is so called galloping.

can be so compensated that a self-sustained oscillation appears. and inversely for a downwards velocity. The drag damping effect coefficients behave that upwards velocity increases the vertical force

For some appropriate ice accretion angle θ_{ice} , the aerodynamic

Figure 2: Aerodynamic coefficients of drag, lift and moment [5]



We chose a dead-end span from a 380kV transmission line in Belgium, the span length is 234m. Its basic data are: AMS $2 \times 620mm^2$ horizontal bundle, subconductor cross section $A = 620mm^2$, Young modulus $E = 5.3 \times 10^{10}N/m^2$, mass of subconductor $m = 1.8kg/m$, subconductor diameter $\phi = 32.4mm$, sub-conductor separation $d = 0.45m$, sagging tension per subconductor $T = 30000N$, intrinsic torsional stiffness $\tau = 460Nm^2$, four identical subspans in this span.

By observation in Europe, single conductor are less sensitive to galloping than bundles. The main reason is because the torsional stiffness of single conductor is low (a few hundred Nm^2 for diameters below 35mm) than that of spaced bundle. Torsional stiffness of bundle conductors can be 20 times larger than that of single. Therefore the static analysis for torsional stiffness is very useful for transmission line design. The following example is about bundle stiffness.

Case 1

SOME SIMULATIONS

This example is based on the Norway case (in next part, case 2). The diameter ratio Q_2 in this case is 0.17. The Figure 3 shows the influence of the reduced wind speed Q_3 on the reduced vertical amplitude $\frac{\phi}{L}$ with different diameter ratio values.

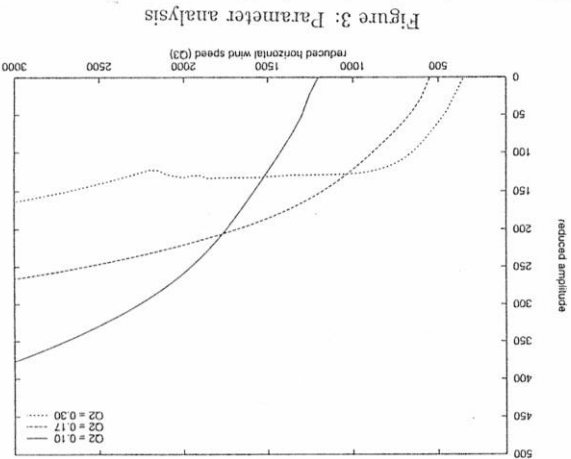


Figure 3: Parameter analysis

An example on the reduced wind speed

experimental observations by [12]. Q_5 , obtained from the theory, mixed two parameters obtained by first time that Q_2 and Q_3 are presented in the literature. In fact physical parameters are introduced in the former parts. This is the and conductor, respectively. L is the span length. The other basic without ice nor wind, ρ_c and ρ_i represent the mass density of ice where d is the subconductor separation, f_v is vertical frequency

- Synchronizing $Q_1 = \frac{\omega_b}{\omega}$
- Diameter ratio $Q_2 = \frac{d}{2\phi}$
- Reduced wind speed $Q_3 = \frac{V_0}{V}$
- Reduced ice density $Q_4 = \frac{\rho_c}{\rho_i}$
- Cable span parameter $Q_5 = \frac{L^2 m g}{\phi^2 T_0}$

galloping parameters:

relations necessarily connecting the structural parameters of transmission line, wind and ice to galloping are found by the following conductor, which is based on experimental results, the specific re-

Based on some analysis from the literature [12] about single the aspects of wind effect, structural effect and ice effect.

tions should be reduced from manipulation, generally according to simple as possible, the basic parameters and coefficients of equation order to get parameters with significant physical meaning while as others and some of them have no significant physical meaning. In (3-DOF system). But by this way, there will be so many parameters. The easiest way is to simply get back all coefficients from Eq.(15) write down the the instability criteria of linearized system with different steps. Generally it has to be done in different steps.

The best way to define galloping parameters is to be able to analysis should be done. physical parameters which influence galloping, a specific parameter bundle orientation, etc. In order to discover the most important type and number of spacers, sag-span ratio, yoke plate dimension, of cable, span length, subconductor diameter, bundle geometry, The basic important parameters of transmission lines are: type

PARAMETER ANALYSIS

obvious in this system.

and torsional modes. The aerodynamic damping terms are also terms including the second order ones between vertical, horizontal theore. From this line system, it is clearly to see the coupling ice position along the span, this is also very different from former over Eq.(14) takes into account the non-uniform distribution of here), which are linearized around the equilibrium position. More- by taking into account tension variation (not explained in detail a full non-linear description of GL , the torsional stiffness, ω_b and ω_i It is very similar to the system obtained by [12] but including

$$\begin{pmatrix} \Delta \ddot{y} \\ \Delta \ddot{x} \\ \Delta \dot{\theta} \end{pmatrix} = \begin{pmatrix} -\frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a \\ -\frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a \\ -\frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a \end{pmatrix} + \begin{pmatrix} \omega_2^2 & 0 & 0 \\ 0 & \omega_2^2 & 0 \\ 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} \Delta y \\ \Delta x \\ \Delta \theta \end{pmatrix} + \begin{pmatrix} \frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a & -\frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a & -\frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a \\ -\frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a & \frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a & \frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a \\ \frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a & -\frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a & -\frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a \end{pmatrix} \begin{pmatrix} \Delta y \\ \Delta x \\ \Delta \theta \end{pmatrix} + \begin{pmatrix} -\frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a & \frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a & \frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a \\ \frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a & -\frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a & -\frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a \\ \frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a & \frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a & -\frac{m}{K} \ddot{y}_a \ddot{C}_L \omega_a \end{pmatrix} \begin{pmatrix} \Delta y \\ \Delta x \\ \Delta \theta \end{pmatrix}$$

mode k is obtained in matrix form by Therefore, the 3-DOF linearized conductor system with each respectively.

where Ψ represents $C_D, C_L, C_M, C_{D\alpha}, C_{L\alpha}, C_{M\alpha}, \sin \theta_0$ and $\cos \theta_0$,

$$\underline{\Psi} = \frac{\pi}{2} \int_0^{\pi} \Psi \sin^2 k \delta \delta \delta$$

The modified aerodynamic coefficients are given by dynamic coefficients of the drag, lift and moment to φ respectively.

where $C_{D\alpha}, C_{L\alpha}$ and $C_{M\alpha}$ are the first order derivatives of aerodynamic coefficients of the drag, lift and moment to φ respectively.

$$+ V^2 \begin{pmatrix} \Delta F_x \\ \Delta F_y \\ \Delta M_w \end{pmatrix} = V_0^2 \begin{pmatrix} K_D(C_{L\alpha} - C_D) & -2K_D C_L & -K_D C_{L\alpha} \\ K_D(C_{D\alpha} + C_L) & -2K_D C_D & -K_D C_{D\alpha} \\ K_M C_{M\alpha} & -2K_M C_M & -K_M C_{M\alpha} \end{pmatrix} \begin{pmatrix} \Delta y \\ \Delta x \\ \Delta \theta \end{pmatrix}$$

$$\begin{pmatrix} \Delta F_x \\ \Delta F_y \\ \Delta M_w \end{pmatrix} = V_0^2 \begin{pmatrix} K_D(C_{L\alpha} - C_D) & -2K_D C_L & -K_D C_{L\alpha} \\ K_D(C_{D\alpha} + C_L) & -2K_D C_D & -K_D C_{D\alpha} \\ K_M C_{M\alpha} & -2K_M C_M & -K_M C_{M\alpha} \end{pmatrix} \begin{pmatrix} \Delta y \\ \Delta x \\ \Delta \theta \end{pmatrix}$$

In order to evaluate the torsional stiffness, we apply a static torque at the mid-span. Torsional stiffness can be then got from the rotation angle. The simulation and the experiment results are shown in Figure 4.

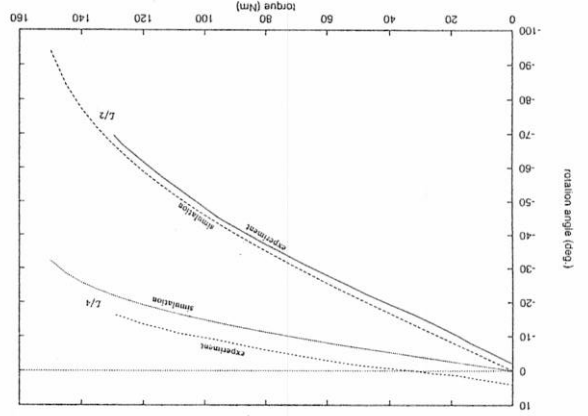


Figure 4: Bundle rotation angles

The experiment is performed by Laborelec (the Belgian laboratory for power plants and networks). Because this model takes into account the tension variations between subconductors which has not been considered by the existing theory [13], and these tension variations may increase bundle stiffness more than 50% in some cases, the results of rotation angles at both mid-span and a quarter agree very much with the experiment. It is also clearly to see that the torsional stiffness will not be linear when the rotation is large.

Case 2

For galloping mechanism study and special investigation on anti-galloping device, it is always necessary to perform some simulations under appropriate meteorological conditions to see the galloping behavior and point out the effects of some basic choices on galloping phenomena. There is an important 420kV transmission line in Norway, where galloping occurred before. With this line there is a section of two spans between the anchoring towers. The span length is 292m and 196m respectively. Its basic data are: Horizontal twin bundle, subconductor cross section $A = 863.10mm^2$, Young modulus $E = 7.0 \times 10^{10} N/m^2$, mass of subconductor $m = 2.879kg/m$, subconductor diameter $\phi = 38.25mm$, subconductor separation $d = 0.45m$, sagging tension per subconductor $T = 50802.07N$, intrinsic torsional stiffness $\tau = 530N/m^2$. 15 spacers per span are chosen in this case.

Galloping will occur after a short time under the following external conditions:
 $V_0 = 15m/s$
WIND
 $\theta_{ice} = 50^\circ$
 $\epsilon = \frac{3}{1}$ (ice thickness = 6mm)

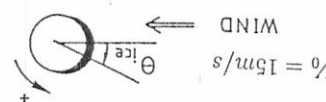


Figure 5 gives the view of galloping in vertical from rising galloping to getting into the limit cycle, i.e. steady galloping. Figure 6 to 8 detail time evaluation at mid-span during steady galloping, by which we can find galloping amplitudes in vertical and horizontal, and torsional angle. It is also important to see the limit cycle shape at mid-span, i.e. galloping ellipse which is shown in Figure 9. This is very useful in establishing phase clearances. By analysis these results we can find this galloping is "up-down" type, and galloping frequencies can be also found from Fourier analyses.

Mechanical aspects are also very important to be considered for long distance power transmission lines of HVAC and HVDC. The phenomena of galloping can cause a lot of problems by both its electrical consequences (flashover between phases at each cycle of oscillation, i.e. once every 5 seconds) causing generally a definitive tripping out of the line for a long period of time, and mechanical damage. Anti-galloping devices are widely used as a method to avoid galloping. The comprehensive mathematical model is the foundation for performing structural

CONCLUSIONS

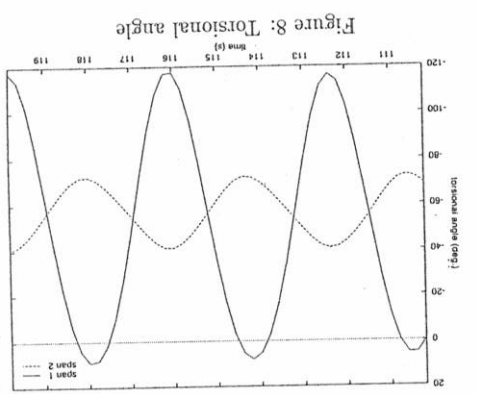


Figure 8: Torsional angle

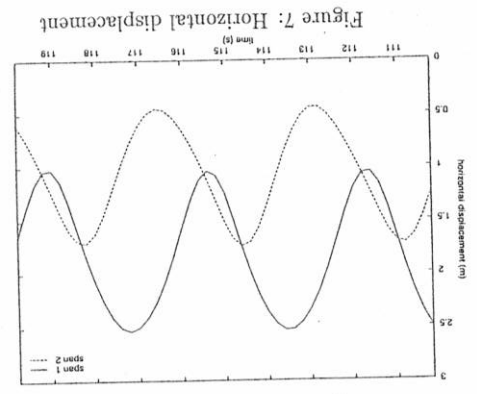


Figure 7: Horizontal displacement

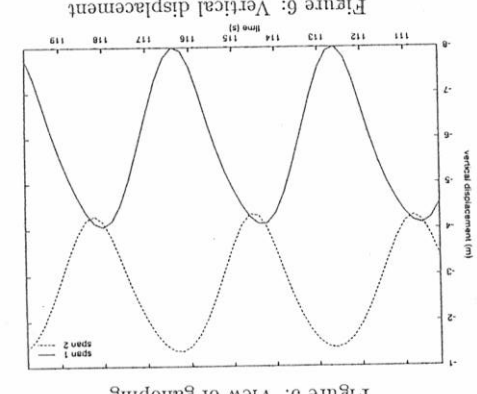


Figure 6: Vertical displacement

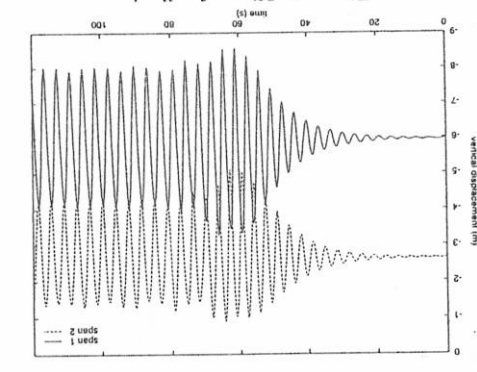


Figure 5: View of galloping

Oliver Chabart was born in Seoul, Korea, on December 10, 1970. He received his degree in electrical and mechanical engineering from the Department of Electrical Energy at the University of Liège in 1993. He is presently a research engineer in the Transmission and Distribution of Electrical Energy at the same University.

Pol Pirlet was born in Saint Georges, Belgium, on December 27, 1936. He received his degree in electrical engineering from the University of Liège in 1960. After one year in Canada he received the M.S. degree from Laval University and his Ph.D degree from the University of Liège in 1972. He is presently full professor in charge of the Transmission and Distribution of Electrical Energy branch.

He is convener of the 36-01 CIGRE Working Group (corona and fields). He is involved in the organization of the CIGRE Conferences in England and Belgium every two years since 1971.

He has published over eighty technical papers in T and D fields. He is Senior Member in IEEE.

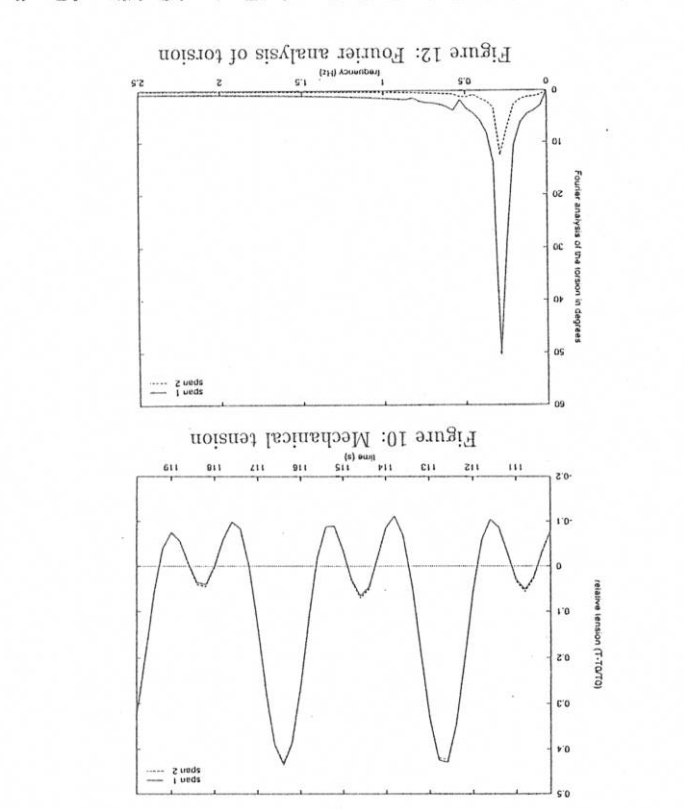
Jianwei Wang was born in Henan, China, on January 21, 1963. He received the B.S. degree from Zhengzhou Institute of Technology and the M.S. grade diploma from Southeast University, China, in 1985 and 1991 respectively, both in electrical engineering.

From 1985 to 1991 he worked as a teaching assistant and a lecturer in the Electrical Engineering Division at Nanjing Institute of Chemical Technology, China. In 1992 he joined the Department of Transmission and Distribution of Electrical Energy at the University of Liège as a researcher. He is presently working toward the Ph.D degree in the field of Overhead Lines Galloping at the same University.

He was an expert of the CIGRE working group 23-02 (high current in substations) for ten years. He is now an expert of the task force on galloping, a part of the CIGRE working group 22-11. He participated to more than 20 international symposiums or congress and has published over forty technical papers. He received the international prize *George Montflore* in 1986.

Jean-Louis Lillen was born in Liège, Belgium, on May 24, 1953. He received his degree in electrical and mechanical engineering in 1976 and his Ph.D degree in 1984 from the University of Liège. He is presently a *Chef de Travaux* in the Department of Transmission and Distribution of Electrical Energy at the same University and a consulting engineer for SAMTECH, a Belgian consultant firm. His main activity is based on the non-linear behavior of cable structures in power systems.

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analysis for investigations on anti-galloping devices. A new 3-DOF mathematical model is detailed in this paper. This model takes into account the second order coupling factors between vertical, horizontal and torsional modes. It can effectively explain some behaviors for both single and bundled conductors, such as bundle stiffness, tension distribution, etc. Indeed, it can be then used for modeling of galloping by simple approach. The specific galloping parameters are also defined by which the most important physical parameters which influence galloping can be found by a simplified method. Several simulations with two real cases are performed. The results of the simulation on torsional stiffness perfectly agree with the experiment. General behaviors of galloping are simulated in a multi-span transmission line. The galloping amplitude in every DOF, tension oscillation, galloping ellipse and so on are also important informations for overhead transmission lines design.